US008036273B2

(12) **United States Patent**
Karczewicz et al.

(10) **Patent No.: US 8,036,273 B2**
(45) **Date of Patent: *Oct. 11, 2011**

(54) **METHOD FOR SUB-PIXEL VALUE INTERPOLATION**

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(73) Assignee: **Nokia Corporation**, Espoo (FI)

(*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35 U.S.C. 154(b) by 0 days.

This patent is subject to a terminal disclaimer.

(21) Appl. No.: **11/839,205**

(22) Filed: **Aug. 15, 2007**

(65) **Prior Publication Data**

US 2008/0069203 A1 Mar. 20, 2008

Related U.S. Application Data

(63) Continuation of application No. 11/090,717, filed on Mar. 25, 2005, now Pat. No. 7,280,599, which is a continuation of application No. 09/954,608, filed on Sep. 17, 2001, now Pat. No. 6,950,469.

(51) **Int. Cl.**
H04B 1/66 (2006.01)

(52) **U.S. Cl.** **375/240.17**; 375/240.16; 375/240.25; 375/240.26; 375/240.12; 382/238; 382/236; 382/233; 382/235

(58) **Field of Classification Search** 375/240.17, 375/240.16, 240.12, 240.25, 240.26; 382/238, 382/236, 233, 235

See application file for complete search history.

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Primary Examiner — Shawn An
(74) *Attorney, Agent, or Firm* — Perman & Green, LLP

(57) **ABSTRACT**

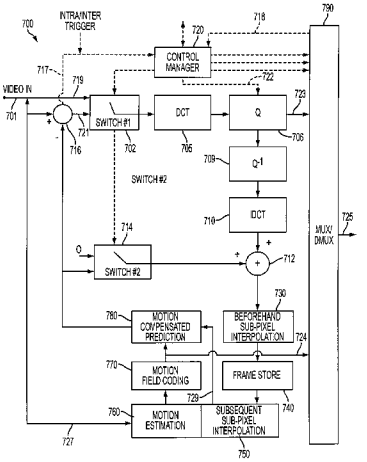
A method of interpolation in video coding in which an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, is interpolated to generate values for sub-pixels at fractional horizontal and vertical locations, the method comprising:

a) when values for sub-pixels at half unit horizontal and unit vertical locations, and unit horizontal and half unit vertical locations are required, interpolating such values directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) when values for sub-pixels at half unit horizontal and half unit vertical locations are required, interpolating such values directly using a weighted sum of values for sub-pixels residing at half unit horizontal and unit vertical locations calculated according to step (a); and

c) when values for sub-pixels at quarter unit horizontal and quarter unit vertical locations are required, interpolating such values by taking the average of at least one pair of a first pair of values of a sub-pixel located at a half unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and half unit vertical location and a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a half unit horizontal and half unit vertical location.

83 Claims, 28 Drawing Sheets



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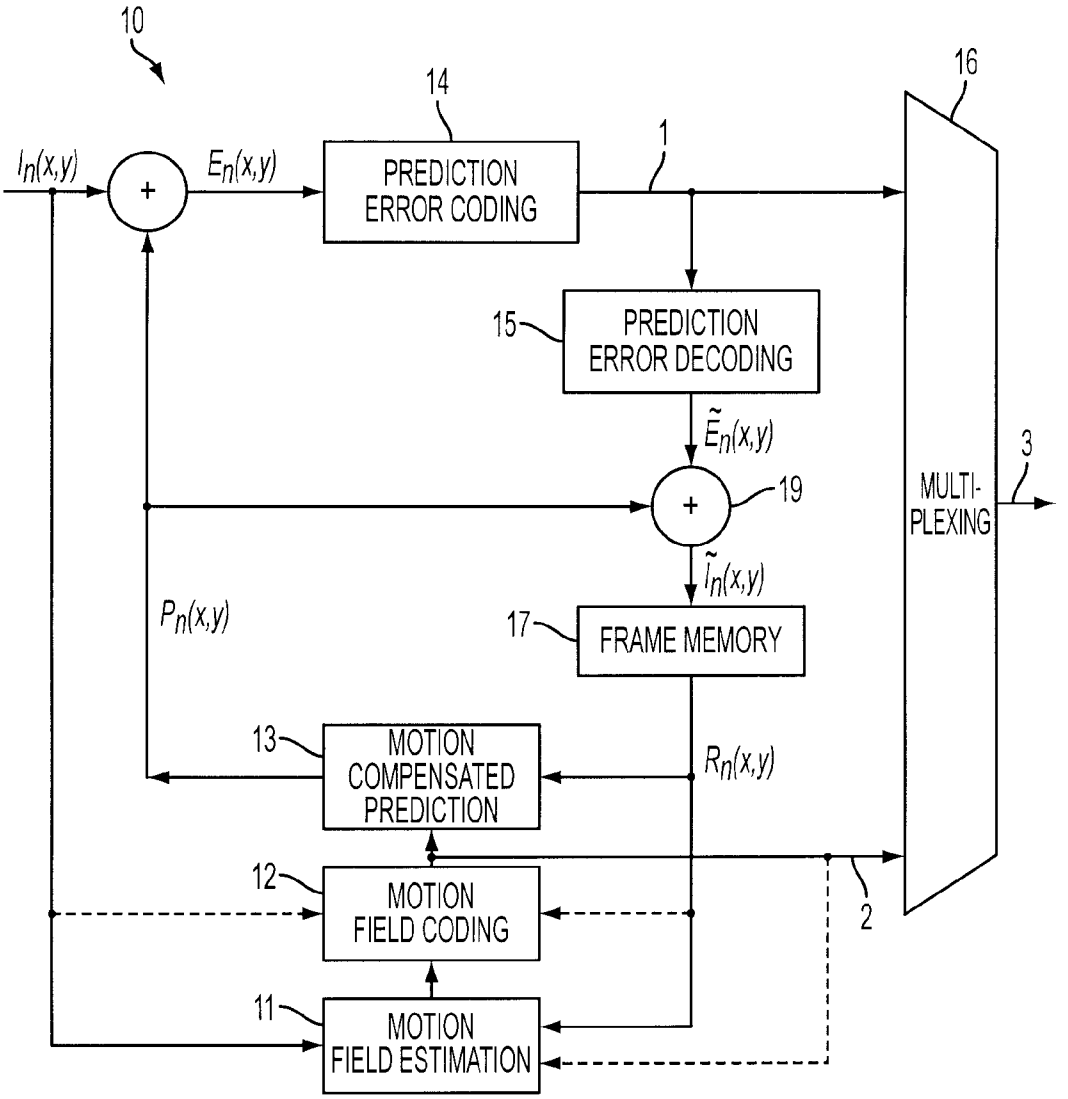


