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Finite Element Method in Machining Processes

 Springer

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Preface

The finite element method is a powerful tool with applications in many industrial sectors. Manufacturing and especially machining is not an exception. Since the early 1970s it has provided valuable information on fundamental understanding of the material removal process but more importantly predictive models that can provide reliable results on many machining parameters. As a modeling method it has proven superior and by far more versatile than any other. The vast number of publications, pertaining to machining, and finite element analysis, proves it.

This Springer Brief aims to provide information on the modeling of machining processes by the finite element method. In Chap. 1 an introduction to machining and especially metal cutting is provided. Some basic features of turning, milling, and drilling are discussed and the terminology that is used throughout the book is introduced. Chapter 2 gives a description of orthogonal and oblique cutting, two schemes very popular among the machining researchers. A discussion on analytical modeling of machining is provided in this chapter. Shear plane, Slip-line field, and shear zone models are discussed. This is a helpful introduction to machining modeling. Chapter 3 is dedicated to finite element method. The features to be implemented in a FEM model are described and the most popular approaches are discussed. In this chapter, numerical formulation, mesh, elements, boundary conditions, and contact considerations are analyzed. Furthermore, material and friction modeling are considered and a discussion on chip separation and breakage criteria and adaptive meshing is provided. From all these numerical considerations and the research conducted so far it may be said that there is not a single solution that is acceptable on how the “perfect model” looks like. The search goes on with new ideas and better tools. The researchers’ arsenal stores better understanding of machining, more powerful computers, and special software. At the end of this Chapter a bibliographical review is provided along with a brief presentation of commercial FEM software. Chapter 4 is the part of the book where examples of finite element models are given. Three areas, namely high speed machining, 3D modeling, and micromachining, are selected. For each area, a discussion on the work done so far and how the models overcome problems that may arise is provided. Chapter 5 is the last one, where the modeling techniques for other

machining operations are described. More specifically, grinding is considered here and a paragraph for non-conventional machining and machining of composite materials is squeezed in. Furthermore, soft computing techniques, molecular dynamics, and meshless methods for machining are presented.

The book is by no means complete, in the sense that for every topic included a lot more can be added. The reader who starts now to get acquainted with FEM models of machining can raise his awareness of what lies ahead of him. The experienced user may review the advancements through all the past years and get new ideas to move on or use it as a reference book.

I would like to thank Professor J. Paulo Davim, Editor of SpringerBriefs Series in Manufacturing and Surface Engineering for his invitation and the trust he put in me to accomplish the task of writing this book, and Professor D. E. Manolakos for his support and valuable advice. I would also like to thank Miss. Quinn from Springer for her assistance and prompt answers. Finally, I thank my family and especially my wife for being so patient with me.

Angelos P. Markopoulos

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Chapter 1

Machining Processes

1.1 Introduction

Surveys indicate that 15 % of all mechanical components value, manufactured in the world, comes from machining operations and that annual expenditure on machine tools and cutting tools are several billion € for industrially developed countries [1, 2]. Although the available data are from some years ago, increasing trends are indicated and are likely to be sustained until today. If labor, machinery, tools and materials costs, social impact from employment in machining related jobs and technological developments becoming available from machining advances are considered, then the importance of machining and its impact on today's industry and society is obvious.

Trends in manufacturing technology are driven by two very important factors, which are closely interconnected, namely better quality and reduced cost. Modern industry strives for products with dimensional and form accuracy and low surface roughness at acceptable cost; an extreme paradigm being micromachining of miniaturized components. From an economic point of view, machining cost reduction achieved through the increase of material removal rate and tool life without compromising surface integrity even for hard-to-machine materials is highly desirable, e.g. turning of hardened steels by CBN tools at increased speeds or as it is usually referred in the literature High Speed Hard Turning. Understanding chip formation mechanisms and predicting cutting forces are of the greatest importance on realizing both the above goals and one way to achieve this, probably the most used one, is modeling.

Machining of metals, although is one of the oldest and very important manufacturing process, has been subjected to systematic study for a little more than a century. Almost for the second half of this time period, studying of metal machining is accompanied by modeling methods. The initial objective of studying and modeling metal machining was to provide a theory which, without any experimental

work, would enable researchers to predict cutting performance and thus solve practical problems confronted in industry. The first analytical models set the basis for more advanced methods developed later in the course of time and when the tools for realistic computational cost and analysis time became available with computer advances. Analytical models supported by metal cutting mechanics and with simplifying assumptions began publishing around 1900s. However, it was not until the 1950s that modeling of machining became a key tool used for understanding the mechanisms of material removing process as well as predicting their performance.

In the early 1970s some pioneering works on machining modeling with the Finite Element Method (FEM) begun to find their way in scientific journals. Over the years and with the increase of computer power as well as the existence of commercial FEM software, this method has proved to be the favorite modeling tool for researchers of the field. This is established by the vast number of publications on this subject as well as the modeling novelties introduced and used, even by the fact that software dedicated solely for the purpose of modeling machining operations exist; more details on the above subjects only marginally discussed here will be presented in [Chaps. 3](#) and [4](#). Finite element models are used today for gaining knowledge on fundamental aspect of material removing mechanisms but more importantly for their ability to predict important parameters such as cutting forces, temperatures, stresses etc. essential for the prediction of the process outcome, the quality of the final product and in a timely and inexpensive way. The requirements for performing such a task are many; theoretical background, manufacturing experience, accurate data and knowledge on modeling are supplies for building a model and interpreting its results.

In this Book an effort to provide a guide on the modeling of machining is attempted. Firstly, machining processes and some important features such as basic terminology and tool geometry that are important for modeling are discussed in [Chap. 1](#). In [Chap. 2](#) an analysis on some benefits as well as limitations of modeling in general and the requirements of machining modeling in particular is briefly argued. Then, in [Chap. 3](#), some important features of mechanics of machining and analytical modeling attempts are described. The most extended part of this book is the subject of FEM modeling of machining which includes various discussions on FEM formulation, material modeling, friction and FEM software among others. [Chapter 4](#) includes case studies to exemplify the use FEM in machining and in various processes in 2D and 3D problems as well as literature review and further reading suggestion, wherever this is needed. The results of the analyses are discussed and useful conclusions are drawn. Some special cases of state-of-the-art machining processes and their peculiarities are also provided. Finally, in [Chap. 5](#), some other modeling methods, besides FEM, that are currently used for modeling and simulating machining are discussed.

1.2 Machining Processes: Metal Cutting

By the term *machining*, processes that shape parts by removing unwanted material, are described. The part being machined, usually called workpiece, can be metallic or non-metallic, i.e. polymer, wood, ceramic or even composite, however, machining of metals will be discussed hereafter. Unwanted material is carried away from the workpiece usually in the form of a chip; evaporation or ablation may take place in some machining operations.

The more narrow term *cutting* is used to describe the formation of a chip via the interaction of a tool in the form of a wedge with the surface of the workpiece, given that there is a relative movement between them. These machining operations include turning, milling, drilling and boring among others and are usually referred as traditional machining processes. Abrasive processes such as grinding are also part of cutting processes of great importance in contemporary industry. Other non-traditional machining operations that may or may not include physical contact between cutting tool and workpiece or may not have a cutting tool in the same sense as traditional processes or utilize thermal or chemical energy for removing material from workpiece, are ultrasonic machining, water jet machining, electro discharge machining, laser machining and electrochemical machining just to name some.

Traditional machining operations and more specifically turning, milling, drilling and grinding will be discussed in the at hand book. These processes were selected as FEM bibliography pertaining to these processes is more extended than others. Although these machining processes exhibit a lot of differences which will be briefly presented below, a physical analysis including orthogonal and oblique cutting can be used to describe them.

