

Channel Estimation on MIMO-OFDM Systems

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Abstract—Modern mobile telecommunication systems are using MIMO combined with OFDM, which is known as MIMO-OFDM systems, to provide robustness and higher spectrum efficiency. The major challenge in this scenario is to obtain an accurate channel estimation to detect information symbols, once the receiver must have the channel state information to equalize and process the received signal. The main goal of this paper is to present some techniques and analysis for channel estimation in MIMO-OFDM systems, considering the influence of various system parameters on the channel estimation error and on the final system performance.

Index Terms—MIMO-OFDM, OFDM, channel estimation, diversity.

I. INTRODUCTION

Nowadays, telecommunication services demand high data rates with reliability. However, to achieve high data rates, it is necessary to use a wide spectral bandwidth, which makes the system economically unfeasible. Another problem is that, in this scenario, the channel becomes very selective [1], impairing the reliability of the received information. In order to minimize these problems, digital signal processing techniques combined with designing transceivers strategies are used, where Multiple Inputs and Multiple Outputs (MIMO) deserves mention. MIMO systems use multiple antennas to transmit and multiple antennas to receive signals [2][3]. The multiple signals transmitted and the multiples replicas obtained in the receiver can be combined to increase the robustness (diversity) or the data rate (multiplexing).

Orthogonal Frequency Division Multiplexing technique (OFDM) [4] are commonly used to overcome the ISI (Inter Symbol Interference) introduced by multipath channel. This technique is employed in several digital communications standards, such as DVB-T, DVB-T2, ISDB-T, WiFi, Wi-Max, LTE, IEEE 802.11 and others.

Therefore, future telecommunication systems tend to combine both techniques mentioned above, known as MIMO-OFDM systems [2][3]. Depending on the designed scheme, a system operating with MIMO-OFDM can provide robustness against frequency-selective and time-variant channels, and/or to obtain multiplexing gain. The major challenge in this scenario is to obtain accurate channel estimation for detection of the information symbols, since the receiver requires the Channel State Information (CSI) to equalize the received symbols, due to the phase rotation and amplitude attenuation caused by the channel [5].

The main goal of this paper is to present some analysis for channel estimation in MIMO-OFDM scheme. A comparison is made between the presented estimation techniques, showing the advantages and disadvantages of each one. The influence of various system parameters on the channel estimation error and in the final performance of the system will also be evaluated. All tests will be conducted using the MATLAB. Root-mean-square-error method is used to measure the deviation between the actual and estimated channel. Another parameter that will be used to analyze the systems performance is the MER (Modulation Error Rate), which measures the dispersion of the constellation of the estimated symbols.

This paper is organized as follows: Sections II and III provide basics concepts of MIMO and OFDM techniques, respectively. Section IV presents some methods to perform the channel estimation in MIMO-OFDM systems. Then, in Section V, the results of the simulations are presented. Finally, in Section VI the final conclusions of the paper are presented.

II. MIMO SYSTEMS

MIMO systems [6] use multiple antennas in the transmitter and receiver sides. The signals sent by the transmitter antennas are received by the receiver antennas and then combined, in order to achieve a reduction of the bit error rate (BER) or a capacity gain. Figure 1 shows a basic MIMO system.

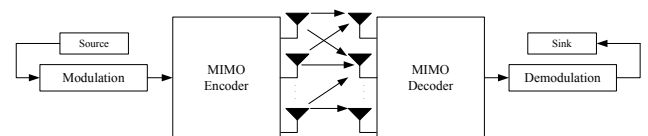


Fig. 1. Basic MIMO system.

Taking advantage of what the MIMO technique can provide, three features stand out: (a) diversity gain, (b) multiplexing gain and (c) both gains. These features are explored in the following subsections.

A. Diversity gain in MIMO systems

MIMO technique for diversity gain [7] takes advantage of the signals arriving at the receiver by secondary channels and signals arriving from multipath propagation. These signals can be combined constructively at the receiver, i.e., in a favorable way to estimate the information transmitted. It is possible to

take advantage of temporal diversity, frequency diversity or space diversity. Figure 2 shows a example of MIMO system for diversity gain, where h_{ij} represents the channel gain between the i -th transmitter antenna and the j -th receiver antenna.