FIG. 1
PRIOR ART

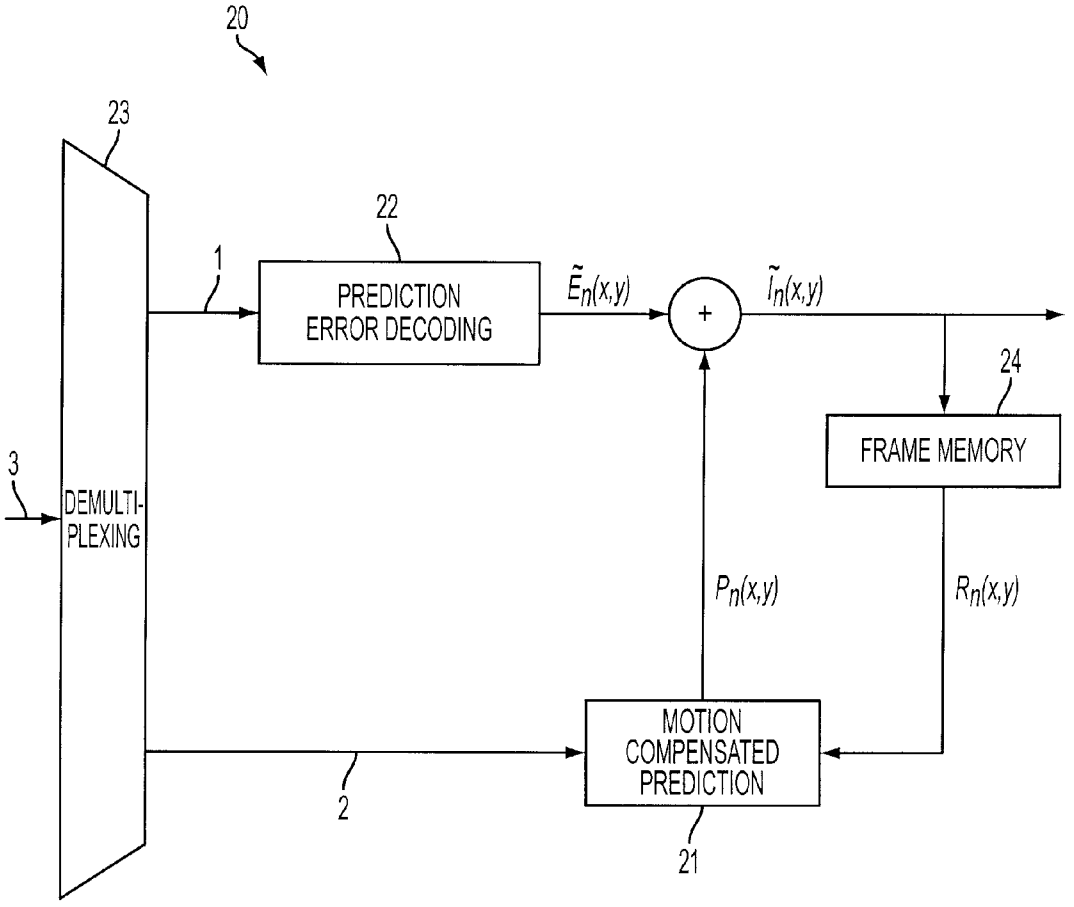


FIG. 2
PRIOR ART

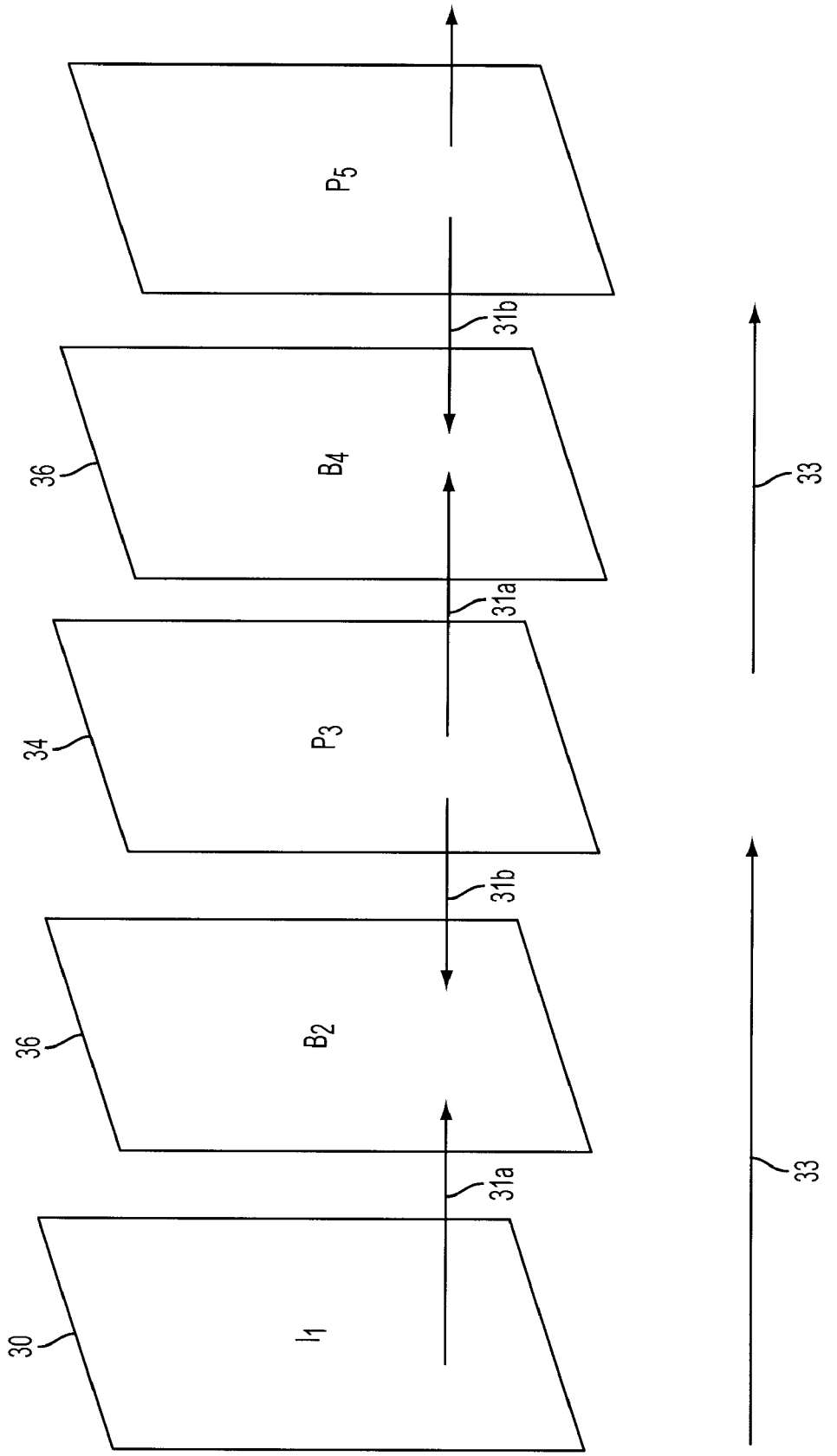


FIG. 3

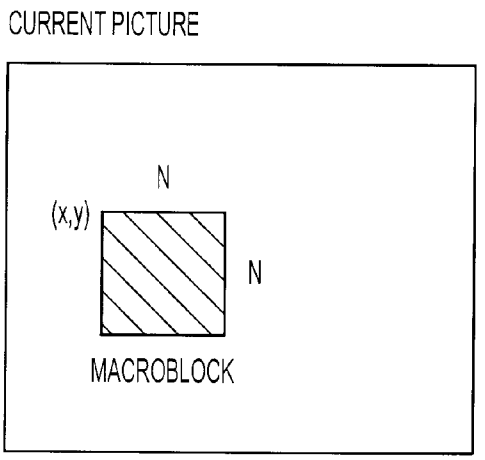


FIG. 4a

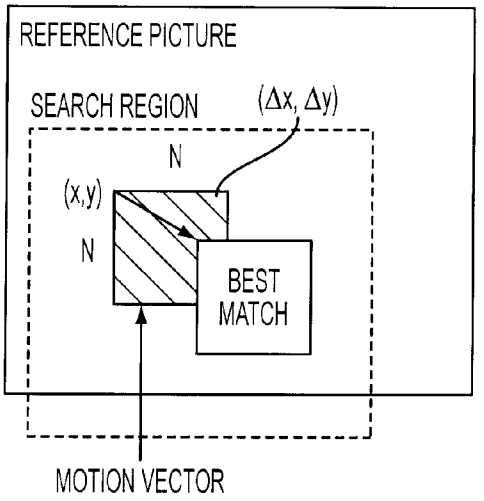


FIG. 4b

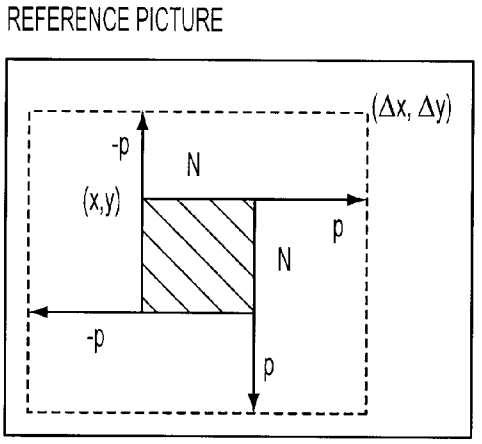


FIG. 4c

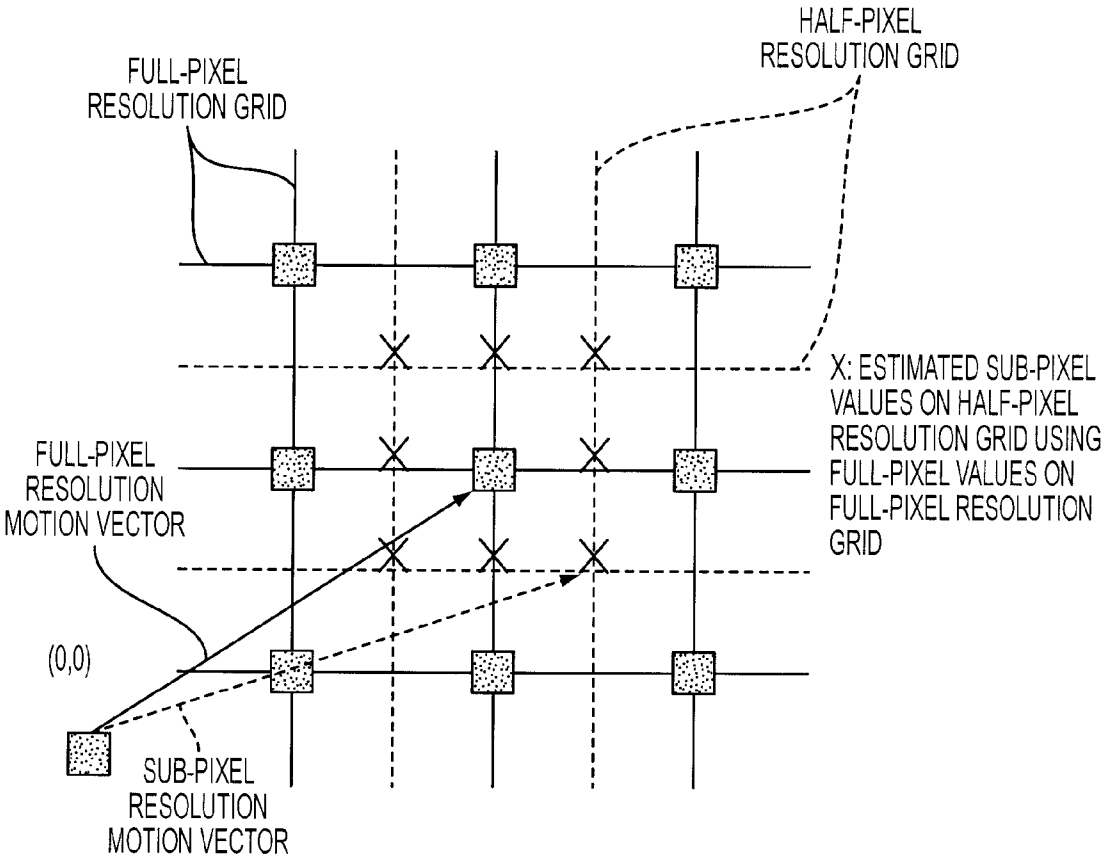

HALF-PIXEL
RESOLUTION GRID
FULL-PIXEL
RESOLUTION GRID
X: ESTIMATED SUB-PIXEL
VALUES ON HALF-PIXEL
RESOLUTION GRID USING
FULL-PIXEL VALUES ON
FULL-PIXEL RESOLUTION
GRID
FULL-PIXEL
RESOLUTION
MOTION VECTOR
(0,0)
SUB-PIXEL
RESOLUTION
MOTION VECTOR

FIG. 5

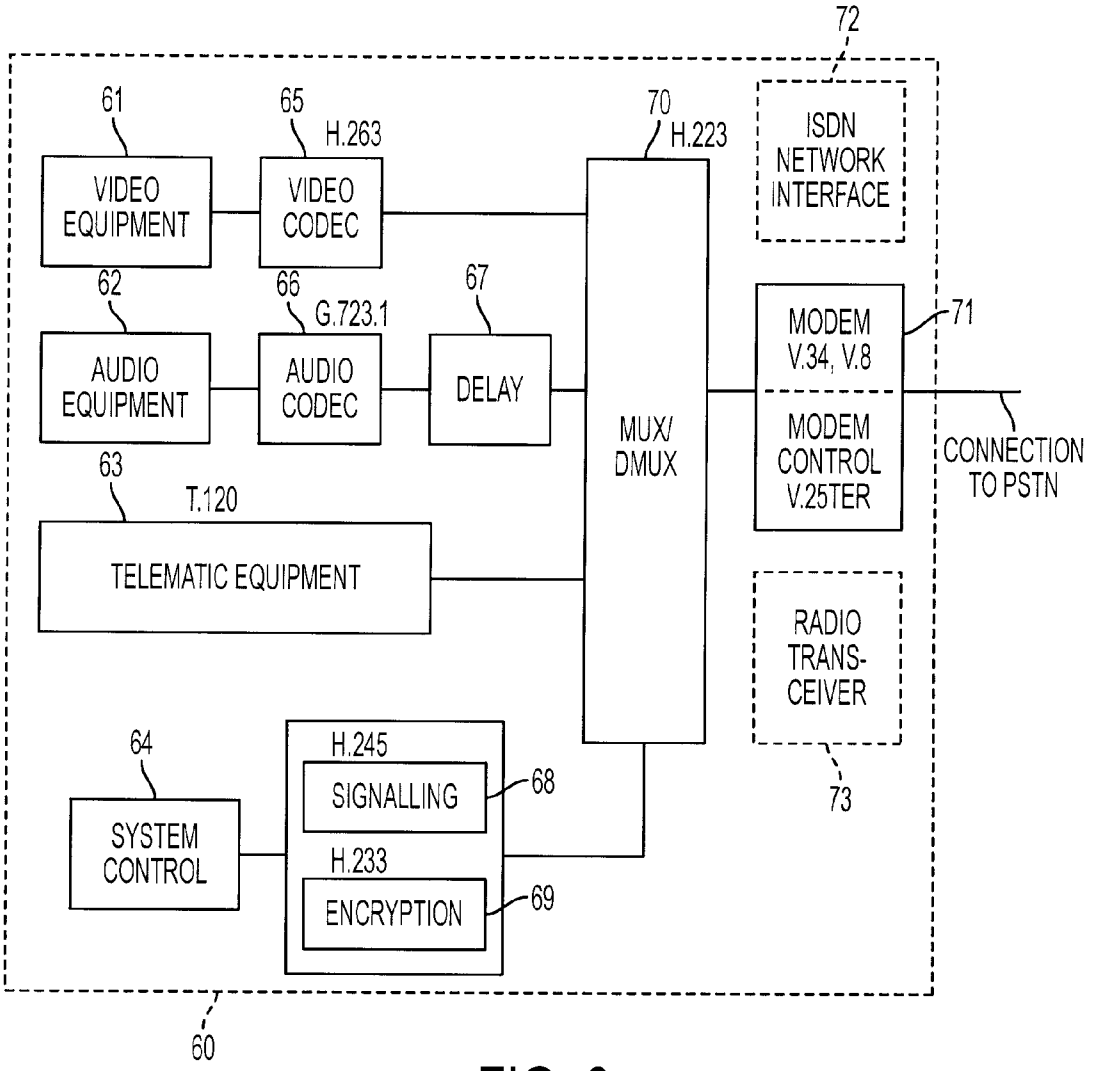

72
61
65
H.263
70
H.223
ISDN NETWORK INTERFACE
VIDEO EQUIPMENT
VIDEO CODEC
62
66
G.723.1
67
MODEM V.34, V.8
71
AUDIO EQUIPMENT
AUDIO CODEC
DELAY
MUX/ DMUX
MODEM CONTROL V.25TER
CONNECTION TO PSTN
63
T.120
TELEMATIC EQUIPMENT
RADIO TRANS-CEIVER
64
H.245
SIGNALLING
68
SYSTEM CONTROL
H.233
ENCRYPTION
69
73
60

FIG. 6

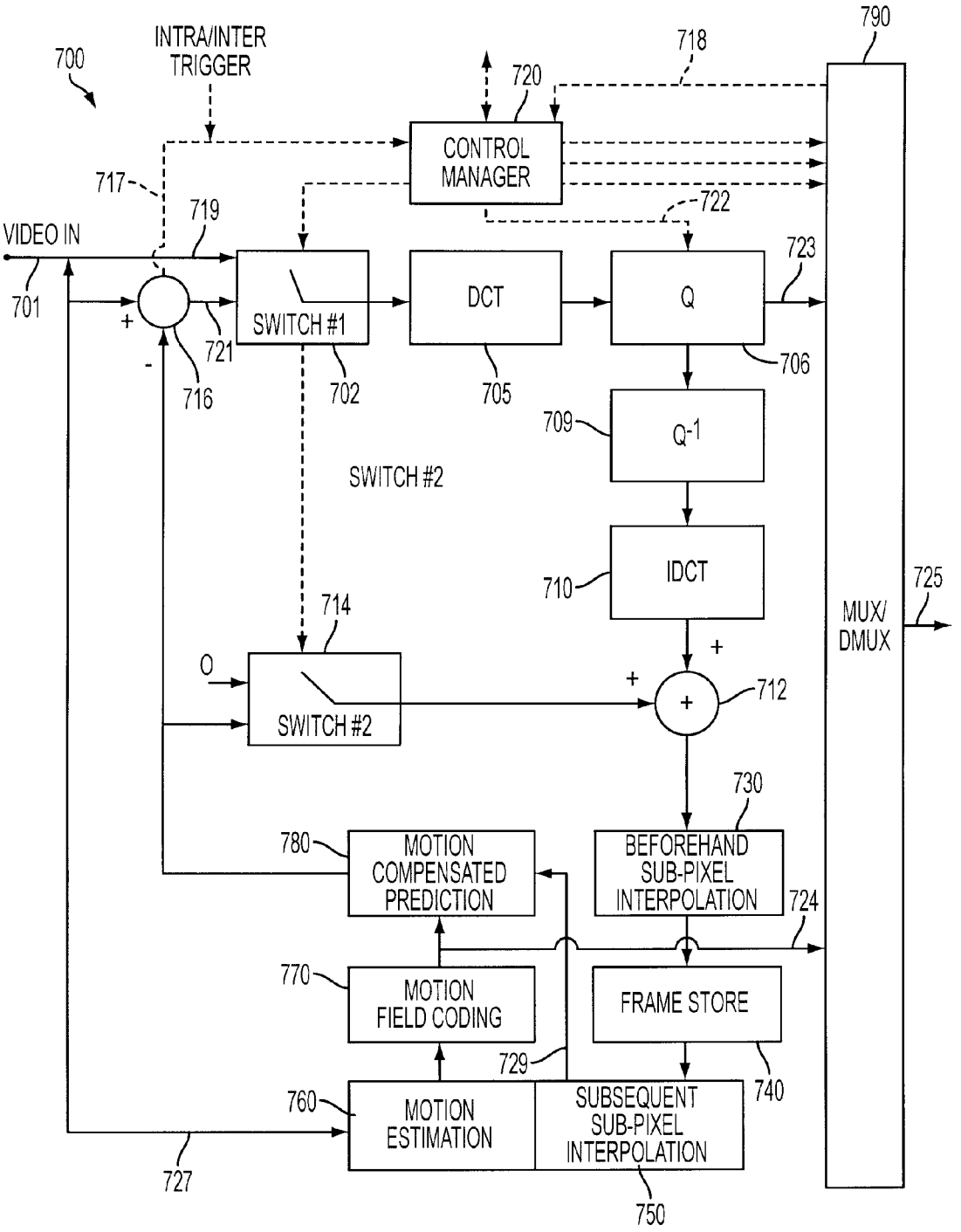

700
INTRA/INTER TRIGGER
790
718
720
CONTROL MANAGER
717
719
722
VIDEO IN
701
723
SWITCH #1
DCT
Q
721
706
716
702
705
709
Q-1
SWITCH #2
710
IDCT
725
MUX/ DMUX
714
0
712
SWITCH #2
730
780
MOTION COMPENSATED PREDICTION
BEFOREHAND SUB-PIXEL INTERPOLATION
724
770
MOTION FIELD CODING
FRAME STORE
729
740
760
MOTION ESTIMATION
SUBSEQUENT SUB-PIXEL INTERPOLATION
727
750

FIG. 7

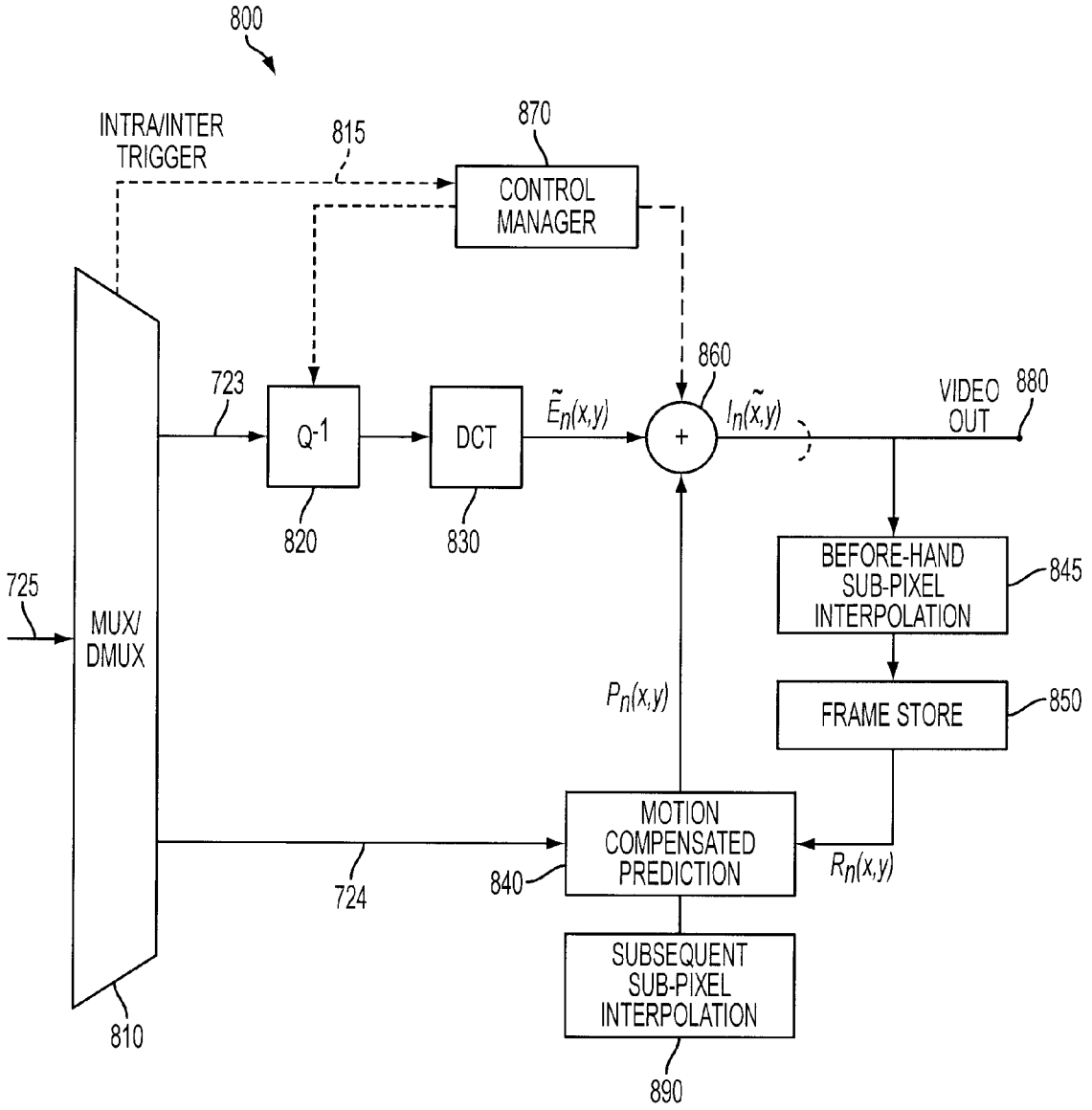

800
INTRA/INTER TRIGGER
815
870
CONTROL MANAGER
723
Q-1
DCT
$\tilde{E}_n(x,y)$
860
+
$I_n(\tilde{x},y)$
VIDEO OUT
880
820
830
BEFORE-HAND SUB-PIXEL INTERPOLATION
845
725
MUX/ DMUX
$P_n(x,y)$
FRAME STORE
850
MOTION COMPENSATED PREDICTION
$R_n(x,y)$
724
840
SUBSEQUENT SUB-PIXEL INTERPOLATION
810
890

FIG. 8

FIGURE INTENTIONALLY OMITTED

FIG. 9

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FIGURE INTENTIONALLY OMITTED