Before moving on to modeling, a brief description of turning, milling and drilling is provided; grinding is discussed individually in [Chap. 5](#). There are many variations of these processes but is out of the scope of this paragraph to describe all of them. Only some geometrical and kinematic features of the processes involved in modeling discussed later on needs to be clarified here. The interested reader is encouraged to search for more details on manufacturing processes in general and machining in particular and some excellent books are proposed [[1](#), [3](#) [9](#)].

1.2.1 Turning

Turning is a process of removing excess material from the workpiece to produce an axisymmetric surface, using a single-point tool. In [Fig. 1.1](#) the general case of cylindrical turning is depicted. The workpiece is rotated at a work speed provided by the machine tool (lathe), which is the cutting speed at which cutting is performed. In order to perform the material removal operation, the workpiece is advanced along the feed direction and a cylindrical surface is generated. Generally speaking, feed is defined as the displacement of the tool relative to the workpiece in the direction of feed motion per revolution or per stroke of the workpiece or

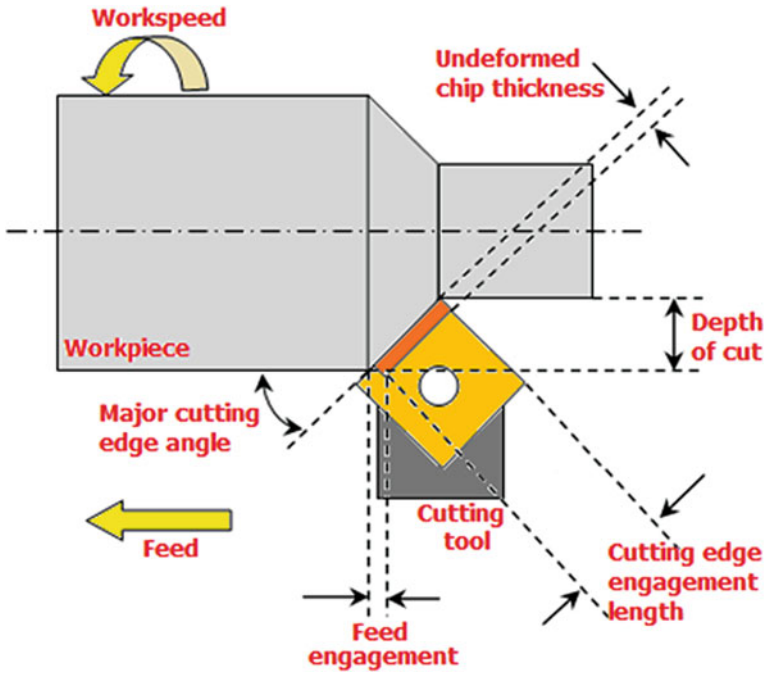


Fig. 1.1 Cylindrical turning

tool. In particular, in turning, feed is the distance that the tool advances in each workpiece revolution. For single-point cutting tools the feed is equal to the feed engagement, the instantaneous engagement of the workpiece and the cutting tool edge. The darker area on the cutting tool in Fig. 1.1, is the cross section of the uncut chip. The undeformed chip thickness in turning a_c , can be calculated through feed f and the major cutting edge angle κ_r , by equation:

$$a_c = f \sin \kappa_r \quad (1.1)$$

The difference between the radius of the uncut workpiece and the machined workpiece is the depth of cut. The cutting tool contacts the workpiece along the cutting edge engagement length. It is obvious that for the case that the major cutting edge angle is 90° , the feed is equal to the undeformed chip thickness and the depth of cut is equal to cutting edge engagement length; the product of feed by depth of cut is the cross-sectional area of the uncut chip.

Turning cutting tools are also characterized by a rake and clearance angles at the tool edge. The rake angle is the inclination of the top face of the cutting edge to the surface being machined. The rake angle can be positive, usually for ductile materials, or negative, for high strength materials. The cutting edge also possesses side and front clearance angles to ensure that there is no contact of the major and minor flanks of the tool with the machined surfaces; if there was contact the

surface integrity of the already machined surface would degrade. Finally, turning tools have a nose radius incorporated between the major and minor cutting edges. After milling and drilling are described some notes on the terminology and special characteristics considering cutting tools are given.

1.2.2 Milling

Milling has many different variants thus allowing for a wide variety of shapes to be processed, involving the machining of horizontal, vertical and inclined surfaces through horizontal or vertical milling machines. In Fig. 1.2, face milling, a process that can be utilized to machine profiles, pockets and slots, is depicted.

The workpiece is reduced in height by an amount equal to the axial depth of cut, over a width equal to the radial width of cut. The feed is the distance that the cutter advances across the workpiece per revolution. In milling the cutting tool has many cutting edges; in the case of Fig. 1.2, the cutting edges are four. Each cutting edge has a major cutting edge angle and creates a chip. For this multi-point tool, material removal is performed by the clockwise rotation of the tool. Cutting edge A located in point 1, in the specific time frame depicted in Fig. 1.2, enters the workpiece and starts creating the chip. This cutter will leave workpiece in point 2, having created a chip with an increasing thickness. Cutter B is already removing material while cutter D is the next in turn to continue this process. If the cutting tool, with cutters facing the opposite side, was rotating anticlockwise and thus entering at point 2 and leaving at point 1, the chip thickness would decrease with the edge's travel. For milling an average undeformed chip thickness can be determined. The difference between the minimum and maximum undeformed chip thickness depends on the cutting conditions.

1.2.3 Drilling

In this process a multi-point tool is used with the aim to create a hole. In Fig. 1.3, depicted is a tool with two flutes, therefore two cutting edges that is rotated and fed downwards along its axis of rotation. Drilling is a multi-point tool process, like milling, but each cutting edge is continuously engaged with the workpiece creating a chip, like turning. Each cutting edge is characterized by the major cutting edge angle of the tool. The tip of the drill is a chisel that advances inside the workpiece, pushing the material to be removed by the cutting edges.

The maximum cutting speed is reached in the outer radius of the major cutting edges and decreases to almost zero in the drill's center. The depth of cut of the process is the radius of the hole being drilled. The axial feed in drilling is expressed as feed per revolution.

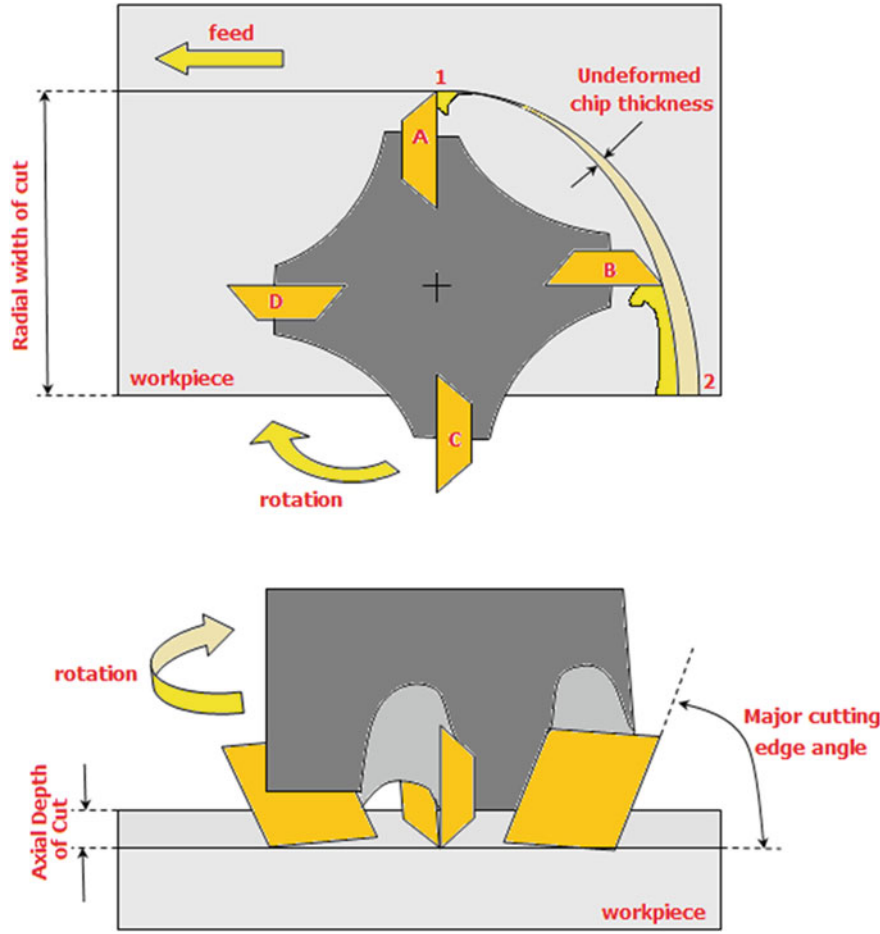


Fig. 1.2 Face milling

1.2.4 Discussion on Cutting Processes and Chip Formation

The brief description of turning, milling and drilling reveals the differences that they exhibit. However, it is more important for modeling to identify the similarities that allow for a unified approach. In Table 1.1, some chip formation terminology that is used in all three processes and the alternative term for each process is provided.