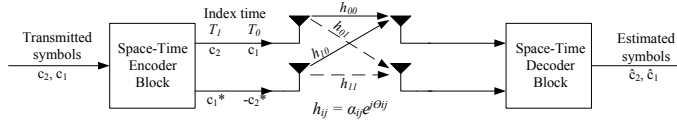


Fig. 2. MIMO system for diversity gain.

B. Multiplexing Gain in MIMO Systems

MIMO systems can be also used to provide multiplexing gain [8], which increases the system capacity, because more than one symbol may be sent at the same time. In order to implement the multiplexing technique, multiple antennas are used to transmit multiple independent information simultaneously on the same frequency at the same time. Since the channel between each transmission and reception antenna will be unique, each transmitted symbol can be recovered through digital signal processing. Zero-Forcing technique is commonly used to recover the data symbols from the received signals. Figure 3 illustrate a MIMO system for multiplexing gain.

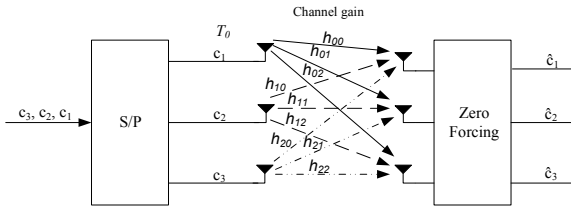


Fig. 3. MIMO system for multiplexing gain.

C. Hybrid MIMO

The two features mentioned in the previous subsections can be used together. This type of system is called hybrid MIMO system [9]. In this scheme a committed relationship should be taken into account, where a higher multiplexing gain implies in less diversity gain and vice-versa. Figure 4 illustrate a possible use of this hybrid technique.

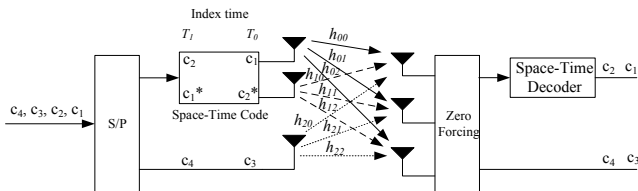


Fig. 4. Hybrid MIMO.

III. OFDM SYSTEMS

The OFDM system [5] is based on the transmission of complex symbols using N orthogonal subcarriers. Thus, it is

possible to transform a high data-rate stream into N low data-rate substreams. In this system, if the number of subcarriers is large enough, the channel frequency response for a single subcarrier may be considered to be flat. Since the subcarriers can be individually demodulated, OFDM provides a higher robustness to the transmitted data. Figure 5 shows the block diagram of the OFDM scheme.

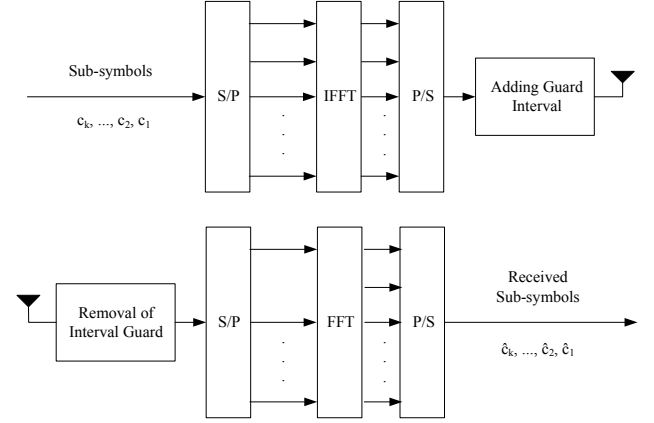


Fig. 5. OFDM system.

In OFDM systems, the transmitted symbols are separated by a guard interval that optimize the performance of communication link. The addition of this extra interval is performed by copying the end of the OFDM symbol at its beginning. The purpose of the guard interval is to introduce immunity to propagation delays, ISI, echoes and reflections, to which digital data is normally very sensitive [10].

IV. CHANNEL ESTIMATION FOR MIMO-OFDM SYSTEMS

The combination of MIMO and OFDM has become very attractive for broadband communication systems, because of the individual characteristics of each technique. Figure 6 shows a simplified MIMO-OFDM system [11][12].

Due to the multipath channel, each OFDM subcarrier is affected by attenuation and a phase rotation. To receive the symbols correctly, the receiver must be able to estimate the channel frequency response. In wireless systems, three methods are commonly used to estimate the channel [13][14], and they are explained next.