FIG. 10

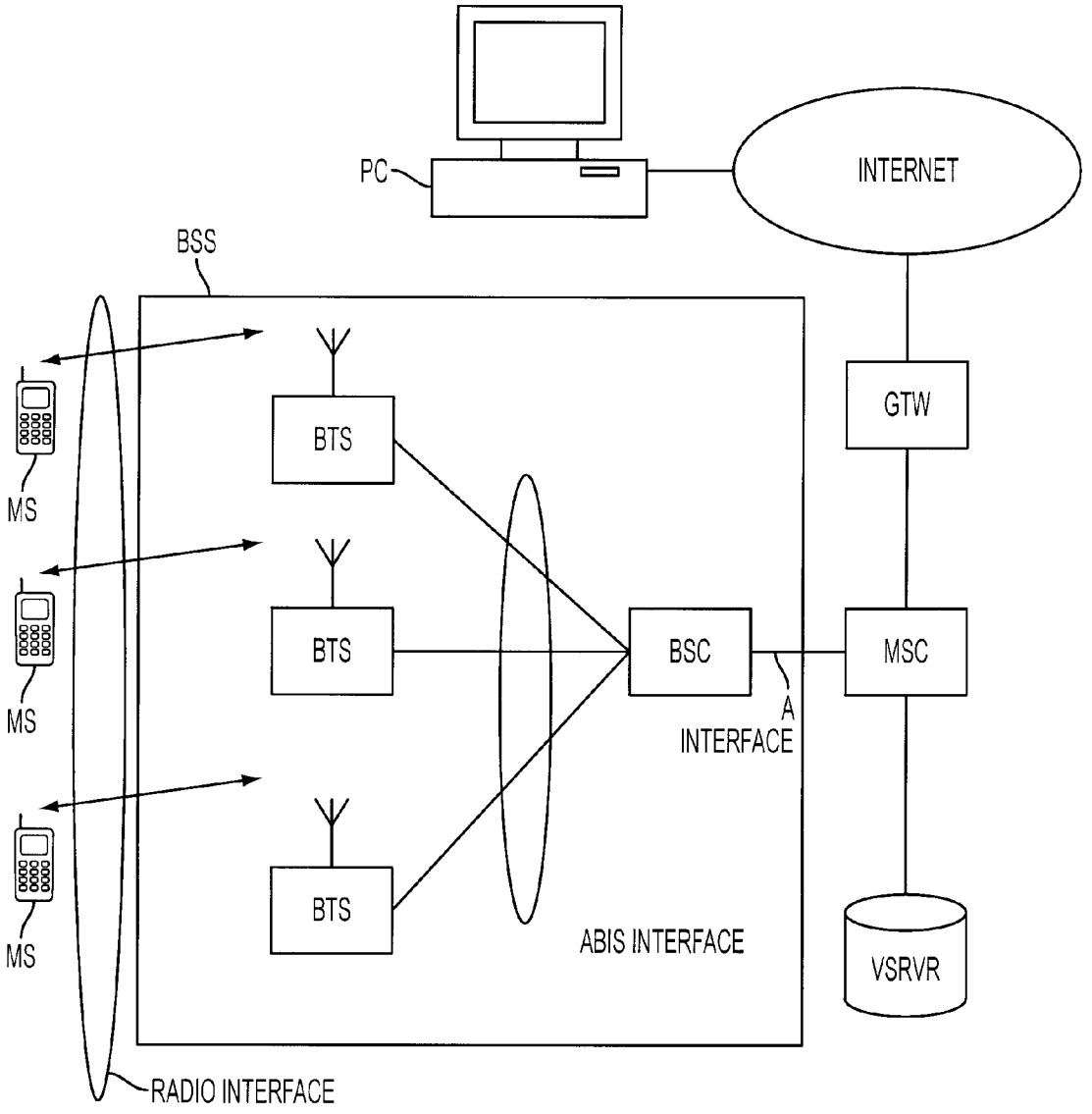

PC
INTERNET
BSS
GTW
BTS
BTS
BTS
MS
MS
MS
BSC
MSC
A
INTERFACE
ABIS INTERFACE
VSRVR
RADIO INTERFACE

FIG. 11

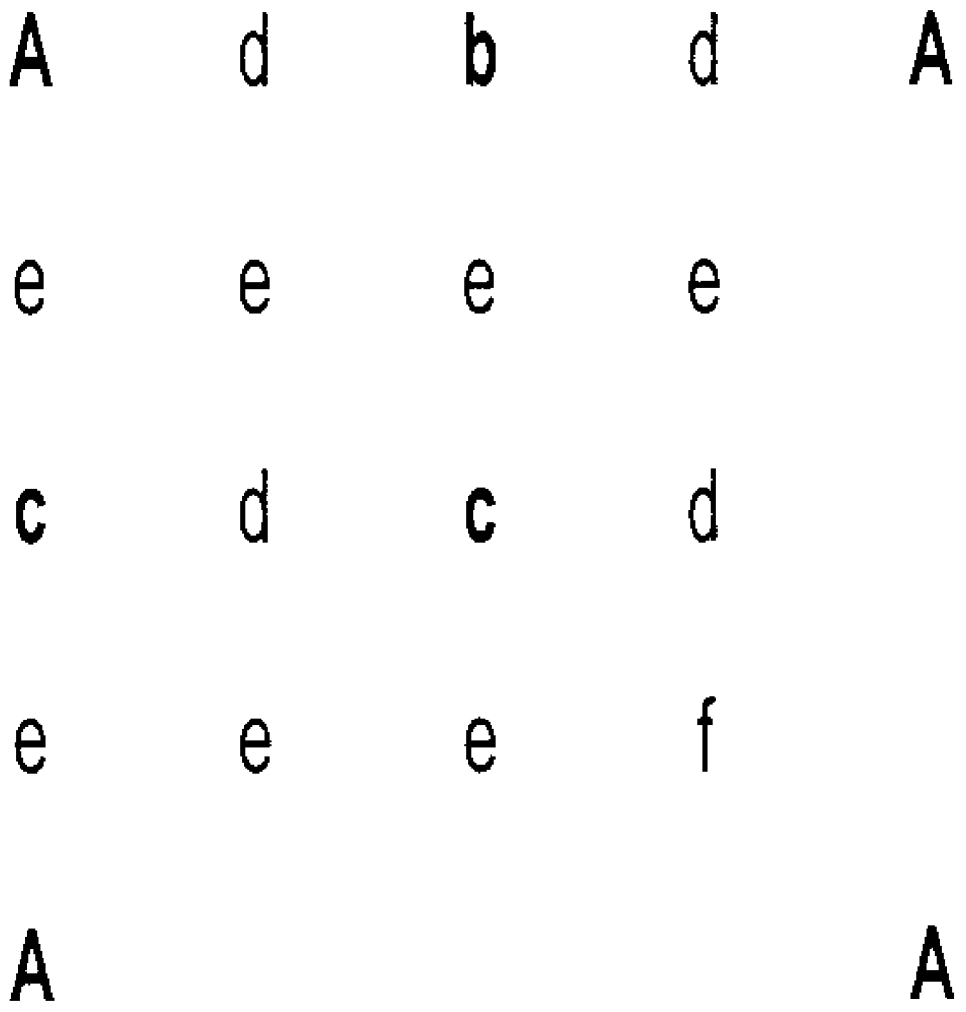


FIG. 12a

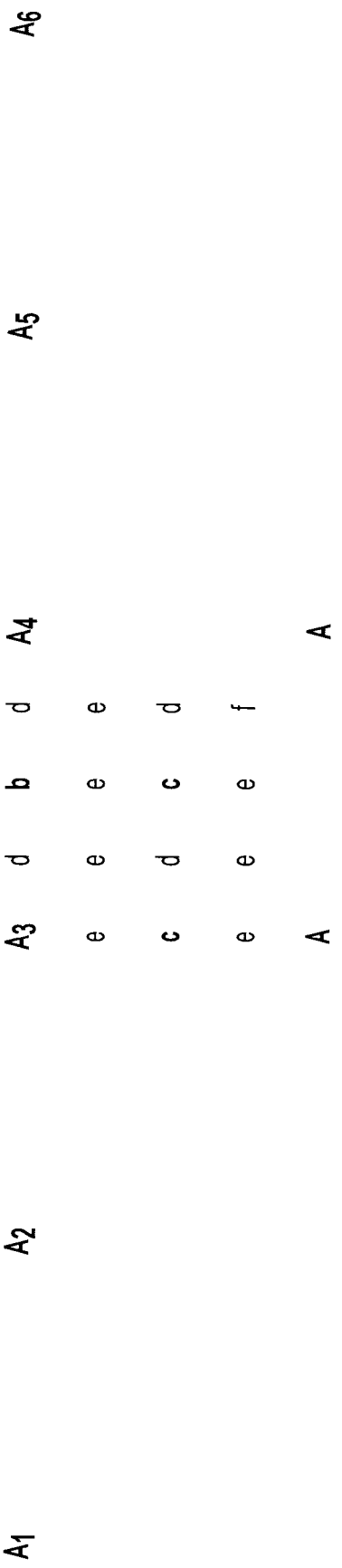


FIG. 12b

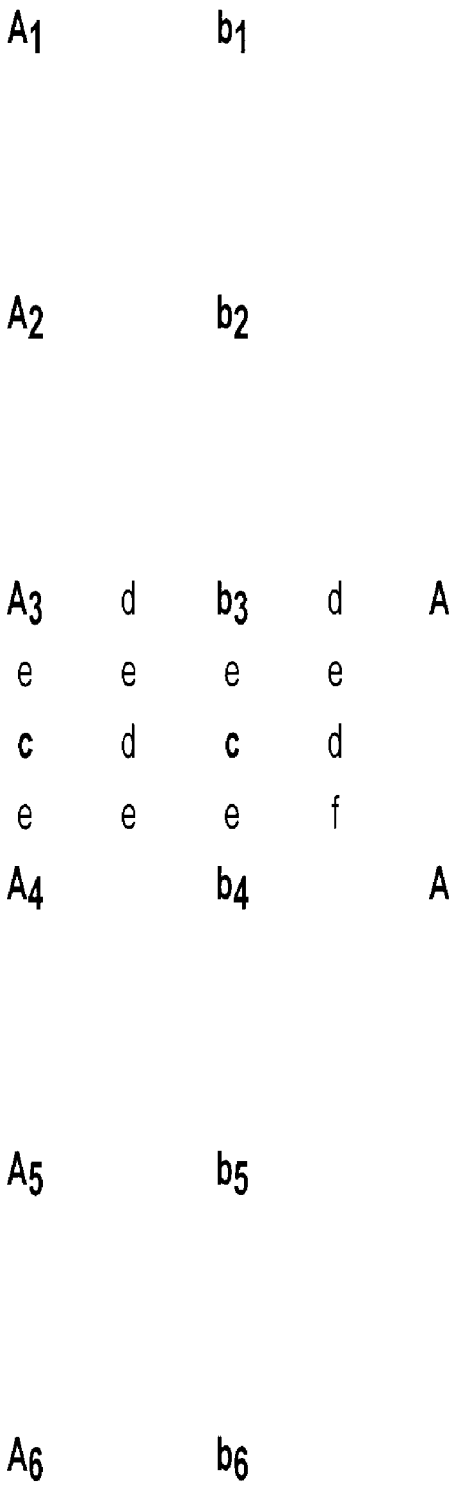


FIG. 12c

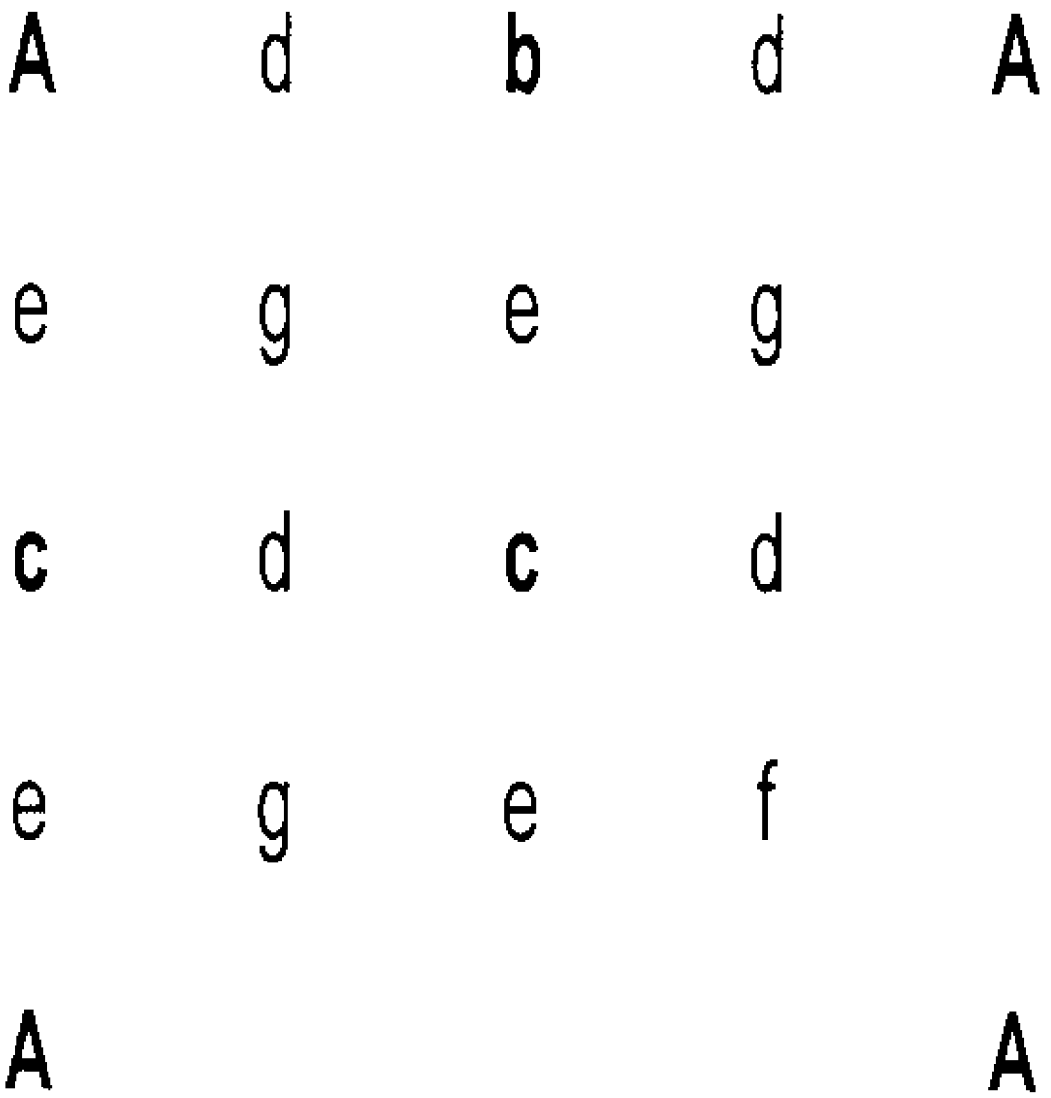


FIG. 13a

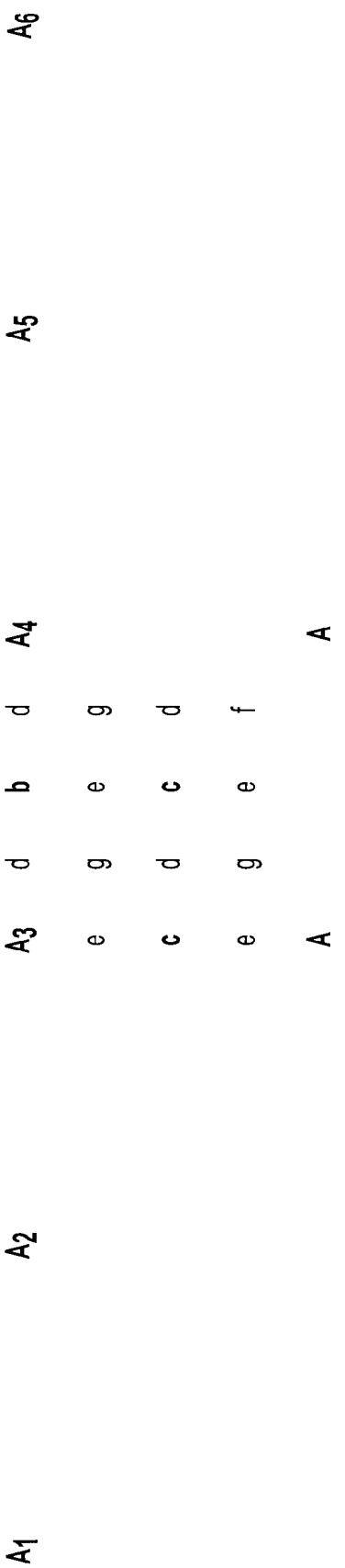


FIG. 13b

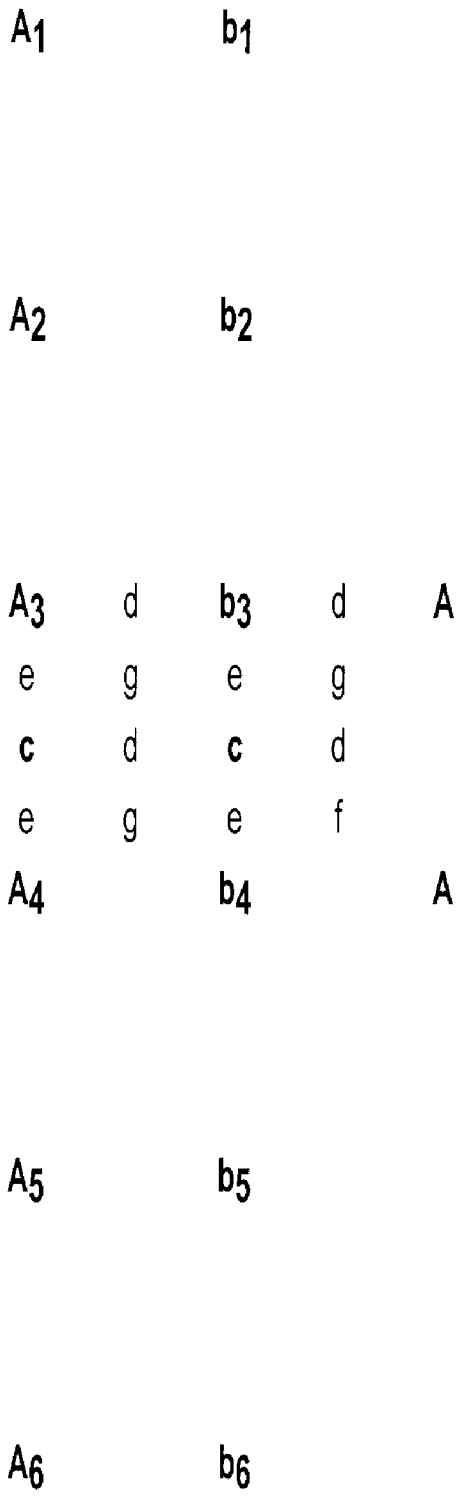


FIG. 13c

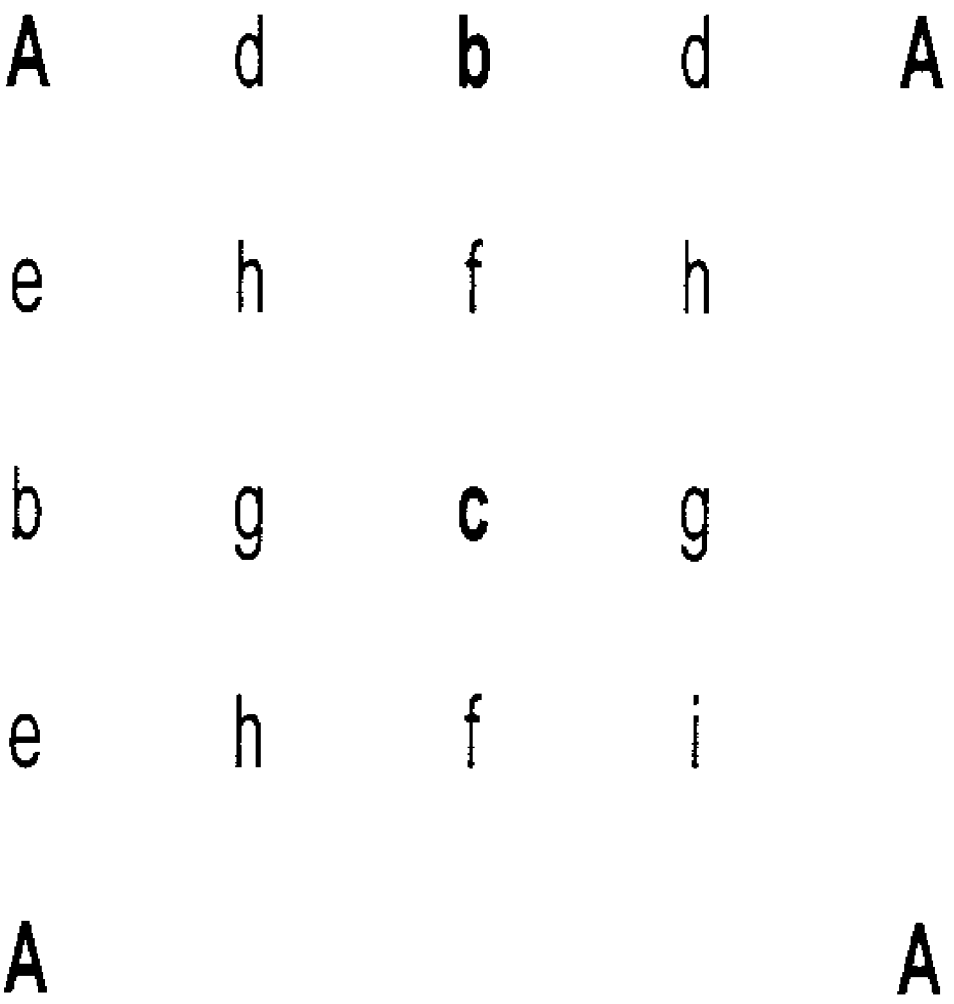


FIG. 14a

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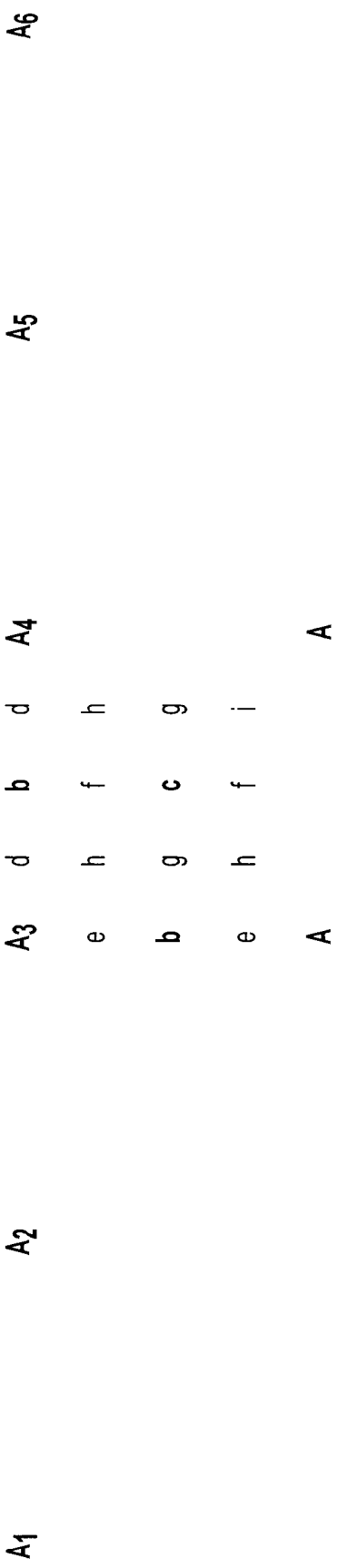