The terms described in Table 1.1 can be the same or different in every process but their overall effect is equivalent. An example is the feed which in turning and drilling is the distance travelled by the cutting edge per workpiece revolution, while in milling it refers to the distance travelled by the workpiece per cutting

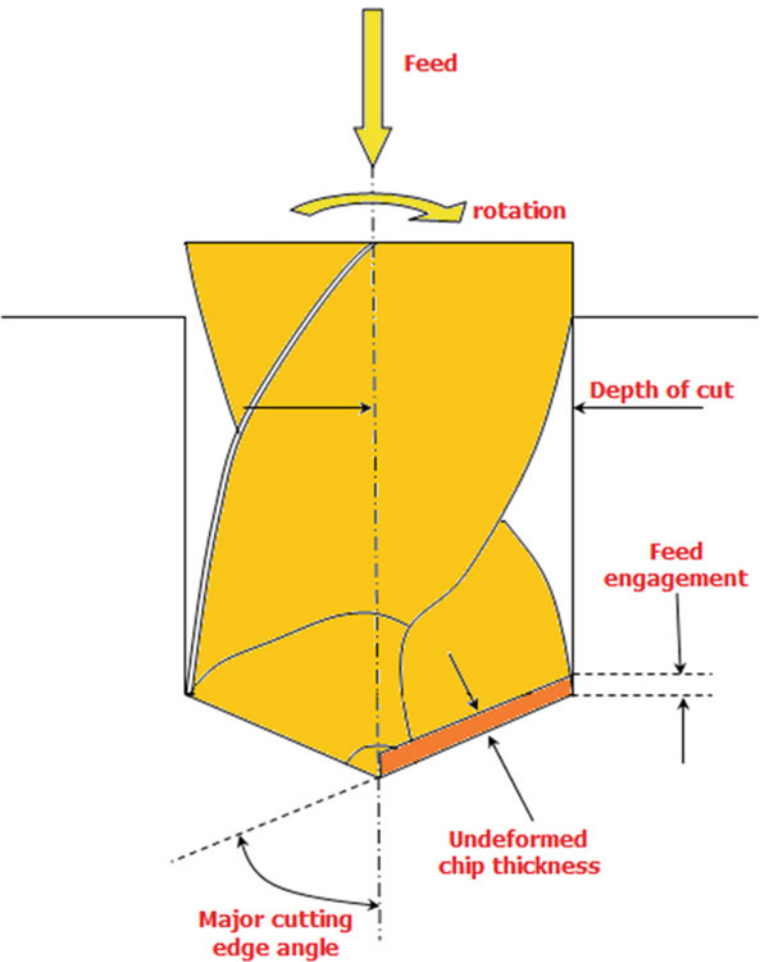


Fig. 1.3 Drilling

Table 1.1 Chip formation terminology for turning, milling and drilling [2]

Term	Turning	Milling	Drilling
Rake angle	Side rake angle	Radial rake angle	Rake angle
Major cutting edge angle	Approach angle	Entering angle	Point angle
Feed	Feed per revolution	Feed per edge ^a	Feed per revolution
Depth of cut	Depth of cut	Axial depth of cut	Hole radius

^a In milling besides feed per edge, feed per minute or feed per tool revolution can be also used

edge. However, the relative movement between the cutting tool and the workpiece in order to create the chip is described in every case.

In turning, the case of the major cutting edge angle being 90° was described; it was concluded that feed and depth of cut are equal to the undeformed chip thickness and the cutting edge engagement length respectively. The former parameters refer to the machine tool movement while the latter to the chip and the way it is formed. It is usual to consider these terms that coincide in every case, although, this is not true, e.g. milling. For further reading on cutting tools, two books are recommended [10, 11].

Depending on the cutting conditions and workpiece material, different kinds of chip may be produced. The three basic types of chip that are typically encountered in metal cutting are continuous chip, continuous chip with built-up edge (BUE) and discontinuous chip. However, besides these basic chip types, another chip type is observed, namely the segmented chip. This was documented later than the previous three because it mainly occurs at higher cutting speeds and when machining difficult-to-machine materials, e.g. titanium alloys; machining at high speeds or machining the above mentioned materials was realized by the development of advanced cutting tools.

Continuous chip is observed when cutting ductile materials at high speeds. The chip is detached from the workpiece through shearing in front of the cutting tool in a zone referred to as primary deformation zone. The chip slides on the tool face and is deformed again; this area is known as the secondary deformation zone. Although continuous chip is associated with low cutting forces, long chip or curling of the chip are not desirable as they increase forces and worsen surface finish; in this case tools with chip breakers are used. In the second kind of chip, BUE is usually formed when ductile materials are machined at low cutting speeds. BUE is material piled up on the cutting edge, resembling the case of cutting with a blunt tool; BUE is associated with increased cutting forces and influences tool wear and surface finish. BUE may be removed with speed increase. Discontinuous chip usually occurs when machining brittle materials or ductile materials at very low speeds due to severe strain from the process. The chip breaks into small parts in the primary deformation zone, when the chip is only partly formed. The serrated or segmented chip, also referred as “shear localized”, results in increased chip velocity, chip-tool friction and temperatures at the rake face of the tool that consequently provoke significant wear and tool life reduction. Although it is generally accepted that chip segmentation is energetically favorable, tool wear issues exist. However, tool life can be prolonged by optimizing cutting parameters, cutting conditions and machining strategy.

Most of the modeling work performed in machining pertains to continuous chip formation. It is considered the simplest type of chip formation, essentially under steady-state process conditions. However, models of the other chip types exist and will be discussed.

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Chapter 2

Cutting Mechanics and Analytical Modeling

2.1 Questions and Answers on Machining Modeling

Prior to the description of the most important modeling methods and their features, it would be helpful to introduce some questions that may come to mind of those who want to use modeling, and attempt to give answers. Although some answers are already given in the previous chapter, a more elaborated approach is presented in this section. The questions raised apply to all kinds of modeling; the answers mostly concern FEM, without excluding all the other methods. In the next chapter some more questions and answers, this time solely for FEM, will be presented.

A first question would be: *what is modeling and what is simulation?* A model can be defined as an abstract system which is equivalent to the real system with respect to key properties and characteristics, and is used for investigations, calculations, explanation of demonstration purposes, which would otherwise be too expensive or not possible. A model permits general statements about elements, structure and behavior of a section of reality. Simulation is an imitation of a dynamic process in a model in order to obtain knowledge which can be transferred to reality. Both definitions, for model and simulation, are quoted from Ref. [1]; the former is from Brockhaus while the latter from VDI Guideline 3663.