A. Channel Estimation using pilot symbols

In this type of estimation, all subcarriers of an specific OFDM symbol carry reference data that are known a priori by the receiver. This estimation method provides a perfect channel estimation during the pilot symbol [15], if the noise is disregarded. However, since a new pilot symbol must be sent within the channel coherence time, this solution can only be used in slow fading channels. In this case, several data symbol can be transmitted between two pilot symbols, reducing the impact of the pilot symbols in the system throughput. The throughput of a OFDM system using pilot symbols is given

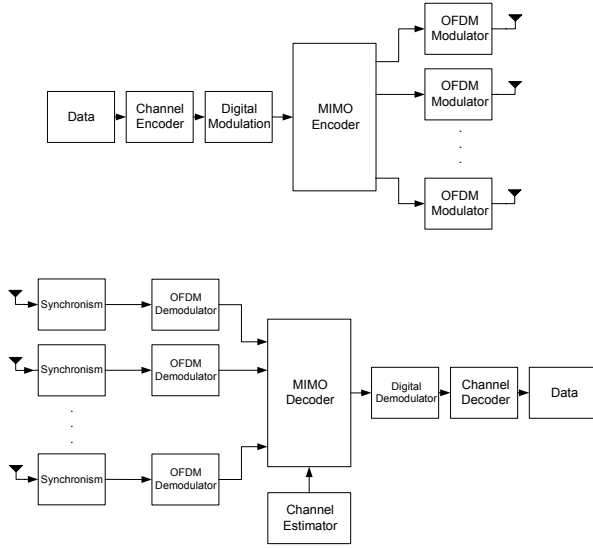


Fig. 6. MIMO-OFDM system.

by

$$R_b = \frac{K_D}{K_D + 1} \times \frac{N \log_2(M)}{T_{OFDM}}, \quad (1)$$

where K_D is the number of OFDM data symbols transmitted between two data symbols, N is the number of subcarriers of an OFDM symbol, M is the modulation used and T_{OFDM} is the time duration of one OFDM symbol. This type of estimation is ideal for highly frequency selective channels with a large coherence time.

B. Channel estimation using pilot subcarriers

In this case, the estimation is performed by sending spaced pilots in all transmitted OFDM symbols [15][16]. The smaller the frequency distance between the pilots, the better is the channel estimation. However, a larger the number of pilots subcarriers, will lead to a prohibitive reduction in the data rate. The throughput, in this case, can be calculated by

$$R_b = (N - N_P) \times \frac{\log_2(M)}{T_{OFDM}}, \quad (2)$$

where N_P represents the number of pilot subcarriers. This type of channel estimation is ideal for faster and less frequency selective channels. Most of the analysis performed in Section V use this method of estimation, because it is widely used by the digital communication standards.

C. Hybrid channel estimation

The hybrid estimation is a combination of the two techniques mentioned previously, where symbols containing only carrier pilots (pilot symbols), and symbols containing data carriers interspersed with pilots are used. Thus, an accurate estimation of the channel is held every K_D OFDM symbols. In the remaining time, the estimation is not as precise as the first one, but enough to maintain a good channel estimation.

In this case, the throughput is given by

$$R_b = \frac{K_D}{K_D + 1} \times \frac{(N - N_P) \log_2(M)}{T_{OFDM}}. \quad (3)$$

D. Channels estimation for MIMO-OFDM

The MIMO-OFDM system that will be used in the paper is presented in Figure 7. This scheme is known as STC-OFDM [7][14] (Space Time Code OFDM) and offers a 4-order diversity gain. In this model, if the noise effect is disregarded,

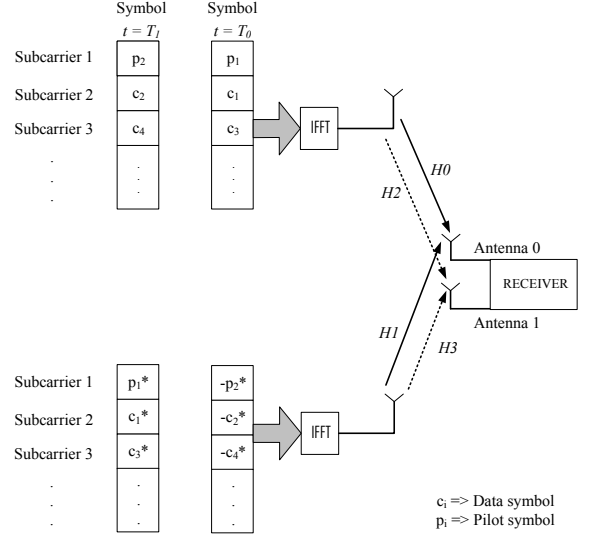


Fig. 7. MIMO-OFDM system analyzed.