FIG. 14b

A_1

A_2

A_3	d	**b**	d	A
e	h	f	h	
b	g	**c**	g	
e	h	f	i	
A_4				A

A_5

A_6

FIG. 14c

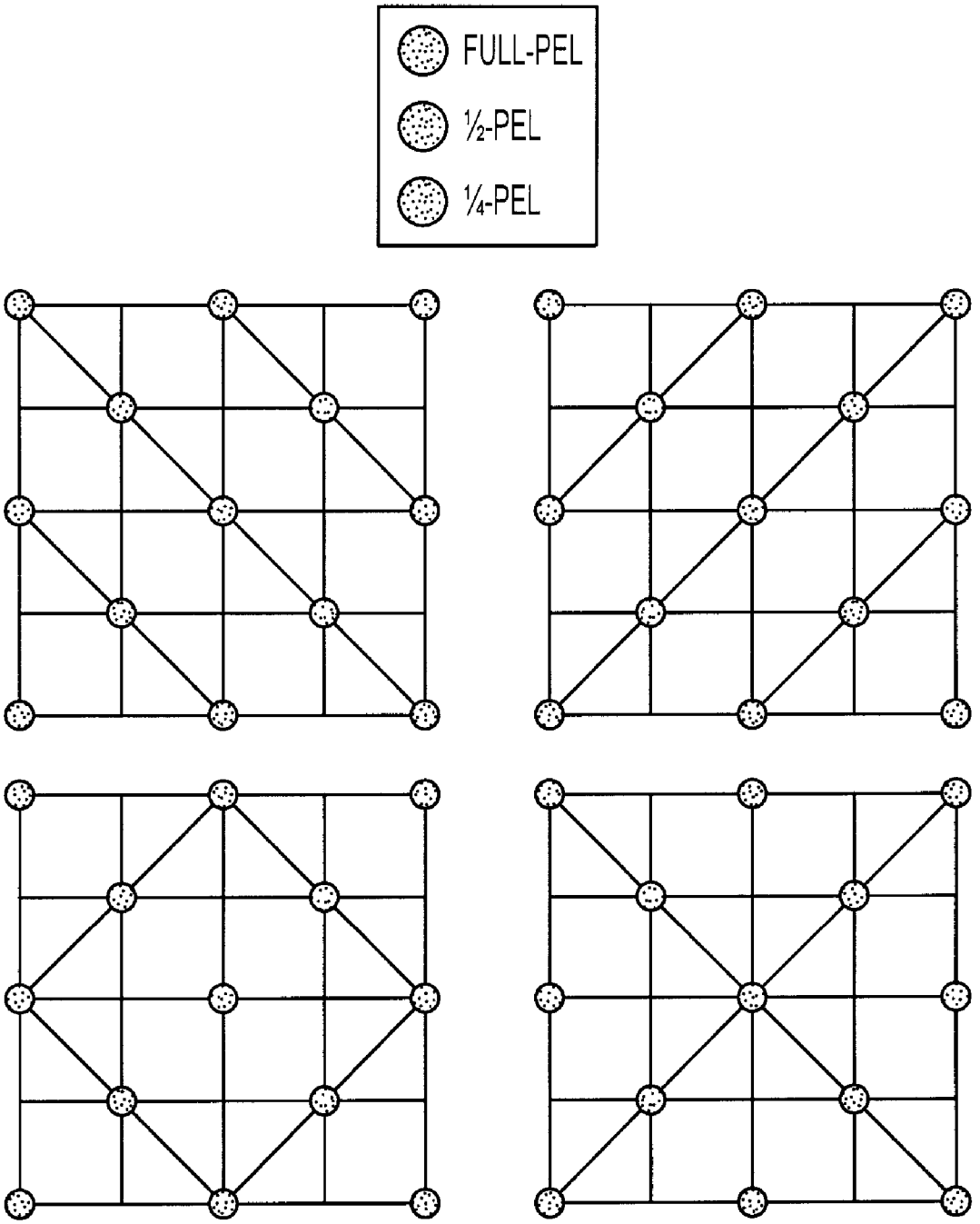


FIG. 15

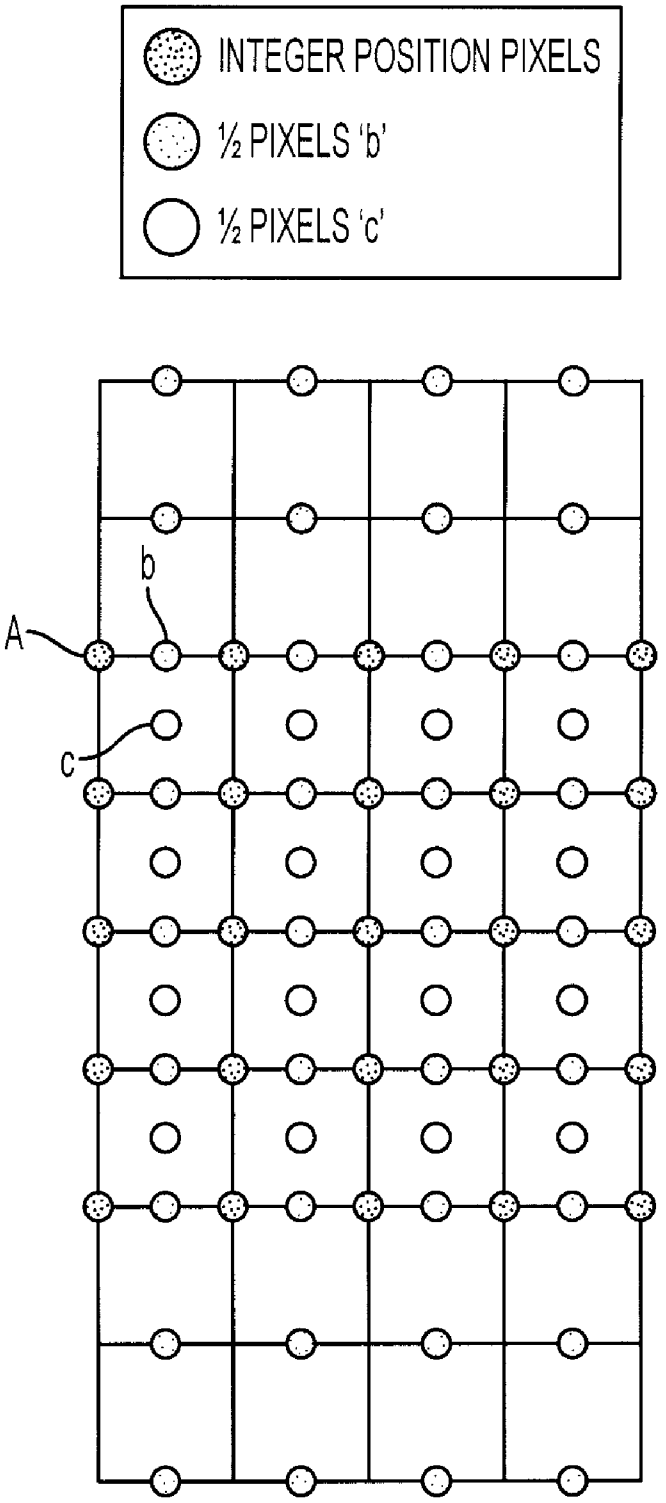


FIG. 16

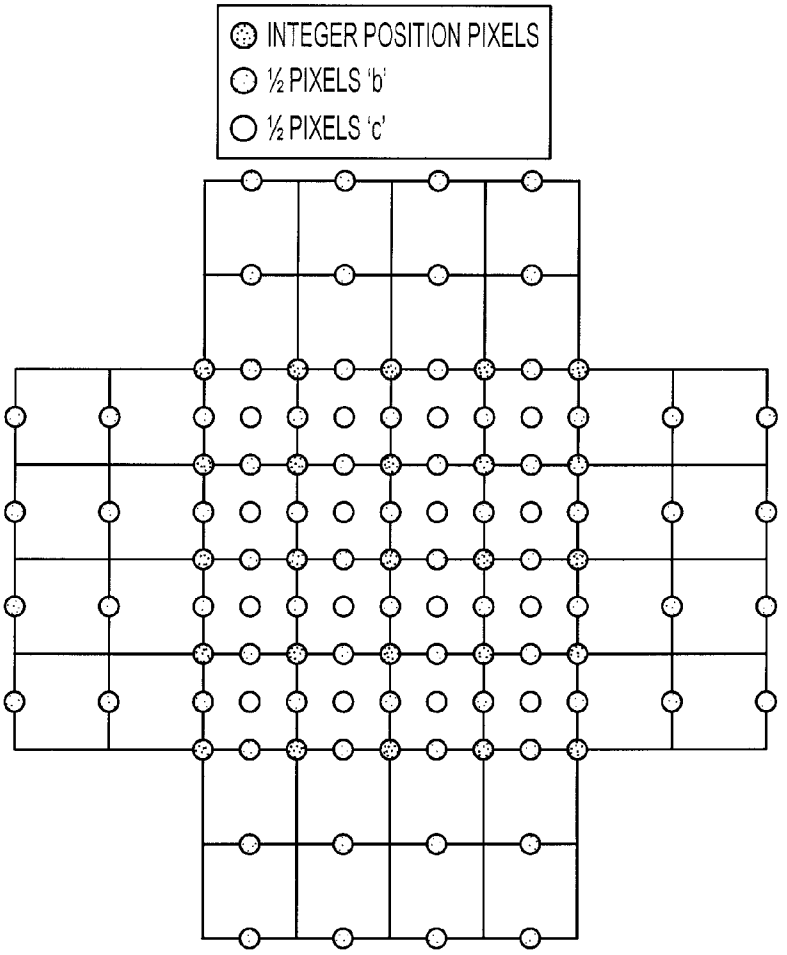


FIG. 17a

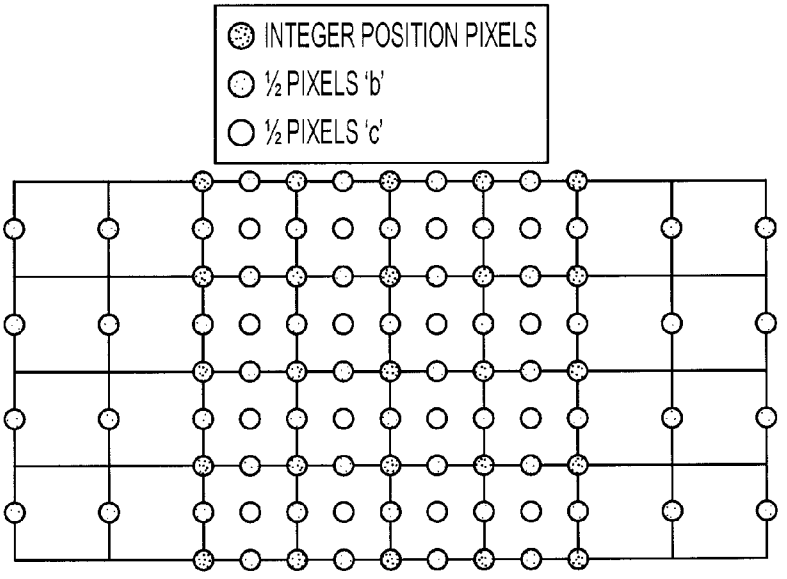


FIG. 17b

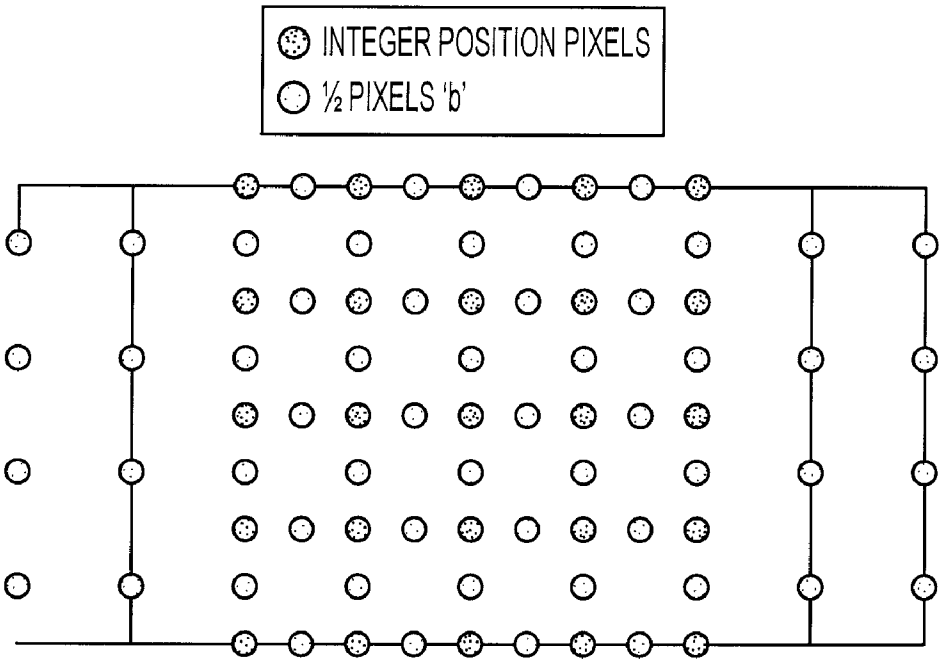


FIG. 18a

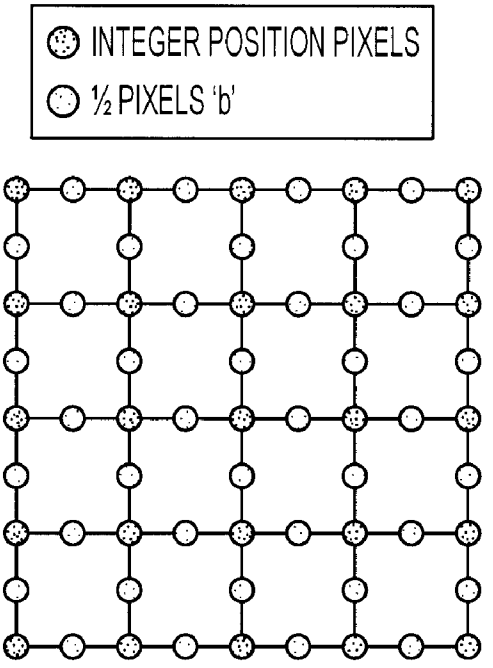


FIG. 18b

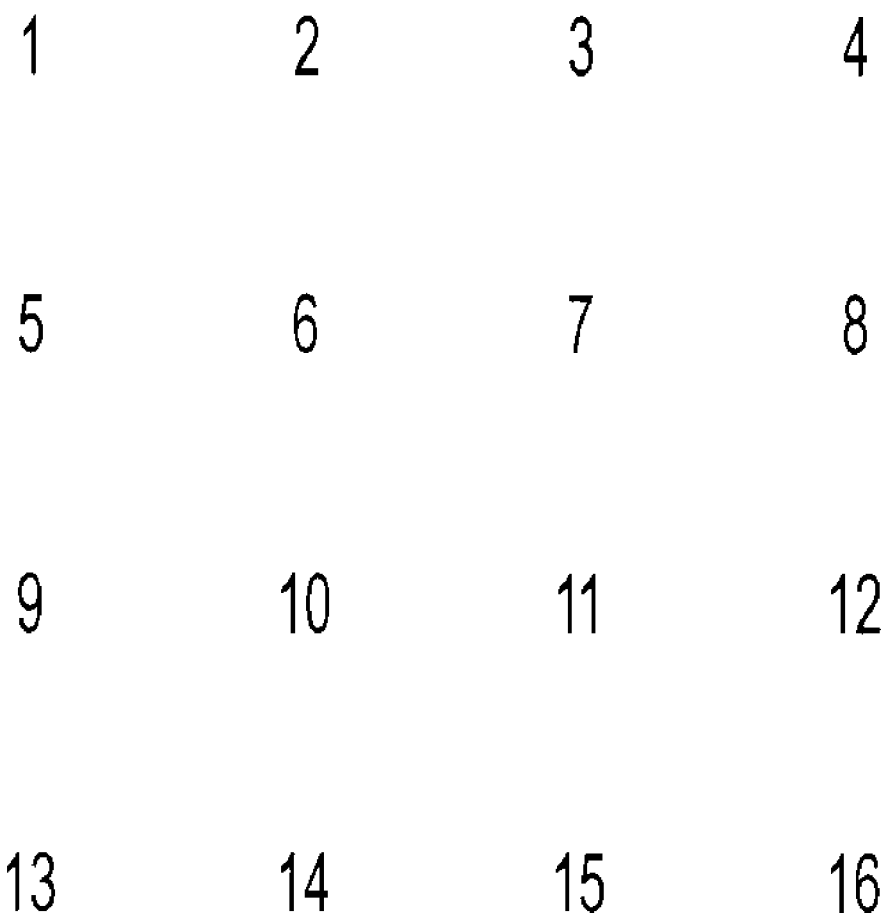


FIG. 19

A	d	b^1	d	b^2	d	b^3	d	A
d	e	d	f	d	f	d	e	
b^1	d	c^{11}	d	c^{12}	d	c^{13}	d	
d	f	d	g	d	g	d	f	
b^2	d	c^{21}	d	c^{22}	d	c^{23}	d	
d	f	d	g	d	g	d	e	
b^3	d	c^{31}	d	c^{32}	d	c^{33}	d	
d	e	d	f	d	f	d	e	
A								

FIG. 20

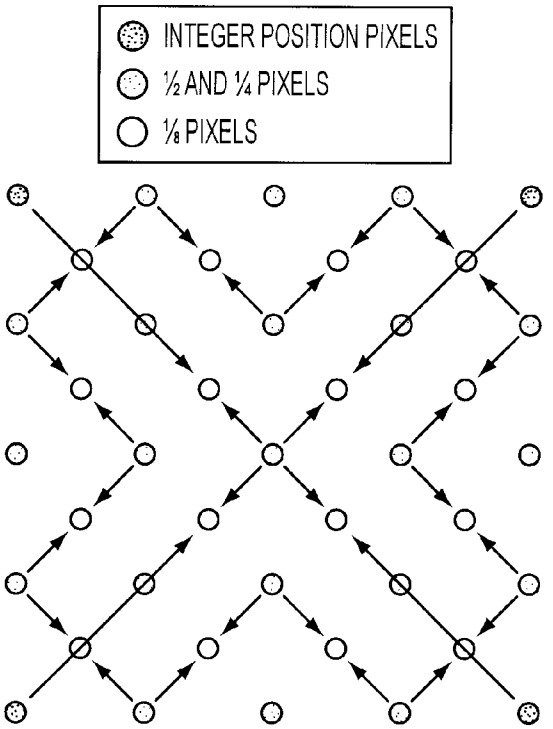


FIG. 21a

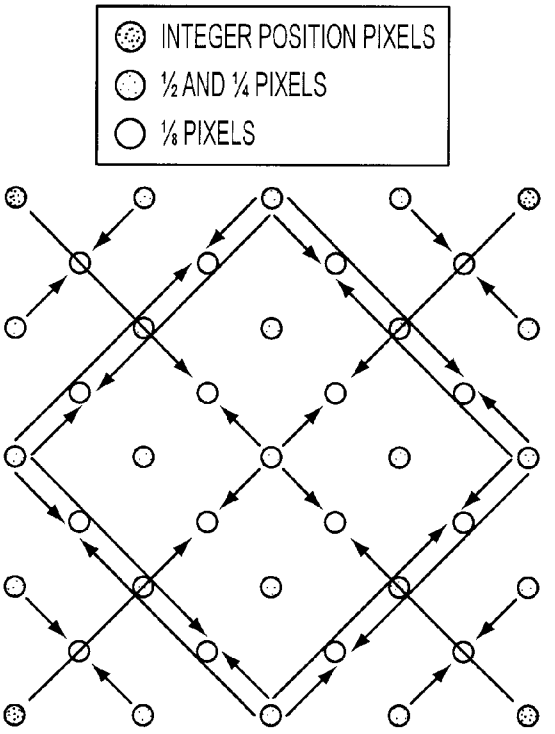


FIG. 21b

1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16
17	18	19	20	21	22	23	24
25	26	27	28	29	30	31	32
33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48
49	50	51	52	53	54	55	56
57	58	59	60	61	62	63	64

FIG. 22

METHOD FOR SUB-PIXEL VALUE INTERPOLATION

CROSS REFERENCE TO RELATED APPLICATIONS

This application is a continuation of, and claims priority to, U.S. application Ser. No. 11/090,717, filed Mar. 25, 2005, now allowed, which is a continuation of, and claims priority to, U.S. application Ser. No. 09/954,608, filed Sep. 17, 2001, now U.S. Pat. No. 6,950,469, all of which are incorporated by reference herein in their entirety.

The present invention relates to a method for sub-pixel value interpolation in the encoding and decoding of data. It relates particularly, but not exclusively, to encoding and decoding of digital video.

BACKGROUND OF THE INVENTION

Digital video sequences, like ordinary motion pictures recorded on film, comprise a sequence of still images, the illusion of motion being created by displaying the images one after the other at a relatively fast frame rate, typically 15 to 30 frames per second. Because of the relatively fast frame rate, images in consecutive frames tend to be quite similar and thus contain a considerable amount of redundant information. For example, a typical scene may comprise some stationary elements, such as background scenery, and some moving areas, which may take many different forms, for example the face of a newsreader, moving traffic and so on. Alternatively, the camera recording the scene may itself be moving, in which case all elements of the image have the same kind of motion. In many cases, this means that the overall change between one video frame and the next is rather small. Of course, this depends on the nature of the movement. For example, the faster the movement, the greater the change from one frame to the next. Similarly, if a scene contains a number of moving elements, the change from one frame to the next is likely to be greater than in a scene where only one element is moving.

It should be appreciated that each frame of a raw, that is uncompressed, digital video sequence comprises a very large amount of image information. Each frame of an uncompressed digital video sequence is formed from an array of image pixels. For example, in a commonly used digital video format, known as the Quarter Common Interchange Format (QCIF), a frame comprises an array of 176×144 pixels, in which case each frame has 25,344 pixels. In turn, each pixel is represented by a certain number of bits, which carry information about the luminance and/or colour content of the region of the image corresponding to the pixel. Commonly, a so-called YUV colour model is used to represent the luminance and chrominance content of the image. The luminance, or Y, component represents the intensity (brightness) of the image, while the colour content of the image is represented by two chrominance components, labelled U and V.

Colour models based on a luminance/chrominance representation of image content provide certain advantages compared with colour models that are based on a representation involving primary colours (that is Red, Green and Blue, RGB). The human visual system is more sensitive to intensity variations than it is to colour variations; YUV colour models exploit this property by using a lower spatial resolution for the chrominance components (U, V) than for the luminance component (Y). In this way the amount of information needed to code the colour information in an image can be reduced with an acceptable reduction in image quality.

The lower spatial resolution of the chrominance components is usually attained by sub-sampling. Typically, a block of 16×16 image pixels is represented by one block of 16×16 pixels comprising luminance information and the corresponding chrominance components are each represented by one block of 8×8 pixels representing an area of the image equivalent to that of the 16×16 pixels of the luminance component. The chrominance components are thus spatially sub-sampled by a factor of 2 in the x and y directions. The resulting assembly of one 16×16 pixel luminance block and two 8×8 pixel chrominance blocks is commonly referred to as a YUV macroblock, or macroblock, for short.