An obvious question that may occur or has occurred to everybody reading this text would be: *Why model machining? What is the benefit coming out of this task?* Today, most of the researchers dealing with machining modeling perform it for its predictive ability. Important parameters of machining such as cutting forces, temperatures, chip morphology, strains and stresses can be calculated before actually any cutting is performed on a machine tool. The trial-and-error approach is far more laborious, costly and time-consuming. With modeling, resources are spared, optimization is achieved and cost is reduced. The above do not mean that experimental work is obsolete, since in most cases a validation of the model is needed and the only way to provide it is to actually test model results in real conditions and make comparisons. However, modeling reduces experimental work

considerably. Furthermore, modeling and experiments add to the understanding of fundamental issues of machining theory. This forms a feedback loop vital for machining research since better understanding of the processes results in better models and so on. After all “understanding is the next best thing to the ability to predict” [2]. In a keynote paper by CIRP [3] two different “traditional schools” in machining modeling were identified, namely the one that treats modeling as an engineering necessity and another that treats modeling as a scientific challenge. On the long run both have to produce accurate models for the benefit of industry.

Who is, then, interested in machining modeling operations? The answer is the academia and the industry since there are benefits for both and the one depends on the other.

All these benefits are important and it seems that modeling is the solution for many problems. One may ask: *what are the drawbacks?* The answer is that it is the difficulties rather than the drawbacks that explain why modeling is not a panacea. The question could be rephrased to: *why is it difficult to model machining?* The answer lies in the fact that there are too many variables that need to be taken into account. First of all, there are a lot of machining operations and even though similarities do exist, many factors that are case sensitive make the proposal of a universal model not realistic. Even the orthogonal cutting system and shear plane models that are widely used are under criticism, as will be discussed in the next chapter. In the previous chapter a concise description of some machining operations was given in order to point out the similarities and differences that need to be accounted for in modeling, and that is only for traditional machining operations.

Secondly, difficulties arise from the fact that machining is still one of the least understood manufacturing operations. Machining typically involves very large stresses and strains in a small volume and at a high speed. The mechanisms of chip formation are quite complex, leading to equally complex theories and models that represent these theories. It is true that models always include simplifications in order to adequately embody theory but the danger of oversimplification is lurking. The result would be either inaccurate and thus erroneous results or models applicable for only very specific and confined cases. It should be noted that any kind of model is always applicable within the extremes of its input data. However, the area of application must be as wide as possible in order to have practical use. The mechanics of metal machining are briefly presented in the next paragraph. It can be observed that the application of the theory of plasticity on machining is far more complex than e.g. forming processes.

Finally, the variation of workpiece and tool properties and geometrical characteristics, machining conditions such as cutting speed, feed and depth of cut, the use of cutting fluids and the interaction of all the above in the same system increases the complexity of a model. The above are, generally speaking, the input data required to get a model started. Different input parameters will result in different output, significantly altering cutting forces, temperatures and chip morphology. In 1984 that “Metal Cutting Principles” by M. C. Shaw was published it seemed “next to impossible to predict metal cutting performance” [4], due to the complexity of model inputs and system interactions. This is where modern modeling techniques

come to fill in the gap, as it will be pointed out in Chaps. 3 and 4 that are dedicated to FEM.

After the selection of the process, the properties and characteristics of the cutting tool and the workpiece and the determination of the cutting conditions, *what else is needed to build a model?* This answer depends on the selected kind of modeling. The finite element method for example would require meshing parameters to be determined, boundary conditions to be inserted and, depending on the formulation used, maybe a separation criterion for chip creation simulation, among others. It is obvious that this question cannot be answered unless a modeling technique is first selected.

Next question would be then: *what kind of modeling should one choose?* The answer would be the one that is able to provide a reliable answer to the variable/output that it is looked for, with the available input data. There are five generic categories of modeling techniques available [1], i.e. empirical, analytical, mechanistic, numerical and artificial intelligence modeling. More complex models may require more input data; other models may not be able to predict a required parameter. Note, also, that the interest in predictive machining modeling has changed over the years due to advances in cutting technology. In the early days of metal cutting, tool wear was of utmost importance but nowadays the interest has shifted over to e.g. accuracy and determination of cutting forces, temperatures and the kind of produced chip. Furthermore, industry is interested in high speed machining and is environmentally conscious, requiring cutting fluids reduction or omission. Analytical models may predict output data, i.e. cutting forces, through equations requiring constants of workpiece material taken from databases, verified by experimental work, but the major drawback is that for out-of-the-ordinary cases no reliable results can be acquired. FEM on the other hand can perform coupled thermo-mechanical analysis but requires a considerable amount of computational power to produce accurate results. Artificial Intelligence techniques are usually simpler and faster models but provide results focused on a parameter or a specific area of the workpiece. It is true to say that the selection of the modeling technique depends heavily on information technology parameters, as well. Speaking for Finite Elements, more accurate representations of machining processes, e.g. 3D models, are coming true due to the fact that more powerful computers that can perform complicated calculation at an acceptable time are now available. Commercial software of FEM and especially for machining has qualified this technique to be the first choice for modeling machining operations, for many researchers.

Finally, *why would a model fail?* A model fails when it cannot predict accurately. However, it may also be considered not acceptable if it is not simple or fast enough for practical use. Many reasons may contribute to failure; lack of accurate input data, inadequate inclusion of all important parameters and misuse of a modeling technique are the most common reasons for that, as will be exhibited in the next chapter.

Machining technology cannot rely on the craftsmanship of technicians or time-consuming experiments in order to advance and meet the requirements of modern industry. Nowadays, machining is more science than art. A scientific approach is

required and modeling offers solutions. Modern modeling techniques, such as FEM, in close cooperation with computer advances are able to provide reliable results in a timely manner, justifying the many publications and research groups that are dealing with them.

2.2 Orthogonal and Oblique Cutting

The chip flow in all wedged-tool machining processes can be described, in theory, in a common way by two different cutting schemes termed orthogonal cutting and oblique cutting, depicted in Figs. 2.1 and 2.2 respectively. In orthogonal cutting the cutting edge of the tool is perpendicular to the direction of relative workpiece-cutting tool motion and also to the side face of the workpiece. From the relative movement of workpiece and cutting tool, a layer of material in the form of chip is removed. In order to continue removing material at a second stage, the tool is taken back to its starting position and fed downwards by the amount f , the feed of the process. Perpendicular to f , d is the depth of cut, which is smaller than or equal to the width of the tool edge. The surface along which the chip flows is the rake face of the tool. The angle between the rake face and a line perpendicular to the machined surface is called rake angle γ . The face of the tool that is near the machined surface of the workpiece is the flank face. The angle between the flank face of the tool and the workpiece is called clearance angle α . The angle between the rake face and the flank face is the wedge angle β . The sum of the three angles is always equal to 90° , thus:

$$\alpha + \beta + \gamma = 90^\circ \quad (2.1)$$

In Fig. 2.1 a positive rake angle is shown; in the same figure the direction for a positive or a negative rake angle is shown. For negative rake angles, the tools possess a wider wedge angle. As pointed out in Sect. 1.2.1, a positive rake angle is used for ductile materials since a “weaker” tool, with smaller wedge angle, will suffice to perform the cutting operation. For high-strength materials, rake angle is chosen to be negative, thereby increasing the wedge angle and creating a stronger cutting edge. However, stronger cutting edge has the disadvantage of requiring greater power consumption and needing a robust tool-workpiece set-up to compensate for the vibrations. The flank face of the tool does not participate in chip removal; it ensures that the tool does not rub on the newly machined surface and affects its quality. However, the clearance angle affects the cutting tool wear rate. If the tool’s clearance is too large it will weaken the wedge angle of the tool, whereas if too small, it will tend to rub on the machined surface.