the received signals in pilot subcarriers at the receiving antenna 0 are given by

$$P'[n] = p[n]H_0 - p^*[n+1]H_1, \quad (4)$$

$$P'[n+1] = p[n+1]H_0 + p^*[n]H_1, \quad (5)$$

where $p[n]$ is a pilot subcarrier transmitted at time instant nT_0 , $(\cdot)^*$ is the conjugate operation and H_i represents the frequency gain for the i -th channel. Thus, assuming that the value $p[n] = p[n+1] = p$ and $p \in \mathbb{R}$ and solving (4) and (5), the channels estimation can be obtained by to

$$H'_0 = \frac{P'[n+1] + P'[n]}{2p}, \quad (6)$$

$$H'_1 = \frac{P'[n+1] - P'[n]}{2p}. \quad (7)$$

The same analysis can be done to estimate the channels H_2 and H_3 , related with the receiving antenna 1. Once obtained the channel estimations at the frequency of the pilot subcarriers, it is then necessary to use some interpolation technique to obtain an estimative of the channel frequency response at the frequency of all data subcarriers. It is important to note that to estimate the channel completely, in the scenario presented in Figure 7, it takes $2 T_{OFDM}$. It means that the channel cannot vary during this time interval. In other words, the coherence time of the channel must be greater than $2 T_{OFDM}$.

The root-mean-square error is used to measure the deviation between the actual and estimated channel. It can be evaluated by

$$E_{CE} = \frac{\sqrt{\sum_{i=0}^{N-1} [H[i] - H'[i]]^2}}{N}, \quad (8)$$

where $H'[i]$ is the estimated channel at subcarrier i and N is the number of subcarriers in one OFDM symbol.

Another important parameter that will be used to analyze the performance of systems is the MER (Modulation Error Rate), which measures the dispersion of the constellation of the estimated symbols. Its value is given by

$$MER = \frac{\sum_{n=0}^{N-1} [I_n^2 + Q_n^2]}{\sum_{n=0}^{N-1} [(I'_n - I_n)^2 + (Q'_n - Q_n)^2]}, \quad (9)$$

where I_n and Q_n represent the in-phase and quadrature components of the n -th transmitted symbol and I'_n and Q'_n represent the in-phase and quadrature components of the estimated symbol. Usually, this measure is expressed in decibels.

V. PERFORMANCE ANALYSIS

The main purpose of this section is to analyze the influence of different system parameters on the channel estimation and, consequently, in the final performance of the system. MATLAB has been used to simulate the system presented in Figure 7. The simulation parameters are shown in Table I.

TABLE I
SYSTEM PARAMETERS.

Parameters	Value
Mapping	16-QAM
Total number of subcarriers	8192
Number of pilot subcarriers	257
OFDM symbol duration(T)	1.024 ms
Distance between the pilot subcarriers	31.25 kHz
Modulation employed in the pilot subcarriers	BPSK
Sampling rate	8 MHz

A. Influence of the interpolation method in the channel estimation and system performance

This subsection presents the simulation results about the influence of interpolation method on the quality of the channel estimation. The root-mean-square error of the channel estimation and the MER of the linear, cubic and DFT interpolation methods are evaluated. All three interpolation methods are detailed in [14]. The delay profile for this analysis is presented in Table II.

TABLE II
DELAY PROFILE OF CHANNEL 1.

Parameter	P_0	P_1	P_2	P_3	P_4	P_5
Delay [μs]	0	0.15	2.22	3.05	5.86	5.93
Gain [dB]	0	-13.8	-16.2	-14.9	-13.6	-16.4

Using the linear interpolation method to estimate the channel, the root-mean-square-error is 3.32×10^{-4} , and the MER is 30.7 [dB]. Figure 8 present the symbol dispersion due to channel estimation error using linear interpolation.