A QCIF image comprises 11×9 macroblocks. If the luminance blocks and chrominance blocks are represented with 8 bit resolution (that is by numbers in the range 0 to 255), the total number of bits required per macroblock is (16×16×8)+2×(8×8×8)=3072 bits. The number of bits needed to represent a video frame in QCIF format is thus 99×3072=304,128 bits. This means that the amount of data required to transmit/record/display a video sequence in QCIF format, represented using a YUV colour model, at a rate of 30 frames per second, is more than 9 Mbps (million bits per second). This is an extremely high data rate and is impractical for use in video recording, transmission and display applications because of the very large storage capacity, transmission channel capacity and hardware performance required.

If video data is to be transmitted in real-time over a fixed line network such as an ISDN (Integrated Services Digital Network) or a conventional PSTN (Public Service Telephone Network), the available data transmission bandwidth is typically of the order of 64 kbits/s. In mobile videotelephony, where transmission takes place at least in part over a radio communications link, the available bandwidth can be as low as 20 kbits/s. This means that a significant reduction in the amount of information used to represent video data must be achieved in order to enable transmission of digital video sequences over low bandwidth communication networks. For this reason video compression techniques have been developed which reduce the amount of information transmitted while retaining an acceptable image quality.

Video compression methods are based on reducing the redundant and perceptually irrelevant parts of video sequences. The redundancy in video sequences can be categorised into spatial, temporal and spectral redundancy. 'Spatial redundancy' is the term used to describe the correlation between neighbouring pixels within a frame. The term 'temporal redundancy' expresses the fact that the objects appearing in one frame of a sequence are likely to appear in subsequent frames, while 'spectral redundancy' refers to the correlation between different colour components of the same image.

Sufficiently efficient compression cannot usually be achieved by simply reducing the various forms of redundancy in a given sequence of images. Thus, most current video encoders also reduce the quality of those parts of the video sequence which are subjectively the least important. In addition, the redundancy of the compressed video bit-stream is itself reduced by means of efficient loss-less encoding. Typically, this is achieved using a technique known as 'variable length coding' (VLC).

Modern video compression standards, such as ITU-T recommendations H.261, H.263(+)(++), H.26L and the Motion Picture Experts Group recommendation MPEG-4 make use of 'motion compensated temporal prediction'. This is a form of temporal redundancy reduction in which the content of some (often many) frames in a video sequence is 'predicted'

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from other frames in the sequence by tracing the motion of objects or regions of an image between frames.

Compressed images which do not make use of temporal redundancy reduction are usually called INTRA-coded or I-frames, whereas temporally predicted images are called INTER-coded or P-frames. In the case of INTER frames, the predicted (motion-compensated) image is rarely precise enough to represent the image content with sufficient quality, and therefore a spatially compressed prediction error (PE) frame is also associated with each INTER frame. Many video compression schemes can also make use of bi-directionally predicted frames, which are commonly referred to as B-pictures or B-frames. B-pictures are inserted between reference or so-called 'anchor' picture pairs (I or P frames) and are predicted from either one or both of the anchor pictures. B-pictures are not themselves used as anchor pictures, that is no other frames are predicted from them, and therefore, they can be discarded from the video sequence without causing deterioration in the quality of future pictures.

The different types of frame that occur in a typical compressed video sequence are illustrated in FIG. **3** of the accompanying drawings. As can be seen from the figure, the sequence starts with an INTRA or I frame **30**. In FIG. **3**, arrows **33** denote the 'forward' prediction process by which P-frames (labelled **34**) are formed. The bi-directional prediction process by which B-frames (**36**) are formed is denoted by arrows **31***a* and **31***b*, respectively.