Orthogonal cutting represents a two-dimensional mechanical problem with no side curling of the chip considered. It represents only a small fragment of machining processes, i.e. planning or end turning of a thin-walled tube. However, it is widely used in theoretical and experimental work due to its simplicity. Because of its 2D

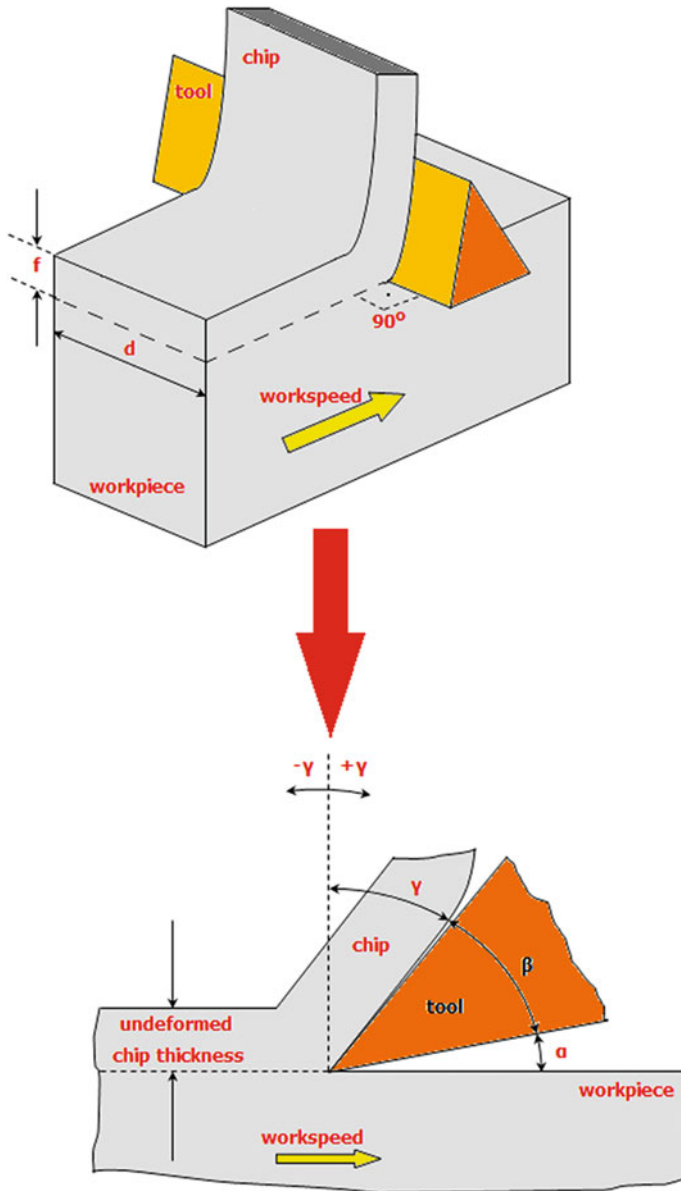


Fig. 2.1 Orthogonal cutting

nature many independent variables are eliminated, e.g. two cutting forces are only identified to orthogonal cutting problems. On the other hand, oblique cutting, where the cutting tool is inclined by angle λ , as it can be seen in Fig. 2.2, corresponds to a three-dimensional problem with more realistic chip flow representation but more

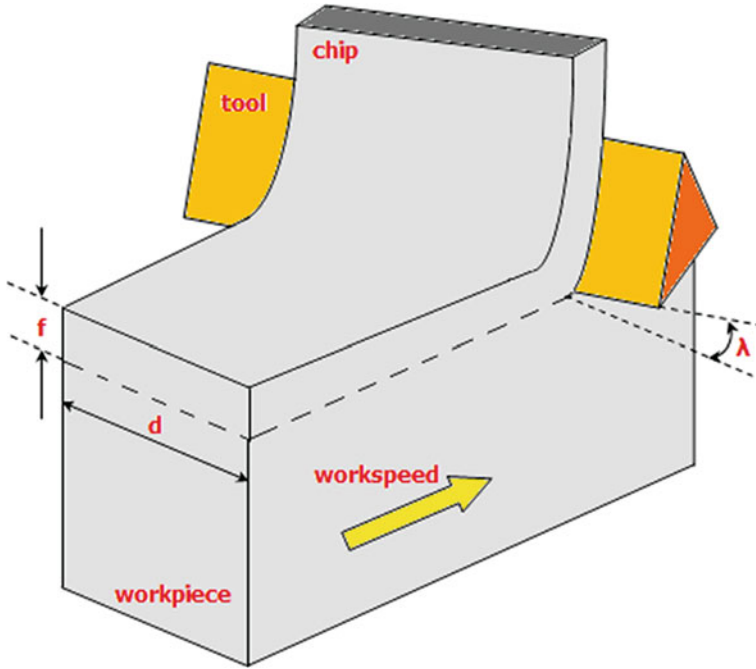


Fig. 2.2 Oblique cutting

complex analysis, i.e. three force components are present and chip curling is accounted for.

In oblique cutting that is a more general case than orthogonal, there are three mutually perpendicular cutting force components. If a coordinate system based on the directions of work speed and feed is adopted, the cutting force, the feed force and the back force are considered. The cutting force is usually the largest and back force the smallest component. For orthogonal cutting, the third force component is ignored, so the force system lies in a single plane, normal to the cutting edge of the tool. The measurement and/or the theoretical calculation of the two cutting force components as well as their resultant force have been the subject of numerous researches in the past. The importance of the knowledge of cutting forces, prior to machining if possible, is important because through these the power requirements of the machine tool, the cutting tool properties and workpiece quality are estimated. For example, if feed force is high and the tool holder is not stiff enough, the cutting edge will be pushed away from the workpiece surface, causing lack of dimensional accuracy. Furthermore, determination of cutting forces can easily lead to the calculation of other parameters, e.g. stresses.

There are two deformation areas distinguished in machining, namely the primary and the secondary deformation zones, see Fig. 2.3; the deformation zones thickness, chip thickness and shear angle are not depicted in any scale in this figure, only the locations are roughly indicated. The primary deformation zone is included in the

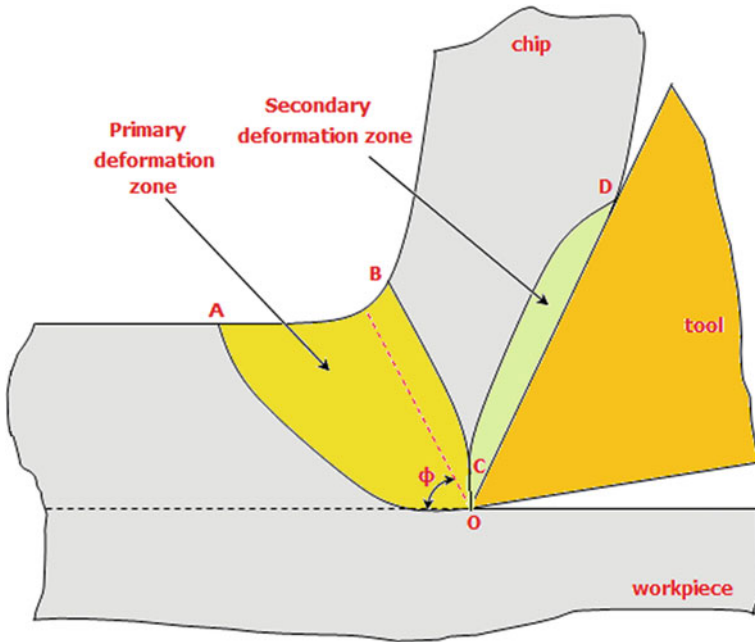


Fig. 2.3 Primary and secondary deformation zone and shear plane angle

OAB area. The workpiece material crossing the OA border undergoes large deformation at high strain rates and exits the zone at OB border, work hardened. It is determined by microscopic examination and experiments that chips are produced by shear within this region. Most of the experimental studies conclude that this zone is of average thickness of about one tenth of chip thickness [4]. The secondary deformation zone is included in OCD. Along OD, the contact length between the rake face of the tool and the chip, the material is deformed due to intensive interfacial friction. The secondary deformation zone is characterized by two regions, the sticking region, closer to the cutting tool tip and the sliding region, above the previous one [5]. In the sticking region, material adheres to the tool and as a result shear within the chip is observed. Both deformation zones are characterized by temperature rise due to severe plastic deformation in the primary and due to friction in the secondary deformation zone. Furthermore, high cutting speeds do not allow for heat conduction to take place and heat is concentrated at a small area around the cutting tool edge. Strain hardening due to deformation and softening due to temperature alter the chip formation characteristics in every step of its formation. The friction coefficient is very hard to be measured in the secondary deformation zone. Several theories are proposed for the calculation of friction, discussed in another part of this book.