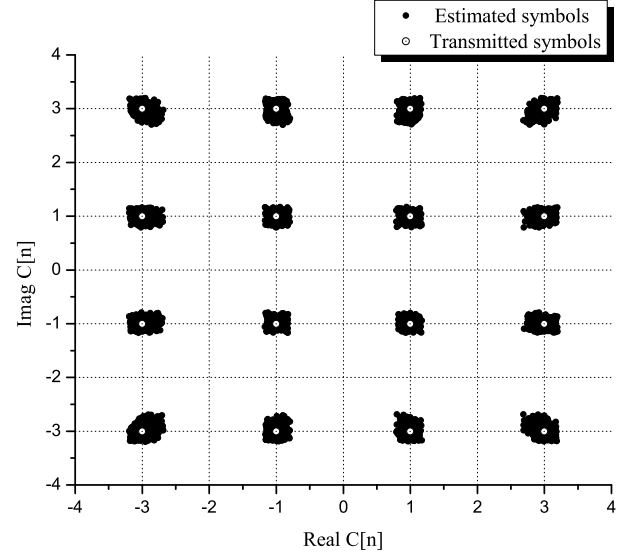


Fig. 8. Symbol dispersion using linear interpolation.

It is important to remember that the deviation suffered by the symbol constellation shown in Figure 8 is only due to channel estimation error.

For the cubic interpolation method, the root-mean-square-error is 5.063×10^{-5} , resulting in an MER of 47.1 [dB]. Figure 9 shows the received symbols constellation using cubic interpolation to estimate the channel.

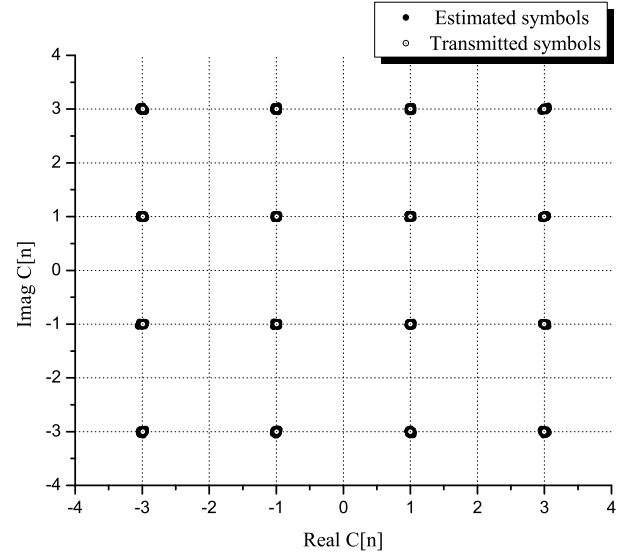


Fig. 9. Symbol dispersion using cubic interpolation.

The third and final interpolation method analyzed is the DFT interpolation. With this method, the estimation error is 2.38×10^{-18} and the MER is 310.7 [dB], which is equivalent

to say that the deviation of the constellation is virtually zero. Figure 10 shows the constellation of the received symbols for the DFT interpolation method.

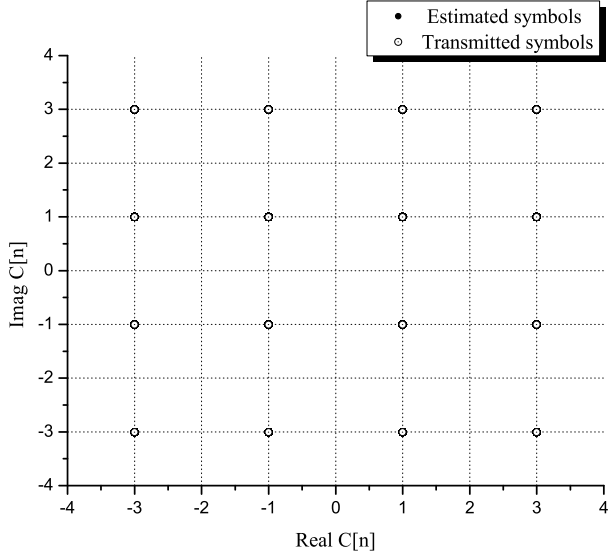


Fig. 10. Symbol dispersion using DFT interpolation.

It is possible to conclude that the interpolation method influences directly in the final system performance, and between three methods shown, the DFT interpolation archived the best result. On the other hand, this interpolation method is the most complex to be implemented [14].