A schematic diagram of an example video coding system using motion compensated prediction is shown in FIGS. **1** and **2**. FIG. **1** illustrates an encoder **10** employing motion compensation and FIG. **2** illustrates a corresponding decoder **20**. The encoder **10** shown in FIG. **1** comprises a Motion Field Estimation block **11**, a Motion Field Coding block **12**, a Motion Compensated Prediction block **13**, a Prediction Error Coding block **14**, a Prediction Error Decoding block **15**, a Multiplexing block **16**, a Frame Memory **17**, and an adder **19**. The decoder **20** comprises a Motion Compensated Prediction block **21**, a Prediction Error Decoding block **22**, a Demultiplexing block **23** and a Frame Memory **24**.

The operating principle of video coders using motion compensation is to minimise the amount of information in a prediction error frame $E_n(x,y)$, which is the difference between a current frame $I_n(x,y)$ being coded and a prediction frame $P_n(x,y)$. The prediction error frame is thus:

$$E_n(x,y)=I_n(x,y)-P_n(x,y). \quad (1)$$

The prediction frame $P_n(x,y)$ is built using pixel values of a reference frame $R_n(x,y)$, which is generally one of the previously coded and transmitted frames, for example the frame immediately preceding the current frame and is available from the Frame Memory **17** of the encoder **10**. More specifically, the prediction frame $P_n(x,y)$ is constructed by finding so-called 'prediction pixels' in the reference frame $R_n(x,y)$ which correspond substantially with pixels in the current frame. Motion information, describing the relationship (e.g. relative location, rotation, scale etc.) between pixels in the current frame and their corresponding prediction pixels in the reference frame is derived and the prediction frame is constructed by moving the prediction pixels according to the motion information. In this way, the prediction frame is constructed as an approximate representation of the current frame, using pixel values in the reference frame. The prediction error frame referred to above therefore represents the difference between the approximate representation of the current frame provided by the prediction frame and the current frame itself. The basic advantage provided by video encoders that use motion compensated prediction arises from the fact that a comparatively compact description of the current frame can be obtained by representing it in terms of the motion information required to form its prediction together with the associated prediction error information in the prediction error frame.

However, due to the very large number of pixels in a frame, it is generally not efficient to transmit separate motion information for each pixel to the decoder. Instead, in most video coding schemes, the current frame is divided into larger image segments S_k and motion information relating to the segments is transmitted to the decoder. For example, motion information is typically provided for each macroblock of a frame and the same motion information is then used for all pixels within the macroblock. In some video coding standards, such as H.26L, a macroblock can be divided into smaller blocks, each smaller block being provided with its own motion information.

The motion information usually takes the form of motion vectors $[\Delta x(x,y),\Delta y(x,y)]$. The pair of numbers $\Delta x(x,y)$ and $\Delta y(x,y)$ represents the horizontal and vertical displacements of a pixel at location (x,y) in the current frame $I_n(x,y)$ with respect to a pixel in the reference frame $R_n(x,y)$. The motion vectors $[\Delta x(x,y),\Delta y(x,y)]$ are calculated in the Motion Field Estimation block **11** and the set of motion vectors of the current frame $[\Delta x(\cdot),\Delta y(\cdot)]$ is referred to as the motion vector field.

Typically, the location of a macroblock in a current video frame is specified by the (x,y) co-ordinate of its upper left-hand corner. Thus, in a video coding scheme in which motion information is associated with each macroblock of a frame, each motion vector describes the horizontal and vertical displacement $\Delta x(x,y)$ and $\Delta y(x,y)$ of a pixel representing the upper left-hand corner of a macroblock in the current frame $I_n(x,y)$ with respect to a pixel in the upper left-hand corner of a substantially corresponding block of prediction pixels in the reference frame $R_n(x,y)$ (as shown in FIG. **4***b*).

Motion estimation is a computationally intensive task. Given a reference frame $R_n(x,y)$ and, for example, a square macroblock comprising N×N pixels in a current frame (as shown in FIG. **4***a*), the objective of motion estimation is to find an N×N pixel block in the reference frame that matches the characteristics of the macroblock in the current picture according to some criterion. This criterion can be, for example, a sum of absolute differences (SAD) between the pixels of the macroblock in the current frame and the block of pixels in the reference frame with which it is compared. This process is known generally as 'block matching'. It should be noted that, in general, the geometry of the block to be matched and that in the reference frame do not have to be the same, as real-world objects can undergo scale changes, as well as rotation and warping. However, in current international video coding standards, only a translational motion model is used (see below) and thus fixed rectangular geometry is sufficient.

Ideally, in order to achieve the best chance of finding a match, the whole of the reference frame should be searched. However, this is impractical as it imposes too high a computational burden on the video encoder. Instead, the search region is restricted to region $[-p,p]$ around the original location of the macroblock in the current frame, as shown in FIG. **4***c*.

In order to reduce the amount of motion information to be transmitted from the encoder **10** to the decoder **20**, the motion vector field is coded in the Motion Field Coding block **12** of the encoder **10**, by representing it with a motion model. In this process, the motion vectors of image segments are re-expressed using certain predetermined functions or, in other words, the motion vector field is represented with a model.

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Almost all currently used motion vector field models are additive motion models, complying with the following general formula:

$$\Delta x(x, y) = \sum_{i=0}^{N-1} a_i f_i(x, y) \quad (2)$$

$$\Delta y(x, y) = \sum_{i=0}^{M-1} b_i g_i(x, y) \quad (3)$$

where coefficients a_i and b_i are called motion coefficients. The motion coefficients are transmitted to the decoder **20** (information stream **2** in FIGS. **1** and **2**). Functions f_i and g_i are called motion field basis functions, and are known both to the encoder and decoder. An approximate motion vector field $(\tilde{\Delta}x(x,y),\tilde{\Delta}y(x,y))$ can be constructed using the coefficients and the basis functions. As the basis functions are known to (that is stored in) both the encoder **10** and the decoder **20**, only the motion coefficients need to be transmitted to the encoder, thus reducing the amount of information required to represent the motion information of the frame.

The simplest motion model is the translational motion model which requires only two coefficients to describe the motion vectors of each segment. The values of motion vectors are given by:

$$\Delta x(x,y)=a_0$$

$$\Delta y(x,y)=b_0 \quad (4)$$

This model is widely used in various international standards (ISO MPEG-1, MPEG-2, MPEG-4, ITU-T Recommendations H.261 and H.263) to describe the motion of 16×16 and 8×8 pixel blocks. Systems which use a translational motion model typically perform motion estimation at full pixel resolution or some integer fraction of full pixel resolution, for example at half or one quarter pixel resolution.

The prediction frame $P_n(x,y)$ is constructed in the Motion Compensated Prediction block **13** in the encoder **10**, and is given by:

$$P_n(x,y)=R_n[x+\tilde{\Delta}x(x,y),y+\tilde{\Delta}y(x,y)] \quad (5)$$

In the Prediction Error Coding block **14**, the prediction error frame $E_n(x,y)$ is typically compressed by representing it as a finite series (transform) of some 2-dimensional functions. For example, a 2-dimensional Discrete Cosine Transform (DCT) can be used. The transform coefficients are quantised and entropy (for example Huffman) coded before they are transmitted to the decoder (information stream **1** in FIGS. **1** and **2**). Because of the error introduced by quantisation, this operation usually produces some degradation (loss of information) in the prediction error frame $E_n(x,y)$. To compensate for this degradation, the encoder **10** also comprises a Prediction Error Decoding block **15**, where a decoded prediction error frame $\tilde{E}_n(x,y)$ is constructed using the transform coefficients. This locally decoded prediction error frame is added to the prediction frame $P_n(x,y)$ in the adder **19** and the resulting decoded current frame $\tilde{I}_n(x,y)$ is stored in the Frame Memory **17** for further use as the next reference frame $R_{n+1}(x,y)$.

The information stream **2** carrying information about the motion vectors is combined with information about the prediction error in multiplexer **16** and an information stream **3** containing typically at least those two types of information is sent to the decoder **20**.

The operation of a corresponding video decoder **20** will now be described.

The Frame Memory **24** of the decoder **20** stores a previously reconstructed reference frame $R_n(x,y)$. The prediction frame $P_n(x,y)$ is constructed in the Motion Compensated Prediction block **21** of the decoder **20** according to equation 5, using received motion coefficient information and pixel values of the previously reconstructed reference frame $R_n(x,y)$. The transmitted transform coefficients of the prediction error frame $E_n(x,y)$ are used in the Prediction Error Decoding block **22** to construct the decoded prediction error frame $\tilde{E}_n(x,y)$. The pixels of the decoded current frame $\tilde{I}_n(x,y)$ are then reconstructed by adding the prediction frame $P_n(x,y)$ and the decoded prediction error frame $\tilde{E}_n(x,y)$:

$$\tilde{I}_n(x,y)=P_n(x,y)+\tilde{E}_n(x,y)=R_n[x+\tilde{\Delta}x(x,y),y+\tilde{\Delta}y(x,y)]+\tilde{E}_n(x,y). \quad (6)$$

This decoded current frame may be stored in the Frame Memory **24** as the next reference frame $R_{n+1}(x,y)$.

In the description of motion compensated encoding and decoding of digital video presented above, the motion vector $[\Delta x(x,y),\Delta y(x,y)]$ describing the motion of a macroblock in the current frame with respect to the reference frame $R_n(x,y)$ can point to any of the pixels in the reference frame. This means that motion between frames of a digital video sequence can only be represented at a resolution which is determined by the image pixels in the frame (so-called full pixel resolution). Real motion, however, has arbitrary precision, and thus the system described above can only provide approximate modelling of the motion between successive frames of a digital video sequence. Typically, modelling of motion between video frames with full pixel resolution is not sufficiently accurate to allow efficient minimisation of the prediction error (PE) information associated with each macroblock/frame. Therefore, to enable more accurate modelling of real motion and to help reduce the amount of PE information that must be transmitted from encoder to decoder, many video coding standards, such as H.263(+)(++) and H.26L, allow motion vectors to point 'in between' image pixels. In other words, the motion vectors can have 'sub-pixel' resolution. Allowing motion vectors to have sub-pixel resolution adds to the complexity of the encoding and decoding operations that must be performed, so it is still advantageous to limit the degree of spatial resolution a motion vector may have. Thus, video coding standards, such as those previously mentioned, typically only allow motion vectors to have full-, half- or quarter-pixel resolution.

Motion estimation with sub-pixel resolution is usually performed as a two-stage process, as illustrated in FIG. **5**, for a video coding scheme which allows motion vectors to have full- or half-pixel resolution. In the first step, a motion vector having full-pixel resolution is determined using any appropriate motion estimation scheme, such as the block-matching process described in the foregoing. The resulting motion vector, having full-pixel resolution is shown in FIG. **5**.

In the second stage, the motion vector determined in the first stage is refined to obtain the desired half-pixel resolution. In the example illustrated in FIG. **5**, this is done by forming eight new search blocks of 16×16 pixels, the location of the top-left corner of each block being marked with an X in FIG. **5**. These locations are denoted as $[\Delta x+m/2,\Delta y+n/2]$, where m and n can take the values −1, 0 and +1, but cannot be zero at the same time. As only the pixel values of original image pixels are known, the values (for example luminance and/or chrominance values) of the sub-pixels residing at half-pixel locations must be estimated for each of the eight new search blocks, using some form of interpolation scheme.

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Having interpolated the values of the sub-pixels at half-pixel resolution, each of the eight search blocks is compared with the macroblock whose motion vector is being sought. As in the block matching process performed in order to determine the motion vector with full pixel resolution, the macroblock is compared with each of the eight search blocks according to some criterion, for example a SAD. As a result of the comparisons, a minimum SAD value will generally be obtained. Depending on the nature of the motion in the video sequence, this minimum value may correspond to the location specified by the original motion vector (having full-pixel resolution), or it may correspond to a location having a half-pixel resolution. Thus, it is possible to determine whether a motion vector should point to a full-pixel or sub-pixel location and if sub-pixel resolution is appropriate, to determine the correct sub-pixel resolution motion vector. It should also be appreciated that the scheme just described can be extended to other sub-pixel resolutions (for example, one-quarter-pixel resolution) in an entirely analogous fashion.

In practice, the estimation of a sub-pixel value in the reference frame is performed by interpolating the value of the sub-pixel from surrounding pixel values. In general, interpolation of a sub-pixel value F(x,y) situated at a non-integer location (x,y)=(n+Δx, m+Δy), can be formulated as a two-dimensional operation, represented mathematically as:

$$F(x, y) = \sum_{k=-K}^{K=1} \sum_{l=-L}^{L=1} f(k+K, l+L) F(n+k, m+l) \tag{7}$$

where f(k,l) are filter coefficients and n and m are obtained by truncating x and y, respectively, to integer values. Typically, the filter coefficients are dependent on the x and y values and the interpolation filters are usually so-called 'separable filters', in which case sub-pixel value F(x,y) can be calculated as follows:

$$F(x, y) = \sum_{k=-K}^{K=1} f(k+K) \sum_{l=-K}^{K=1} f(l+K) F(n+k, m+l) \tag{8}$$

The motion vectors are calculated in the encoder. Once the corresponding motion coefficients are transmitted to the decoder, it is a straightforward matter to interpolate the required sub-pixels using an interpolation method identical to that used in the encoder. In this way, a frame following a reference frame in the Frame Memory **24**, can be reconstructed from the reference frame and the motion vectors.

The simplest way of applying sub-pixel value interpolation in a video coder is to interpolate each sub-pixel value every time it is needed. However, this is not an efficient solution in a video encoder, because it is likely that the same sub-pixel value will be required several times and thus calculations to interpolate the same sub-pixel value will be performed multiple times. This results in an unnecessary increase of computational complexity/burden in the encoder.

An alternative approach, which limits the complexity of the encoder, is to pre-calculate and store all sub-pixel values in a memory associated with the encoder. This solution is called interpolation 'before-hand' interpolation hereafter in this document. While limiting complexity, before-hand interpolation has the disadvantage of increasing memory usage by a large margin. For example, if the motion vector accuracy is one quarter pixel in both horizontal and vertical dimensions, storing pre-calculated sub-pixel values for a complete image results in a memory usage that is 16 times that required to store the original, non-interpolated image. In addition, it involves the calculation of some sub-pixels which might not actually be required in calculating motion vectors in the encoder. Before-hand interpolation is also particularly inefficient in a video decoder, as the majority of pre-calculated sub-pixel values will never be required by the decoder. Thus, it is advantageous not to use pre-calculation in the decoder.

So-called 'on-demand' interpolation can be used to reduce memory requirements in the encoder. For example, if the desired pixel precision is quarter pixel resolution, only sub-pixels at one half unit resolution are interpolated before-hand for the whole frame and stored in the memory. Values of one-quarter pixel resolution sub-pixels are only calculated during the motion estimation/compensation process as and when it is required. In this case memory usage is only 4 times that required to store the original, non-interpolated image.

It should be noted that when before-hand interpolation is used, the interpolation process constitutes only a small fraction of the total encoder computational complexity/burden, since every pixel is interpolated just once. Therefore, in the encoder, the complexity of the interpolation process itself is not very critical when before-hand sub-pixel value interpolation is used. On the other hand, on-demand interpolation poses a much higher computational burden on the encoder, since sub-pixels may be interpolated many times. Hence the complexity of interpolation process, which may be considered in terms of the number of computational operations or operational cycles that must be performed in order to interpolate the sub-pixel values, becomes an important consideration.

In the decoder, the same sub-pixel values are used a few times at most and some are not needed at all. Therefore, in the decoder it is advantageous not to use before-hand interpolation at all, that is, it is advantageous not to pre-calculate any sub-pixel values.

Two interpolation schemes have been developed as part of the work ongoing in the ITU-Telecommunications Standardization Sector, Study Group 16, Video Coding Experts Group (VCEG), Questions 6 and 15. These approaches were proposed for incorporation into ITU-T recommendation H.26L and have been implemented in test models (TML) for the purposes of evaluation and further development. The test model corresponding to Question 15 is referred to as Test Model 5 (TML5), while that resulting from Question 6 is known as Test Model 6 (TML6). The interpolation schemes proposed in both TML5 and TML6 will now be described.

Throughout the description of the sub-pixel value interpolation scheme used in test model TML5, reference will be made to FIG. **12***a*, which defines a notation for describing pixel and sub-pixel locations specific to TML5. A separate notation, defined in FIG. **13***a*, will be used in the discussion of the sub-pixel value interpolation scheme used in TML6. A still further notation, illustrated in FIG. **14***a*, will be used later in the text in connection with the sub-pixel value interpolation method according to the invention. It should be appreciated that the three different notations used in the text are intended to assist in the understanding of each interpolation method and to help distinguish differences between them. However, in all three figures, the letter A is used to denote original image pixels (full pixel resolution). More specifically, the letter A represents the location of pixels in the image data representing a frame of a video sequence, the pixel values of pixels A being either received as current frame $I_n(x,y)$ from a video source, or reconstructed and stored as a reference frame $R_n(x, y)$ in the Frame Memory **17**, **24** of the encoder **10** or the

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decoder **20**. All other letters represent sub-pixel locations, the values of the sub-pixels situated at the sub-pixel locations being obtained by interpolation.