A simplified approach proposes that shearing in the primary deformation zone takes place along a shear plane, characterized by shear angle ϕ , between the shear

plane and the workpiece surface. Although this single shear plane model is criticized, it is usually referred in machining handbooks due to its simplicity and it is the basis for calculating several process parameters. In any case, it is imperative to estimate shear angle and friction parameters in order to calculate cutting forces, as explained above. In the next section, an overview of the theoretical approach of machining, cutting mechanics, advances in cutting mechanics and analytical models will be discussed, before moving on to FEM analysis, since all these topics are closely connected.

2.3 Cutting Mechanics and Analytical Modeling

The history of research pertaining to metal cutting is well documented by Finnie [6] who pinpoints the work of Cocquilhat [7] in 1851 as the first research in the area of measuring the work required to remove a given material volume by drilling. However, the first work on chip formation by Time [8] in 1870 presented the results obtained when observing cutting. In this publication it was argued that the chip is created by shearing ahead of the tool. Astakhov claims that this is one of the first publication that a shear plane theory is suggested [9], probably the first being the one by Usachev in 1883 [10]. It is also shown that there is no contradiction between Time and Tresca [11]; Tresca argued that the chip in metal cutting is produced by compression ahead of the tool. Zvorykin [12] was the first to provide physical explanation for this model; his work resulted to an equation predicting the shear angle. In 1881, Mallock [13] also identified the shearing mechanism in chip formation and emphasized the importance of friction in the tool-chip interface. However, it was the work of Ernst and Merchant [14] in 1941 that made the shear plane model popular; most of the fundamental works on metal cutting mechanics reference this paper and many analytical models of orthogonal cutting still use the relations derived from this work. In the following paragraphs some key points of analytical modeling and advances in mechanics of cutting will be discussed.

Analytical models, only briefly described, are considered the predecessors of numerical models. This is by no way meant to say that numerical models substituted analytical modeling, since a lot of researchers still are working on this subject and the value of these models is paramount. It is meant to say that they have the same origins and form the basis on which FEM models and simulations are made. In another paragraph it will be discussed what the benefits, and some drawbacks as well, are from choosing numerical modeling over analytical. As it can be concluded analytical models are quite controversial and up to date there is no model universally accepted or employed. The subject cannot be portrayed in its full length within this book. However, many excellent books on mechanics of machining can be found and it is the author's opinion that they should be considered by the prospective modeler before moving on to numerical or any other kind of machining modeling [5, 9, 15 18]. These books include theory of

plasticity, slip-line theory, shear zone models and usually chapters on numerical modeling as well, among other subjects.

2.3.1 Lower and Upper Bound Solutions

Most of the analytical modeling works aim at producing equations that can determine cutting forces, without any experimental work; that is useful since other parameters can be derived by cutting forces and analysis in tool wear, surface integrity and workpiece quality can be carried out. The problem involved in the determination of the cutting forces, when the cutting conditions are known, ends up in determining a suitable relationship between the shear angle, the rake angle and the friction coefficient. Several methods have been employed that either overestimate or underestimate the results; the real value of the cutting forces probably lies between these lower and upper bounds.

Lower bound solutions employ the principle of maximum work, i.e. the deformation caused by the applied stresses results to maximum dissipation of energy. The system tends to reach the state of minimum energy compatible with the equilibrium and yield conditions. Any other statically compatible system will produce work that is either equal or less than that of the actual system.

In the upper bound solutions the strain increments of a fully plastic body rather than the stress equilibrium is considered. The principle of maximum work is employed in this case from the point of view of strain. The material is incompressible, thus the plastic volume remains constant. An element of this system deforms so that it exhibits maximum resistance. If the stresses are deduced from deformations imposed by the kinematic conditions, the estimation of their values will be equal or greater than the ones actually occurring.

2.3.2 Shear Plane Models

Shear plane models are closely connected to the theory of Ernst and Merchant, as mentioned above. This shear model was based on the so-called card model of Piispanen [19, 20]. The chip is formed by shear along a single plane inclined at an angle ϕ . The chip is straight and has infinite contact length with the tool. The shear stress along the shear plane is equal to the material flow stress in shear.

The chip is assumed to be a rigid body in equilibrium. The equilibrium refers to the forces on the chip-tool interface and across the shear plane. In Fig. 2.4 the Merchant's circle force diagram is given. All forces are shown acting at the tool tip.

The resultant force F is resolved in components F_N and F_F that are normal to the tool face the former and along the tool face the latter. It is also resolved to F_{SN} and F_S that are normal to and along the shear plane respectively. Finally, it can also be resolved into components F_c , the cutting force, and F_t the feed or thrust force. Furthermore, the rake angle γ , the shear angle ϕ and the mean angle of friction

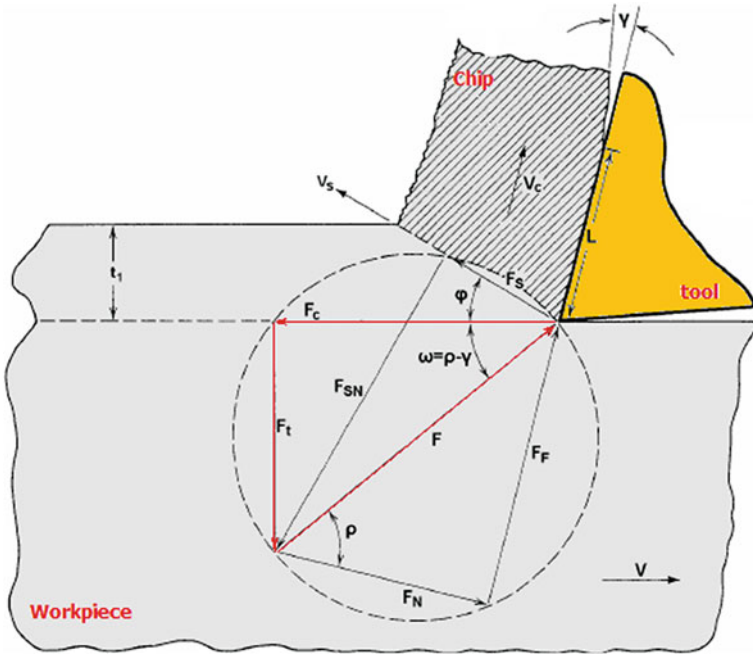


Fig. 2.4 Merchant's circle

between chip and tool ρ are shown. The friction angle ρ is related to the friction coefficient μ through equation:

$$\rho = \arctan(\mu) = \arctan(F_F/F_N) \quad (2.2)$$

According to Ernst and Merchant's theory, an upper bound one, a shear angle needs to be found that the cutting work will reduce to a minimum. In other words, since the work is proportional to the cutting force F_c , an expression of the cutting force with the shear angle needs to be found and then obtain the ϕ for which F_c is a minimum. From Fig. 2.4, it can easily be concluded that:

$$F_S = F \cos(\phi + \rho - \gamma) \quad (2.3)$$

Furthermore, the same force component can be calculated in relation to the shear strength of the workpiece material on the shear plane τ_s , the cross-sectional area of the shear plane A_S and the cross-sectional area of the undeformed chip A_C , via the following equation:

$$F_S = \tau_s A_S = \frac{\tau_s A_C}{\sin \phi} \quad (2.4)$$

Thus from Eqs. 2.3 and 2.4 it is:

$$F = \frac{\tau_s A_c}{\sin \phi} \cdot \frac{1}{\cos(\phi + \rho - \gamma)} \quad (2.5)$$