B. Influence of the delay profile in the channel estimation error and system performance.

The system with parameters shown in Table I has been simulated in two channels with different delay profiles, which are presented in Table III and Table IV.

TABLE III
DELAY PROFILE OF CHANNEL 2.

Parameter	P_0	P_1	P_2	P_3	P_4	P_5
Delay [μs]	0	0.15	2.22	3.05	5.86	5.93
Gain [dB]	-0.02	-27	-32	-29	-27	-32

TABLE IV
DELAY PROFILE OF CHANNEL 3.

Parameter	P_0	P_1	P_2	P_3	P_4	P_5
Delay [μs]	0	0.3	3.5	4.4	9.5	12.7
Gain [dB]	0	-12	-4	-7	-15	-22

The Table V presents the coherence bandwidth for all channels analyzed in this paper. As it can be seen, the delay profile in Table IV (channel 3) is more severe than the others, resulting in a more frequency selective channel. The objective of this analysis is to evaluate how the delay profile interferes in the system performance.

TABLE V
COHERENCE BANDWIDTH.

Channel	BW_C - coherence 50%	BW_C - coherence 90%
Channel 1	137.46 kHz	13.74 kHz
Channel 2	617.42 kHz	61.74 kHz
Channel 3	89.84 kHz	8.98 kHz

The three interpolation methods were analyzed on channels 2 e 3. The results obtained for each interpolation technique on each channel are shown in Tables VI and VII.

TABLE VI
RESULTS FOR EACH INTERPOLATION METHOD ON CHANNEL 2.

Interpolation	E_{CE}	MER [dB]
Linear	6.36×10^{-5}	44.76
Cubic	3.80×10^{-5}	49.29
DFT	2.35×10^{-18}	310.97

TABLE VII
RESULTS FOR EACH INTERPOLATION METHOD ON CHANNEL 3.

Interpolation	E_{CE}	MER [dB]
Linear	8.18×10^{-4}	18.13
Cubic	5.89×10^{-4}	20.45
DFT	3.95×10^{-18}	300.29

With this results, one can conclude that the system performance is more degraded on channels with severe delay profiles, which are more frequency selective. Thus, it is necessary to use more pilot subcarriers in order to prevent the system from being affected by the channel estimation, resulting in a higher MER.

C. Influence of the number of pilot subcarriers in the channel estimation and system performance

In this analysis, the number of pilot subcarriers has been reduced to understand how the number of pilot subcarriers interferes in the channel estimation error and in the final system performance. It is important to note that reducing the number of pilot subcarriers means increasing the frequency spacing between them. In the first, the spacing considered between two pilots is 2 subcarriers, which is then increased to 4, 6, 8, 10, 12...200 subcarriers. The E_{CE} and the MER obtained for linear interpolation using the delay profile presented in Table II and the system parameters presented in Table I, except for the number of pilots, are shown in Figure 11 and Figure 12, respectively.

As shown in Figure 11, when the spacing between pilots increases, i.e., the number of pilots to estimate the channel reduces, the estimation error increases. In Figure 12, when the number of pilots subcarrier decreases, the MER value also decreases but in an exponential way. It must be regarded that in a practical system it is necessary to find a trade-off between number of subcarriers and E_{CE} , since the increased number of pilot subcarriers reduces system throughput.

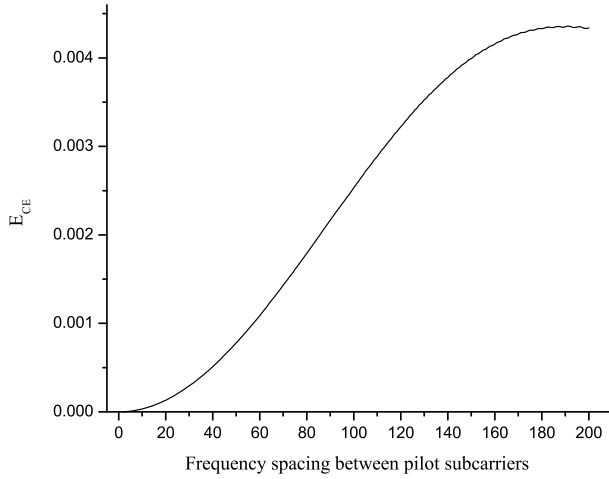


Fig. 11. Channel estimation error as function of the spacing between pilot subcarriers for linear interpolation.