Certain other terms will also be used in a consistent manner throughout the text to identify particular pixel and sub-pixel locations. These are as follows:

The term 'unit horizontal location' is used to describe the location of any sub-pixel that is constructed in a column of the original image data. Sub-pixels c and e in FIGS. **12***a* and **13***a*, as well as sub-pixels b and e in FIG. **14***a* have unit horizontal locations.

The term 'unit vertical location' is used to describe any sub-pixel that is constructed in a row of the original image data. Sub-pixels b and d in FIGS. **12***a* and **13***a* as well as sub-pixels b and d in FIG. **14***a* have unit vertical locations.

By definition, pixels A have unit horizontal and unit vertical locations.

The term 'half horizontal location' is used to describe the location of any sub-pixel that is constructed in a column that lies at half pixel resolution. Sub-pixels b, c, and e shown in FIGS. **12***a* and **13***a* fall into this category, as do sub-pixels b, c and f in FIG. **14***a*. In a similar manner, the term 'half vertical location' is used to describe the location of any sub-pixel that is constructed in a row that lies at half-pixel resolution, such as sub-pixels c and d in FIGS. **12***a* and **13***a*, as well as sub-pixels b, c and g in FIG. **14***a*.

Furthermore, the term 'quarter horizontal location' refers to any sub-pixel that is constructed in a column which lies at quarter-pixel resolution, such as sub-pixels d and e in FIG. **12***a*, sub-pixels d and g in FIG. **13***a* and sub-pixels d, g and h in FIG. **14***a*. Analogously, the term 'quarter vertical location' refers to sub-pixels that are constructed in a row which lies at quarter-pixel resolution. In FIG. **12***a*, sub-pixels e and f fall into this category, as do sub-pixels e, f and g in FIG. **13***a* and sub-pixels e, f and h in FIG. **14***a*.

The definition of each of the terms described above is shown by 'envelopes' drawn on the corresponding figures.

It should further be noted that it is often convenient to denote a particular pixel with a two-dimensional reference. In this case, the appropriate two-dimensional reference can be obtained by examining the intersection of the envelopes in FIGS. **12***a*, **13***a* and **14***a*. Applying this principle, pixel d in FIG. **12***a*, for example, has a half horizontal and half vertical location and sub-pixel e has a unit horizontal and quarter vertical location. In addition, and for ease of reference, sub-pixels that reside at half unit horizontal and unit vertical locations, unit horizontal and half unit vertical locations as well as half unit horizontal and half unit vertical locations, will be referred to as ½ resolution sub-pixels. Sub-pixels which reside at any quarter unit horizontal and/or quarter unit vertical location will be referred to as ¼ resolution sub-pixels.

It should also be noted that in the descriptions of the two test models and in the detailed description of the invention itself, it will be assumed that pixels have a minimum value of 0 and a maximum value of 2^n-1 where n is the number of bits reserved for a pixel value. The number of bits is typically 8. After a sub-pixel has been interpolated, if the value of that interpolated sub-pixel exceeds the value of 2^n-1, it is restricted to the range of $[0, 2^n-1]$, i.e. values lower than the minimum allowed value will become the minimum value (0) and values larger than the maximum will the become maximum value (2^n-1). This operation is called clipping.

The sub-pixel value interpolation scheme according to TML5 will now be described in detail with reference to FIGS. **12***a*, **12***b* and **12***c*.

1. The value for the sub-pixel at half unit horizontal and unit vertical location, that is ½ resolution sub-pixel b in FIG. **12***a*, is calculated using a 6-tap filter. The filter interpolates a value for ½ resolution sub-pixel b based upon the values of the 6 pixels (A_1 to A_6) situated in a row at unit horizontal locations and unit vertical locations symmetrically about b, as shown in FIG. **12***b*, according to the formula $b=(A_1-5A_2+20A_3+20A_4-5A_5+A_6+16)/32$. The operator / denotes division with truncation. The result is clipped to lie in the range $[0, 2^n-1]$.
2. Values for the ½ resolution sub-pixels labelled c are calculated using the same six tap filter as used in step 1 and the six nearest pixels or sub-pixels (A or b) in the vertical direction. Referring now to FIG. **12***c*, the filter interpolates a value for the ½ resolution sub-pixel c located at unit horizontal and half vertical location based upon the values of the 6 pixels (A_1 to A_6) situated in a column at unit horizontal locations and unit vertical locations symmetrically about c, according to the formula $c=(A_1-5A_2+20A_3+20A_4-5A_5+A_6+16)/32$. Similarly, a value for the ½ resolution sub-pixel c at half horizontal and half vertical location is calculated according to $c=(b_1-5b_2+20b_3+20b_4-5b_5+b_6+16)/32$. Again, the operator / denotes division with truncation. The values calculated for the c sub-pixels are further clipped to lie in the range $[0, 2^n-1]$.

At this point in the interpolation process the values of all ½ resolution sub-pixels have been calculated and the process proceeds to the calculation of ¼ resolution sub-pixel values.

3. Values for the ¼ resolution sub-pixels labelled d are calculated using linear interpolation and the values of the nearest pixels and/or ½ resolution sub-pixels in the horizontal direction. More specifically, values for ¼ resolution sub-pixels d located at quarter horizontal and unit vertical locations, are calculated by taking the average of the immediately neighbouring pixel at unit horizontal and unit vertical location (pixel A) and the immediately neighbouring ½ resolution sub-pixel at half horizontal and unit vertical location (sub-pixel b), i.e. according to $d=(A+b)/2$. Values for ¼ resolution sub-pixels d located at quarter horizontal and half vertical locations, are calculated by taking the average of the immediately neighbouring ½ resolution sub-pixels c which lie at unit horizontal and half vertical location and half horizontal and half vertical locations respectively, i.e. according to $d=(c_1+c_2)/2$. Again operator / indicates division with truncation.
4. Values for the ¼ resolution sub-pixels labelled e are calculated using linear interpolation and the values of the nearest pixels and/or ½ resolution sub-pixels in the vertical direction. In particular, ¼ resolution sub-pixels e at unit horizontal and quarter vertical locations are calculated by taking the average of the immediately neighbouring pixel at unit horizontal and unit vertical location (pixel A) and the immediately neighbouring sub-pixel at unit horizontal and half vertical location (sub-pixel c) according to $e=(A+c)/2$. ¼ resolution sub-pixels e_3 at half horizontal and quarter vertical locations are calculated by taking the average of the immediately neighbouring sub-pixel at half horizontal and unit vertical location (sub-pixel b) and the immediately neighbouring sub-pixel at half horizontal and half vertical location (sub-pixel c), according to $e=(b+c)/2$. Furthermore, ¼ resolution sub-pixels e at quarter horizontal and quarter vertical locations are calculated by taking the average of the immediately neighbouring sub-pixels at quarter horizontal and unit vertical location and the corresponding sub-pixel at quarter horizontal and half vertical location (sub-pixels d), according to $e=(d_1+d_2)/2$. Once more, operator / indicates division with truncation.

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5. The value for ¼ resolution sub-pixel f is interpolated by averaging the values of the 4 closest pixels values at unit horizontal and vertical locations, according to $f=(A_1+A_2+A_3+A_4+2)/4$, where pixels A_1, A_2, A_3 and A_4 are the four nearest original pixels.

A disadvantage of TML5 is that the decoder is computationally complex. This results from the fact that TML5 uses an approach in which interpolation of ¼ resolution sub-pixel values depends upon the interpolation of ½ resolution sub-pixel values. This means that in order to interpolate the values of the ¼ resolution sub-pixels, the values of the ½ resolution sub-pixels from which they are determined must be calculated first. Furthermore, since the values of some of the ¼ resolution sub-pixels depend upon the interpolated values obtained for other ¼ resolution sub-pixels, truncation of the ¼ resolution sub-pixel values has a deleterious effect on the precision of some of the ¼ resolution sub-pixel values. Specifically, the ¼ resolution sub-pixel values are less precise than they would be if calculated from values that had not been truncated and clipped. Another disadvantage of TML5 is that it is necessary to store the values of the ½ resolution sub-pixels in order to interpolate the ¼ resolution sub-pixel values. Therefore, excess memory is required to store a result which is not ultimately required.

The sub-pixel value interpolation scheme according to TML6, referred to herein as direct interpolation, will now be described. In the encoder the interpolation method according to TML6 works like the previously described TML5 interpolation method, except that maximum precision is retained throughout. This is achieved by using intermediate values which are neither rounded nor clipped. A step-by-step description of interpolation method according to TML6 as applied in the encoder is given below with reference to FIGS. **13***a*, **13***b* and **13***c*.

1. The value for the sub-pixel at half unit horizontal and unit vertical location, that is ½ resolution sub-pixel b in FIG. **13***a*, is obtained by first calculating an intermediate value b using a six tap filter. The filter calculates b based upon the values of the 6 pixels (A_1 to A_6) situated in a row at unit horizontal locations and unit vertical locations symmetrically about b, as shown in FIG. **13***b*, according to the formula $b=(A_1-5A_2+20A_3+20A_4-5A_5+A_6)$. The final value of b is then calculated as b=(b+16)/32 and is clipped to lie in the range $[0, 2^n-1]$. As before, the operator / denotes division with truncation.
2. Values for the ½ resolution sub-pixels labelled c are obtained by first calculating intermediate values c. Referring to FIG. **13***c*, an intermediate value c for the ½ resolution sub-pixel c located at unit horizontal and half vertical location is calculated based upon the values of the 6 pixels (A_1 to A_6) situated in a column at unit horizontal locations and unit vertical locations symmetrically about c, according to the formula $c=(A_1-5A_2+20A_3+20A_4-5A_5+A_6)$. The final value for the ½ resolution sub-pixel c located at unit horizontal and half vertical location is then calculated according to c=(c+16)/32. Similarly, an intermediate value c for the ½ resolution sub-pixel c at half horizontal and half vertical location is calculated according to $c=(b_1-5b_2+20b_3+20b_4-5b_5+b_6)$. A final value for this ½ resolution sub-pixel is then calculated according to (c+512)/1024. Again, the operator / denotes division with truncation and the values calculated for ½ resolution sub-pixels c are further clipped to lie in the range $[0, 2^n-1]$.
3. Values for the ¼ resolution sub-pixels labelled d are calculated as follows. Values for ¼ resolution sub-pixels d located at quarter horizontal and unit vertical locations, are calculated from the value of the immediately neighbouring pixel at unit horizontal and unit vertical location (pixel A) and the intermediate value b calculated in step (1) for the immediately neighbouring ½ resolution sub-pixel at half horizontal and unit vertical location (½ resolution sub-pixel b), according to d=(32A+b+32)/64. Values for ¼ resolution sub-pixels d located at quarter horizontal and half vertical locations, are interpolated using the intermediate values c calculated for the immediately neighbouring ½ resolution sub-pixels c which lie at unit horizontal and half vertical location and half horizontal and half vertical locations respectively, according to $d=(32c_1, +c_2+1024)/2048$. Again operator / indicates division with truncation and the finally obtained ¼ resolution sub-pixel values d are clipped to lie in the range $[0, 2^n-1]$.
4. Values for the ¼ resolution sub-pixels labelled e are calculated as follows. Values for ¼ resolution sub-pixels e located at unit horizontal and quarter vertical locations are calculated from the value of the immediately neighbouring pixel at unit horizontal and unit vertical location (pixel A) and the intermediate value c calculated in step (2) for the immediately neighbouring ½ resolution sub-pixel at unit horizontal and half vertical location, according to e=(32A+c+32)/64. Values for ¼ resolution sub-pixels e located at half horizontal and quarter vertical locations are calculated from the intermediate value b calculated in step (1) for the immediately neighbouring ½ resolution sub-pixel at half horizontal and unit vertical location and the intermediate value c calculated in step (2) for the immediately neighbouring ½ resolution sub-pixel at half horizontal and half vertical location, according to e=(32b+c+1024)/2048. Once more, operator / indicates division with truncation and the finally obtained ¼ resolution sub-pixel values e are clipped to lie in the range $[0, 2^n-1]$.
5. Values for ¼ resolution sub-pixels labelled g are computed using the value of the nearest original pixel A and the intermediate values of the three nearest neighbouring ½ resolution sub-pixels, according to $g=(1024A+32b+32c_1+c_2+2048)/4096$. As before, operator / indicates division with truncation and the finally obtained for ¼ resolution sub-pixel values g are clipped to lie in the range $[0, 2^n-1]$.
6. The value for ¼ resolution sub-pixel f is interpolated by averaging the values of the 4 closest pixels at unit horizontal and vertical locations, according to $f=(A_1+A_2+A_3+A_{4+2})/4$, where the locations of pixels A_1, A_2, A_3 and A_4 are the four nearest original pixels.

In the decoder, sub-pixel values can be obtained directly by applying 6-tap filters in horizontal and vertical directions. In the case of ¼ sub-pixel resolution, referring to FIG. **13***a*, the filter coefficients applied to pixels and sub-pixels at unit vertical location are [0, 0, 64, 0, 0, 0] for a set of six pixels A, [1, −5, 52, 20, −5, 1] for a set of six sub-pixels d, [2, −10, 40, 40, −10, 2] for a set of six sub-pixels b, and [1, −5, 20, 52, −5, 1] for a set of six sub-pixels d. These filter coefficients are applied to respective sets of pixels or sub-pixels in the same row as the sub-pixel values being interpolated.

After applying the filters in the horizontal and vertical directions, interpolated value c is normalized according to c=(c+2048)/4096 and clipped to lie in the range $[0, 2^n-1]$. When a motion vector points to an integer pixel position in either the horizontal or vertical direction, many zero coefficients are used. In a practical implementation of TML6, different branches are used in the software which are optimised for the different sub-pixel cases so that there are no multiplications by zero coefficients.

It should be noted that in TML6, ¼ resolution sub-pixel values are obtained directly using the intermediate values referred to above and are not derived from rounded and

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clipped values for ½ resolution sub-pixels. Therefore, in obtaining the ¼ resolution sub-pixel values, it is not necessary to calculate final values for any of the ½ resolution sub-pixels. Specifically, it is not necessary to carry out the truncation and clipping operations associated with the calculation of final values for the ½ resolution sub-pixels. Neither is it necessary to have stored final values for ½ resolution sub-pixels for use in the calculation of the ¼ resolution sub-pixel values. Therefore TML6 is computationally less complex than TML5, as fewer truncating and clipping operations are required. However, a disadvantage of TML6 is that high precision arithmetic is required both in the encoder and in the decoder. High precision interpolation requires more silicon area in ASICs and requires more computations in some CPUs. Furthermore, implementation of direct interpolation as specified in TML6 in an on-demand fashion has a high memory requirement. This is an important factor, particularly in embedded devices.

In view of the previously presented discussion, it should be appreciated that due to the different requirements of the video encoder and decoder with regard to sub-pixel interpolation, there exists a significant problem in developing a method of sub-pixel value interpolation capable of providing satisfactory performance in both the encoder and decoder. Furthermore, neither of the current test models (TML5, TML6) described in the foregoing can provide a solution that is optimum for application in both encoder and decoder.

SUMMARY OF THE INVENTION

According to a first aspect of the invention there is provided method of interpolation in video coding in which an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, is interpolated to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $\frac{1}{2}^x$, where x is a positive integer having a maximum value N, the method comprising:

a) when values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations are required, interpolating such values directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) when values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations are required, interpolating such values directly using a choice of a first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and a second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations, the first and second weighted sums of values being calculated according to step (a); and

c) when a value for a sub-pixel situated at a $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical location is required, interpolating such a value by taking a weighted average of the value of a first sub-pixel or pixel situated at a $\frac{1}{2}^{N-m}$ unit horizontal and $\frac{1}{2}^{N-n}$ unit vertical location and the value of a second sub-pixel or pixel located at a $\frac{1}{2}^{N-p}$ unit horizontal and $\frac{1}{2}^{N-q}$ unit vertical location, variables m, n, p and q taking integer values in the range 1 to N such that the first and second sub-pixels or pixels are located diagonally with respect to the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location.

Preferably a first and a second weight are used in the weighted average referred to in (c), the relative magnitudes of the weights being inversely proportional to the (straight-line diagonal) proximity of the first and the second sub-pixel or pixel to the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location.

In a situation where the first and the second sub-pixel or pixel are symmetrically located with respect to (equidistant from) the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location, the first and second weights may have equal values.

The first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations in step b) may be used when a sub-pixel at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^N$ unit vertical location is required.

The second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations in step b) may be used when a sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location is required.