Geometrically it is deducted that:

$$F_c = F \cos(\rho - \gamma) \quad (2.6)$$

Combining Eqs. 2.5 and 2.6 it may be concluded that:

$$F_c = \frac{\tau_s A_c}{\sin \phi} \cdot \frac{\cos(\rho - \gamma)}{\cos(\phi + \rho - \gamma)} \quad (2.7)$$

If the last equation is differentiated with respect to ϕ and equated to zero, it is possible to calculate a shear angle for which the cutting force is minimum. The equation is:

$$2\phi + \rho - \gamma = \pi/2 \quad (2.8)$$

This equation agreed poorly with experimental results of metal machining. Merchant attempted an alternative solution [21]. When Eq. 2.7 was differentiated it was assumed that A_c , γ and τ_s were independent of ϕ . In the new theory, deformation and friction are reflected through a change of the force acting in the direction perpendicular to the plane of shear, thus the normal stress σ_s of the shear plane affects the shear stress τ_s . In the modified analysis a new relation is included:

$$\tau_s = \tau_o + k\sigma_s \quad (2.9)$$

This relation is known as the Bridgman relation and k is the slope of the τ – σ relation; the shear stress increases linearly with an increase in normal strength and the line intersects the shear stress axis at τ_o . With this revised theory the new result for shear angle is:

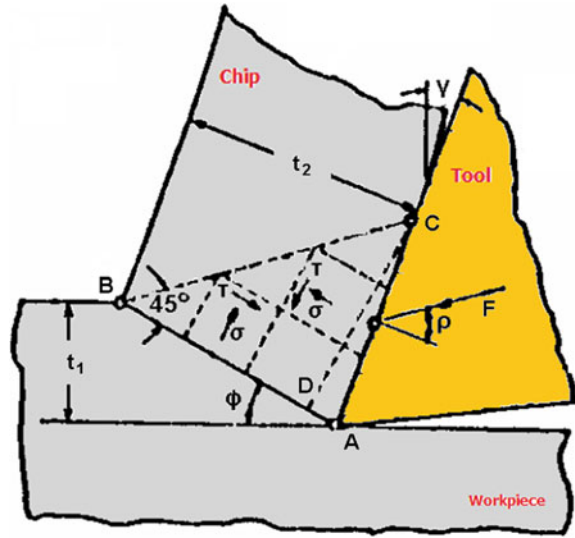
$$2\phi + \rho - \gamma = C \quad (2.10)$$

C is a constant that depends on the workpiece material.

2.3.3 Slip-Line Field Models

Stress analysis in a plane strain loaded material indicates that at any point there are two orthogonal directions that the shear stresses are reaching a maximum, but these directions can vary from point to point. A line, which generally speaking is curved, tangential along its length to the maximum shear stress is called a slip-line; a complete set of slip-lines in a plastic region forms a slip-line field. The slip-line field theory must follow rules that allow the construction of a slip-line field for a particular case. First of all, the boundary between a part of a material that is plastically loaded and another that has not yielded is a slip-line. In machining, the

Fig. 2.5 Lee and Shaffer's slip line field theory for orthogonal cutting



borders of the primary deformation zone with the workpiece on the one side and the chip on the other are slip-lines. Similarly, a slip-line is the border between the secondary deformation zone and the chip. Another rule is that slip-lines must intersect free surfaces at 45° angle.

Lee and Shaffer's work was the first contribution of the slip-line field models of chip formation [22]. It was the result of applying simplified plasticity analysis to metal cutting, more specifically to orthogonal cutting with continuous chip. It was assumed that in this plane strain conditions, the workpiece material is rigid perfectly plastic, i.e. the elastic strain is neglected during deformation and once the yielding point is exceeded deformation takes place at constant stress for varying strains, strain rates and temperatures. The constructed slip-line field is shown in Fig. 2.5.

In this lower bound solution all deformations take place in a stress field bounded by rigid bodies; this stress field transmits the cutting forces from the shear plane to the chip resulting in the triangular plastic zone ABC. In this region no deformation occurs but the material is stressed to its yield point, so that the maximum shear stress is the shear stress on the shear plane. The two directions of the maximum shear stress are indicated by the slip-lines. The shear plane AB is the one set of slip-lines because the maximum shear stress must occur along the shear plane. Furthermore, BC can be regarded a free surface since no forces act on the chip after BC, stresses cannot be transmitted from there. Thus, according to the second rule mentioned above, ABC is equal to $\pi/4$. Assuming that stresses act uniformly at the chip-tool interface, normal stresses will meet the boundary at angles ρ and $\rho + \pi/2$. Maximum shear stresses are $\pi/4$ to the direction of normal stresses and thus ACB is $(\pi/4) - \rho$. The shear angle can be calculated by equation:

$$\phi + \rho - \gamma = \pi/4 \quad (2.11)$$

It is evident that when the mean angle of friction between chip and tool is $\pi/4$ and the rake angle is zero, shear plane angle is also zero, which is not possible. Lee and Shaffer proposed a solution for this case of high friction and low rake angle, assuming built-up edge formation.

The slip-line theory was also used by other researchers who suggested curved AB and CD boundaries [23, 24]. These models reveal the non-uniqueness of machining processes; different chip shapes and thicknesses result from the same specified conditions. The non-uniqueness of the possible solutions is a significant limitation, resulting mainly by the rigid plastic workpiece material assumption.

At this point it would be interesting to make a note on the work of Zorev in relation to the slip-line field theory [5]. Zorev proposed an approximate form of the shear lines in the plastic zone as it can be seen in Fig. 2.6 on top. This is a qualitative model for which no solution is provided. However, a simplified form was proposed as shown in the same figure; in this simplified model the curved shear lines are replaced by straight ones and it is assumed that no shearing occurs along the shear lines adjacent to the tool rake face. By using geometrical relationships a generalized solution is derived as:

$$2\phi_{sp} + \rho - \gamma \approx (\pi/2) - \psi_{sp} \quad (2.12)$$

In this equation the ϕ_{sp} , the specific shear angle is introduced and ψ_{sp} is the angle of inclination of the tangent to the outer boundary of the plastic zone. The interesting about this solution is that if various values of ψ_{sp} are substituted, the shear angle relations by other researchers are derived, i.e. for ψ_{sp} equal to zero, representing the single shear plane model, the Ernst and Merchant solution is obtained, for $\psi_{sp} = C_1$ and $C = (\pi/2) - C_1$ the modified Merchant solution is obtained and for $\psi_{sp} = \rho - \gamma$ the Lee and Shaffer solution is derived.

