UNITED STATES PATENT AND TRADEMARK OFFICE

BEFORE THE PATENT TRIAL AND APPEAL BOARD

UBER TECHNOLOGIES, INC.,
Petitioner

v.

SURGETECH LLC,
Patent Owner

Patent 11,334,598

DECLARATION OF KYLE NOREIGA

I, Kyle Noreiga, declare as follows:

1. I am a Research Specialist at Cogency Global Inc. ("Cogency").

2. At the direction of Groombridge, Wu, Baughman & Stone LLP ("Groombridge") and as part of my employment with Cogency, I searched the online catalogue of the Library of Congress for the book titled "Pricing and Revenue Optimization" by Robert Phillips on March 21, 2023, which, at Groombridge's direction, I scanned a portion of, and provided to Groombridge. That scanned portion is attached as Exhibit A.

3. Attached as Exhibit B is a copy of the catalogue record of the Library of Congress, retrieved as a result of the online search I conducted on March 21, 2023, for the book "Pricing and Revenue Optimization."

4. I understand that willfully making false statements may result in legal consequences such as fines or imprisonment. I make this declaration of my own personal knowledge, and all statements are true. If sworn as a witness in this matter, I could and would competently testify to the matters stated herein.

Sworn to this 27th day of March, 2023 in Washington, D.C.

Kyle Noreiga

Kyle N---iga

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Sworn to this 28th day of March, 2023 in Washington, D.C.

Kyle Noreiga

Kyle Noreiga

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