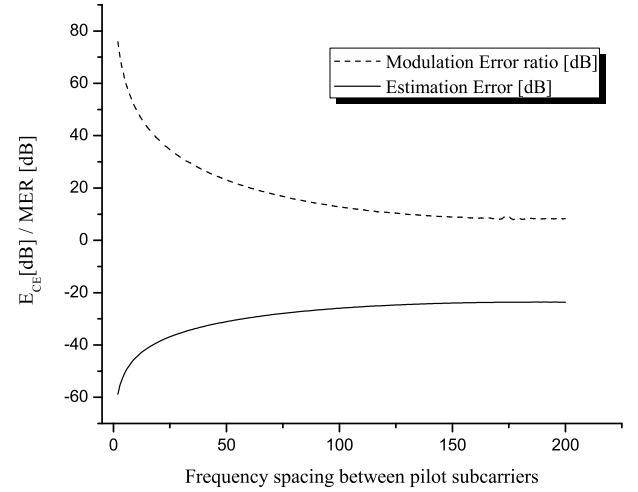


Fig. 13. Channel estimation error and modulation error ratio.

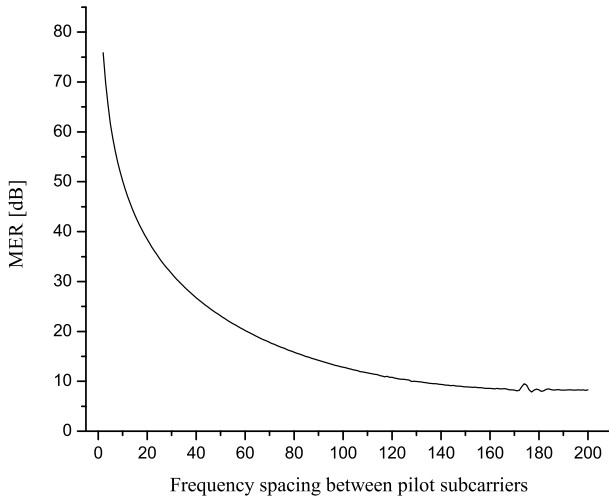


Fig. 12. Modulation error ratio as function of the spacing between pilot subcarriers for linear interpolation.

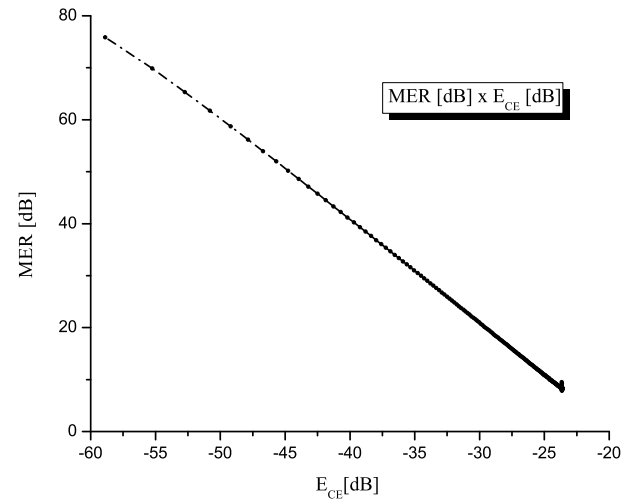


Fig. 14. MER versus E_{CE} both in dB.

One can see that as the channel estimation error increases, the MER of system decreases. However, it is not so easy to establish the exact relationship between these two measures, due to the fact that the MER is expressed in dB and the error is presented in a linear scale.

Figure 13 shows the MER and the channel estimation error, both in logarithmic scale. In this figure, it is more evident how strong the relationship between estimation error and the MER system is. When reducing the distance between the pilot subcarriers the estimation error decreases exponentially, while the MER increases exponentially.

Figure 14 presents the MER versus the estimation error, both in logarithmic scale. Thus, it is possible to conclude that the MER is related almost linearly with the channel estimation error, if both measures are analyzed on a logarithmic scale. Several tests have been performed for the others interpolation methods and others channels with different delay profiles, and the same results have been obtained.

Figure 15 shows the results obtained for all three interpolation methods considered in this paper, where the channel delay profile considered is described in Table II. As can be seen in Figure 15, the linearity between MER and E_{CE} is maintained for all three interpolation techniques.