2.3.4 Shear Zone Models

The next step in analytical modeling was to enhance some features that were neglected or simplified in previous models but play an important role in metal cutting. Most shear plane models assume that shear stress on the shear plane is uniform, no strain hardening is considered and that friction along the cutting tool-chip interface is characterized by a constant friction coefficient; this last assumption is in contradiction with experimental data. If it is assumed that deformation takes place in a narrow band centered on the shear plane, more general material assumptions can be used. The effects of yield stress varying with strain and sometimes with strain rate and temperature were considered and simplification of the equilibrium and flow was achieved. Pioneering work in this area is associated with the work of Oxley. Based on experimental data, where the plastic flow patterns are observed, it is assumed that the shear zone thickness is about one tenth of the shear zone length. Then strain rate and strain at every point in the primary deformation zone can be calculated; strain rates are derived from

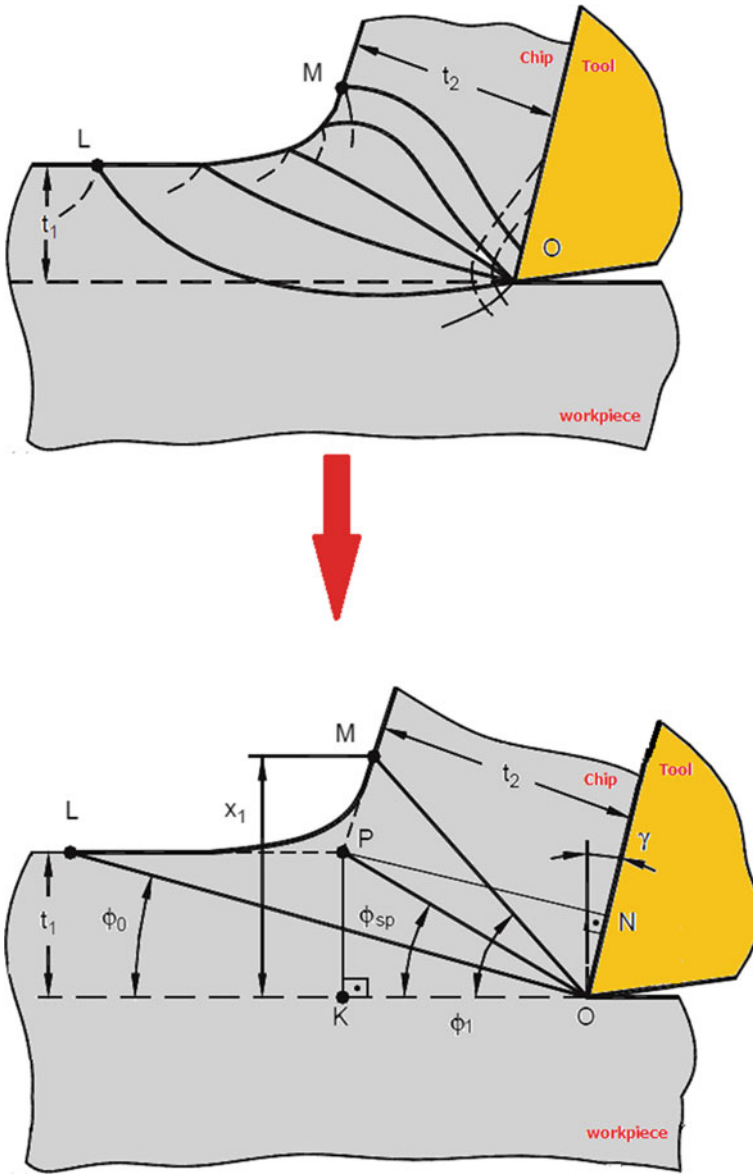


Fig. 2.6 Zorev's qualitative model on *top* and simplified model *below*

variations in the velocity with respect to the position and strains are calculated by integrating strain rates with respect to time along the streamlines of the flow. Similar assumptions are used to compute strain rates and strains in the secondary deformation zone.

Table 2.1 Shear angle formulas

Model	Formula	Year
Ernst Merchant	$\phi = \frac{\pi}{4} - \frac{1}{2}(\rho - \gamma)$	1941
Merchant	$\phi = \frac{C}{2} - \frac{1}{2}(\rho - \gamma)$	1945
Stabler	$\phi = \frac{\pi}{4} - \rho + \frac{\gamma}{2}$	1951
Lee Shaffer	$\phi = \frac{\pi}{4} - (\rho - \gamma)$	1951
Hucks	$\phi = \frac{\pi}{4} - \frac{a \tan(2\mu)}{2} + \gamma$	1951
Shaw et al.	$\phi = \frac{\pi}{4} - (\rho - \gamma) \pm \eta$	1953
Sata	$\phi = \frac{\pi}{4} - \gamma \pm \frac{\gamma}{2} \frac{15^\circ}{\gamma}$	1954
Weisz	$\phi = 54.7^\circ - (\rho - \gamma)$	1957
Kronenberg	$\phi = a \cot \left[\frac{e^{\mu \left(\frac{\pi}{2} - \gamma \right)} - \sin \gamma}{\cos \gamma} \right]$	1957
Colding	$\phi = a \tan \left[\frac{2 \left(\frac{f}{h} + 2 \right)}{\left(\frac{f}{h} + 1 \right)} \cot(2\Omega) - (\rho - \gamma) \right]$	1958
Oxley	$\phi = a \tan \left[1 + \frac{\pi}{2} - 2\phi + \frac{\cos 2(\phi - \gamma)}{\tan \rho} \sin 2(\phi - \gamma) \right] - (\rho - \gamma)$	1961
Sata Yoshikawa	$\phi = a \cot \left[\cot \theta + \frac{\cos \theta}{\sin(\theta + \gamma)} kL \right]$	1963
Das Tobias	$D = \frac{\cos(\rho - \gamma)}{\cos(\rho - \gamma + \phi)}$	1964

The shear zone models are an obvious improvement over the preceding models. Many additions to the first model proposed by Oxley have been reported. A full account of these developments would be out of the scope of this work; a detailed description of Oxley’s works is given in [17].

2.3.5 Discussion on Analytical Modeling of Machining

The analysis presented here is not at all a complete one; with more than 50 shear angle solutions identified in the relevant literature as it is reported in [3] this would be impossible within this book. However, an outline of the most important models and the development over the years is presented. Furthermore, in Table 2.1 some shear angle formulas are gathered. In the following lines some drawbacks in the analytical modeling procedure are discussed.

The single shear plane model has been criticized over the years and experimental data do not correlate with the theory results. Astakhov [25] summarized the major inherent drawbacks of the single shear plane model as being the infinite strain rate, the unrealistic high shear strain that is in contradiction with material testing results, the rigid perfectly plastic workpiece material assumption, the improper accounting for the resistance of the processed workpiece material, the perfectly sharp cutting edge of the tool and the fact that there is no contact on the tool flank surface that are not realistic for common practice and the inapplicability of the model in brittle material machining. Furthermore, for the Ernst and Merchant theory, drawbacks include the incorrect velocity and force diagrams presented and the assumption of

constant friction coefficient. However, this model is still in use by researchers due to its simplicity.

Slip-line solutions like the ones presented in Sect. 2.3.3 also have poor correlation with experimental results and no strain hardening is considered. Furthermore, the non-uniqueness of the models raises criticism on the results. Finally, Zorev's general model is based on geometrical considerations and no principle of mechanics of materials or physical laws are used. It is argued that all solutions related to this model, including Ernst and Merchant and Lee and Shaffer theory have little to do with physics and the mechanics of metal cutting [25].

The analyses already presented pertained only to orthogonal cutting with continuous chip. However, the shear plane model has been extended to three dimensions [26] and the slip-line model has been proposed for oblique cutting [27]. A three-dimensional analysis similar to the work of Oxley has been presented by Usui [28–30], which includes secondary cutting edge and nose radius effects; the results apply to turning, milling and groove cutting. However, both Oxley's and Usui's models are quite complex and for their application stress and strain data at the strain rates and temperatures encountered in metal machining are needed. The lack of these data is a significant drawback. These are the reasons that these models, although more complete than all the others since they include temperature effects and can be used in tool wear and segmented chip formation modeling and are in agreement with experimental data, are not widely used outside the research groups that they developed them. Nevertheless, Usui's tool wear estimation algorithm is integrated into finite element models for the prediction of tool wear; the commercial FEM software Third Wave AdvantEdge has the option of using this algorithm in the analyses it can perform.

Finally, another form of modeling for cutting force models will be briefly discussed here, namely Mechanistic modeling; a review can be found in [31]. This kind of modeling is not purely analytical because it is based on metal cutting mechanics but also depends on empirical cutting data; it is a combination of analytical and experimental modeling techniques. Such an approach avoids the complications of incorporating parameters such as shear angle and friction angle, by using experimental force data and it is suitable for use in oblique cutting and various cutting processes.

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