The same analysis has been performed for the channel delay profile shown in Table III and the result are presented in Figure 16. The linearity has been maintained and the result was practically the same presented in Figure 15.

The final analysis presented has been performed in the most frequency selective channel presented, with delay profile shown in Table IV. The results for this channel is shown in Figure 17, where one can also see the linearity between the MER and E_{CE} . However, when the number of pilot subcarriers is reduced there are a region of non-linearity, which is more pronounced in the linear interpolation technique.

The results presented in this paper can be used to derive a model to estimate the symbol error rate of QAM system considering the channel estimation error.

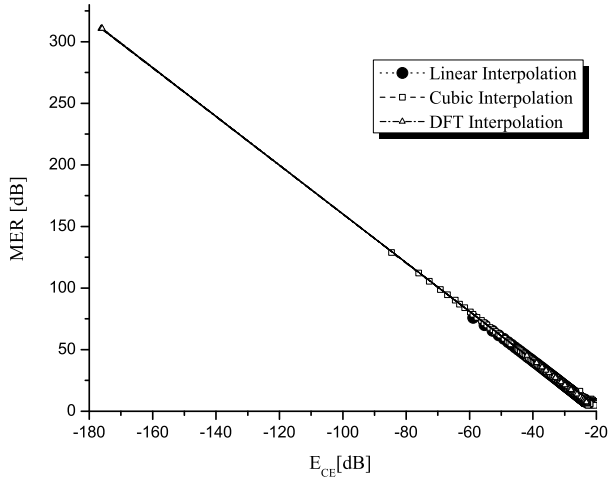


Fig. 15. MER versus E_{CE} both in dB for all interpolation methods analyzed on channel 1.

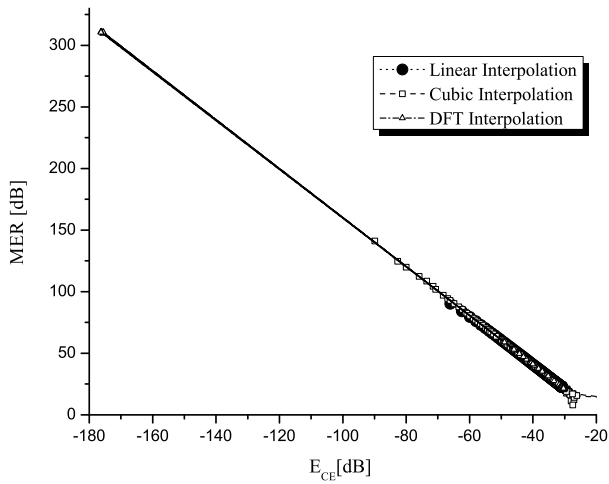


Fig. 16. MER versus E_{CE} both in dB for all interpolation methods analyzed on channel 2.

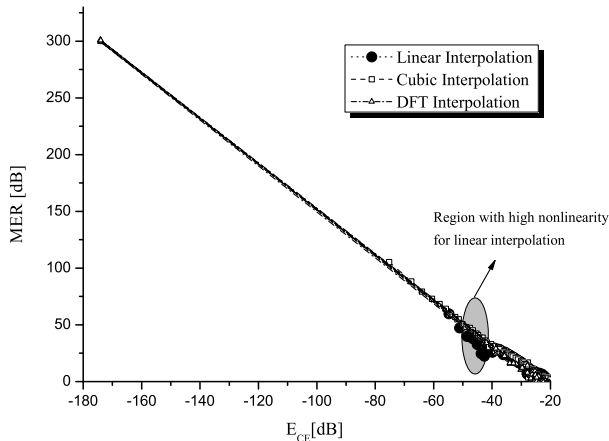


Fig. 17. MER versus E_{CE} both in dB for all interpolation methods analyzed on channel 3.

VI. CONCLUSIONS

One challenge in MIMO-OFDM is to perform an accurate channel estimation. This paper has presented some channel es-

timization techniques that can be used in MIMO-OFDM system that are used for diversity. The influence of the interpolation technique in the channel estimation error and the system MER has been analyzed. It was also shown how the number of pilot subcarriers impacts on the channel estimation error. Different channels with different delay profiles have also been analyzed. A linear relationship between the channel estimation error and the MER has been found, when both measures are analyzed in a logarithmic scale. This results show that it is possible to model E_{CE} as an equivalent noise and use this model to estimate the symbol error probability caused by the channel estimation error.

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