In one embodiment, when values for sub-pixels at $\frac{1}{2}^N$ unit horizontal and unit vertical locations, and $\frac{1}{2}^N$ horizontal and $\frac{1}{2}^{N-1}$ vertical locations are required, such values are interpolated by taking the average of the values of a first pixel or sub-pixel located at a vertical location corresponding to that of the sub-pixel being calculated and unit horizontal location and a second pixel or sub-pixel located at a vertical location corresponding to that of the sub-pixel being calculated and $\frac{1}{2}^{N-1}$ unit horizontal location.

When values for sub-pixels at unit horizontal and $\frac{1}{2}^N$ unit vertical locations, and $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations are required, they may be interpolated by taking the average of the values of a first pixel or sub-pixel located at a horizontal location corresponding to that of the sub-pixel being calculated and unit vertical location and a second pixel or sub-pixel located at a horizontal location corresponding to that of the sub-pixel being calculated and $\frac{1}{2}^{N-1}$ unit vertical location.

Values for sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations may be interpolated by taking the average of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

Values for sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations may be interpolated by taking the average of values of a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

Values for half of the sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations may be interpolated by taking the average of a first pair of values of a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location and values for the other half of the sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations are interpolated by taking the average of a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

Values for sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations are alternately interpolated for one such sub-pixel by taking the average of a first pair of values of a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location and values and for a neighbouring such sub-pixel by taking the average of a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

The sub-pixels at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical locations may be alternately interpolated in a horizontal direction.

The sub-pixels at $1/2^N$ unit horizontal and $1/2^N$ unit vertical locations may be alternately interpolated in a horizontal direction.

When values for some sub-pixels at $1/2^N$ unit horizontal and $1/2^N$ unit vertical locations are required, such values may be interpolated by taking the average of a plurality of nearest neighbouring pixels.

At least one of step a) and step b) interpolating sub-pixel values directly using weighted sums may involve the calculation of an intermediate value for the sub-pixel values having a dynamic range greater than the specified dynamic range.

The intermediate value for a sub-pixel having $1/2^{N-1}$ sub-pixel resolution may be used the calculation of a sub-pixel value having $1/2^N$ sub-pixel resolution.

According to a second aspect of the invention, there is provided a method of interpolation in video coding in which an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, is interpolated to generate values for sub-pixels at fractional horizontal and vertical locations, the method comprising:

a) when values for sub-pixels at half unit horizontal and unit vertical locations, and unit horizontal and half unit vertical locations are required, interpolating such values directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) when values for sub-pixels at half unit horizontal and half unit vertical locations are required, interpolating such values directly using a weighted sum of values for sub-pixels residing at half unit horizontal and unit vertical locations calculated according to step (a); and

c) when values for sub-pixels at quarter unit horizontal and quarter unit vertical locations are required, interpolating such values by taking the average of at least one pair of a first pair of values of a sub-pixel located at a half unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and half unit vertical location and a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a half unit horizontal and half unit vertical location.

According to a third aspect of the invention, there is provided a method of interpolation in video coding in which an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, is interpolated to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $1/2^x$ where x is a positive integer having a maximum value N, the method comprising:

a) when values for sub-pixels at $1/2^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $1/2^{N-1}$ unit vertical locations are required, interpolating such values directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) when a value for a sub-pixel at a sub-pixel horizontal and sub-pixel vertical location is required, interpolating such a value directly using a choice of a first weighted sum of values for sub-pixels located at a vertical location corresponding to that of the sub-pixel being calculated and a second weighted sum of values for sub-pixels located at a horizontal location corresponding to that of the sub-pixel being calculated.

The sub-pixels used in the first weighted sum may be sub-pixels residing at $1/2^{N-1}$ unit horizontal and unit vertical locations and the first weighted sum may be used to interpolate a value for a sub-pixel at $1/2^{N-1}$ unit horizontal and $1/2^N$ unit vertical location.

The sub-pixels used in the second weighted sum may be sub-pixels residing at unit horizontal and $1/2^{N-1}$ unit vertical locations and the second weighted sum may be used to interpolate a value for a sub-pixel at $1/2^N$ unit horizontal and $1/2^{N-1}$ unit vertical location.

When values for sub-pixels at $1/2^N$ unit horizontal and $1/2^N$ unit vertical locations are required, they may be interpolated by taking the average of at least one pair of a first pair of values of a sub-pixel located at a $1/2^{N-1}$ unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and $1/2^{N-1}$ unit vertical location and a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a $1/2^{N-1}$ unit horizontal and $1/2^{N-1}$ unit vertical location.

In the foregoing, N may be equal an integer selected from a list consisting of the values 2, 3, and 4.

Sub-pixels at quarter unit horizontal location are to be interpreted as being sub-pixels having as their left-hand nearest neighbour a pixel at unit horizontal location and as their right-hand nearest neighbour a sub-pixel at half unit horizontal location as well as sub-pixels having as their left-hand nearest neighbour a sub-pixel at half unit horizontal location and as their right-hand nearest neighbour a pixel at unit horizontal location. Correspondingly, sub-pixels at quarter unit vertical location are to be interpreted as being sub-pixels having as their upper nearest neighbour a pixel at unit vertical location and as their lower nearest neighbour a sub-pixel at half unit vertical location as well as sub-pixels having as their upper nearest neighbour a sub-pixel at half unit vertical location and as their lower nearest neighbour a pixel at unit vertical location.

The term dynamic range, refers to the range of values which the sub-pixel values and the weighted sums can take.

Preferably changing the dynamic range, whether by extending it or reducing it, means changing the number of bits which are used to represent the dynamic range.

In an embodiment of the invention, the method is applied to an image that is sub-divided into a number of image blocks. Preferably each image block comprises four corners, each corner being defined by a pixel located at a unit horizontal and unit vertical location. Preferably the method is applied to each image block as the block becomes available for sub-pixel value interpolation. Alternatively, sub-pixel value interpolation according to the method of the invention is performed once all image blocks of an image have become available for sub-pixel value interpolation.

Preferably the method is used in video encoding. Preferably the method is used in video decoding.

In one embodiment of the invention, when used in encoding, the method is carried out as before-hand interpolation, in which values for all sub-pixels at half unit locations and values for all sub-pixels at quarter unit locations are calculated and stored before being subsequently used in the determination of a prediction frame during motion predictive coding. In alternative embodiments, the method is carried out as a combination of before-hand and on-demand interpolation. In this case, a certain proportion or category of sub-pixel values is calculated and stored before being used in the determination of a prediction frame and certain other sub-pixel values are calculated only when required during motion predictive coding.

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Preferably, when the method is used in decoding, sub-pixels are only interpolated when their need is indicated by a motion vector.

According to a fourth aspect of the invention, there is provided a video coder for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the video coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $\frac{1}{2}^x$, where x is a positive integer having a maximum value N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using a choice of a first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and a second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations, the first and second weighted sums of values being calculated according to step (a); and

c) interpolate a value for a sub-pixel situated at a $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical location by taking a weighted average of the value of a first sub-pixel or pixel situated at a $\frac{1}{2}^{N-m}$ unit horizontal and $\frac{1}{2}^{N-n}$ unit vertical location and the value of a second sub-pixel or pixel located at a $\frac{1}{2}^{N-p}$ unit horizontal and $\frac{1}{2}^{N-q}$ unit vertical location, variables m, n, p and q taking integer values in the range 1 to N such that the first and second sub-pixels or pixels are located diagonally with respect to the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location.

The video coder may comprise a video encoder. It may comprise a video decoder. There may be a codec comprising both the video encoder and the video decoder.

According to a fifth aspect of the invention, there is provided a communications terminal comprising a video coder for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the video coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $\frac{1}{2}^x$, where x is a positive integer having a maximum value N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using a choice of a first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and a second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations, the first and second weighted sums of values being calculated according to step (a); and

c) interpolate a value for a sub-pixel situated at a $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical location by taking a weighted average of the value of a first sub-pixel or pixel situated at a $\frac{1}{2}^{N-m}$ unit horizontal and $\frac{1}{2}^{N-n}$ unit vertical location and the value of a second sub-pixel or pixel located at a $\frac{1}{2}^{N-p}$ unit horizontal and $\frac{1}{2}^{N-q}$ unit vertical location, variables m, n, p and q taking integer values in the range 1 to N such that the first and second sub-pixels or pixels are located diagonally with respect to the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location.

The communications terminal may comprise a video encoder. It may comprise a video decoder. Preferably, it comprises a video codec comprising a video encoder and a video decoder.

Preferably the communications terminal comprising a user interface, a processor and at least one of a transmitting block and a receiving block, and a video coder according to at least one of the third and fourth aspects of the invention. Preferably the processor controls the operation of the transmitting block and/or the receiving block and the video coder.

According to a sixth aspect of the invention, there is provided a telecommunications system comprising a communications terminal and a network, the telecommunications network and the communications terminal being connected by a communications link over which coded video can be transmitted, the communications terminal comprising a video coder for coding for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the video coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $\frac{1}{2}^x$, where x is a positive integer having a maximum value N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using a choice of a first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and a second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations, the first and second weighted sums of values being calculated according to step (a); and

c) interpolate a value for a sub-pixel situated at a $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ unit vertical location by taking a weighted average of the value of a first sub-pixel or pixel situated at a $\frac{1}{2}^{N-m}$ unit horizontal and $\frac{1}{2}^{N-n}$ unit vertical location and the value of a second sub-pixel or pixel located at a $\frac{1}{2}^{N-p}$ unit horizontal and $\frac{1}{2}^{N-q}$ unit vertical location, variables m, n, p and q taking integer values in the range 1 to N such that the first and second sub-pixels or pixels are located diagonally with respect to the sub-pixel at $\frac{1}{2}^N$ unit horizontal and $\frac{1}{2}^N$ vertical location.

Preferably the telecommunications system is a mobile telecommunications system comprising a mobile communications terminal and a wireless network, the connection between the mobile communications terminal and the wireless network being formed by a radio link. Preferably the network enables the communications terminal to communicate with other communications terminals connected to the network over communications links between the other communications terminals and the network.

According to a seventh aspect of the invention, there is provided a telecommunications system comprising a communications terminal and a network, the telecommunications network and the communications terminal being connected

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by a communications link over which coded video can be transmitted, the network comprising a video coder for coding for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the video coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the fractional horizontal and vertical locations being defined according to $\frac{1}{2}^{x}$, where x is a positive integer having a maximum value N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using a choice of a first weighted sum of values for sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and a second weighted sum of values for sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations, the first and second weighted sums of values being calculated according to step (a); and

c) interpolate a value for a sub-pixel situated at a $\frac{1}{2}^{N}$ unit horizontal and $\frac{1}{2}^{N}$ unit vertical location by taking a weighted average of the value of a first sub-pixel or pixel situated at a $\frac{1}{2}^{N-m}$ unit horizontal and $\frac{1}{2}^{N-n}$ unit vertical location and the value of a second sub-pixel or pixel located at a $\frac{1}{2}^{N-p}$ unit horizontal and $\frac{1}{2}^{N-q}$ unit vertical location, variables m, n, p and q taking integer values in the range 1 to N such that the first and second sub-pixels or pixels are located diagonally with respect to the sub-pixel at $\frac{1}{2}^{N}$ unit horizontal and $\frac{1}{2}^{N}$ vertical location.

According to an eighth aspect of the invention there is provided a video coder for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the resolution of the sub-pixels being determined by a positive integer N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate a value for a sub-pixel at a sub-pixel horizontal and sub-pixel vertical location is required directly using a choice of a first weighted sum of values for sub-pixels located at a vertical location corresponding to that of the sub-pixel being calculated and a second weighted sum of values for sub-pixels located at a horizontal location corresponding to that of the sub-pixel being calculated.

The interpolator may be further adapted to form the first weighted sum using the values of sub-pixels residing at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations and to use the first weighted sum to interpolate a value for a sub-pixel at $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N}$ unit vertical location.

The interpolator may be further adapted to form the second weighted sum using the values of sub-pixels residing at unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations and to use the second weighted sum to interpolate a value for a sub-pixel at $\frac{1}{2}^{N}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

The interpolator may be further adapted to interpolate values for sub-pixels at $\frac{1}{2}^{N}$ unit horizontal and $\frac{1}{2}^{N}$ unit vertical locations by taking the average of at least one pair of a first pair of values of a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical location, and a sub-pixel located at a unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location and a second pair of values of a pixel located at a unit horizontal and unit vertical location, and a sub-pixel located at a $\frac{1}{2}^{N-1}$ unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical location.

According to a ninth aspect of the invention there is provided a communications terminal comprising a video coder for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the resolution of the sub-pixels being determined by a positive integer N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate a value for a sub-pixel at a sub-pixel horizontal and sub-pixel vertical location is required directly using a choice of a first weighted sum of values for sub-pixels located at a vertical location corresponding to that of the sub-pixel being calculated and a second weighted sum of values for sub-pixels located at a horizontal location corresponding to that of the sub-pixel being calculated.

According to a tenth aspect of the invention there is provided a telecommunications system comprising a communications terminal and a network, the telecommunications network and the communications terminal being connected by a communications link over which coded video can be transmitted, the communications terminal comprising a video coder for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the coder comprising an interpolator adapted to generate values for sub-pixels at fractional horizontal and vertical locations, the resolution of the sub-pixels being determined by a positive integer N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate a value for a sub-pixel at a sub-pixel horizontal and sub-pixel vertical location is required directly using a choice of a first weighted sum of values for sub-pixels located at a vertical location corresponding to that of the sub-pixel being calculated and a second weighted sum of values for sub-pixels located at a horizontal location corresponding to that of the sub-pixel being calculated.

According to an eleventh aspect of the invention there is provided a telecommunications system comprising a communications terminal and a network, the telecommunications network and the communications terminal being connected by a communications link over which coded video can be transmitted, the network comprising a video coder for coding for coding an image comprising pixels arranged in rows and columns and represented by values having a specified dynamic range, the pixels in the rows residing at unit horizontal locations and the pixels in the columns residing at unit vertical locations, the coder comprising an interpolator adapted to generate values for sub-pixels at fractional hori-

zontal and vertical locations, the resolution of the sub-pixels being determined by a positive integer N, the interpolator being adapted to:

a) interpolate values for sub-pixels at $\frac{1}{2}^{N-1}$ unit horizontal and unit vertical locations, and unit horizontal and $\frac{1}{2}^{N-1}$ unit vertical locations directly using weighted sums of pixels residing at unit horizontal and unit vertical locations;

b) interpolate a value for a sub-pixel at a sub-pixel horizontal and sub-pixel vertical location is required directly using a choice of a first weighted sum of values for sub-pixels located at a vertical location corresponding to that of the sub-pixel being calculated and a second weighted sum of values for sub-pixels located at a horizontal location corresponding to that of the sub-pixel being calculated.

According to the twelfth aspect of the invention, the disclosed embodiments are directed to a method for sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being arranged in rows and columns, the pixel and sub-pixel locations being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the method comprising:

(a) interpolating a sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, according to a predetermined choice of a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates 1/2, 1/2, and a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of both K and L, including zero, situated within a quadrant of the rectangular bounded region defined by corner pixels having co-ordinates 1/2, 1/2 and the nearest neighbouring pixel;

(b) interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of both K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

(c) interpolating sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent bounded rectangular regions.

According to the thirteenth aspect of the invention, the disclosed embodiments are directed to a method for quarter resolution sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being arranged in rows and columns, the pixel and sub-pixel locations being representable mathematically within the rectangular bounded region using the co-ordinate notation K/4, L/4, K and L being positive integers having respective values between zero and 4, the method comprising:

(a) interpolating a sub-pixel value for a sub-pixel having co-ordinates with both K and L equal to 1 or 3, according to a predetermined choice of a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates 2/4, 2/4, and a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with both K and L equal to zero, 2 or 4, situated within a quadrant of the rectangular bounded region defined by corner pixels having co-ordinates 2/4, 2/4 and the nearest neighbouring pixel;

(b) interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to 2 and L equal zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, used in the interpolation of the sub-pixels having co-ordinates with both K and L equal to 1 or 3, using weighted sums of the values of pixels located in rows and columns respectively; and

(c) interpolating a sub-pixel value for the sub-pixel having co-ordinates with both K and L equal to 2, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with both K and L equal to 1 or 3, using a predetermined choice of either a weighted sum of the values of the sub-pixel having co-ordinates with K equal to 2 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the value of the sub-pixel having co-ordinates with K equal to zero and L equal to 2 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

According to the fourteenth aspect of the invention, the disclosed embodiments are direct to a method for eighth resolution sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being arranged in rows and columns, the pixel and sub-pixel locations being representable mathematically with the rectangular bounded region using the co-ordinate notation K/8, L/8, K and L being positive integers having respective values between zero and 8, the method comprising:

(a) interpolating a sub-pixel value for a sub-pixel having co-ordinates with both K and L equal to 1, 3, 5 or 7, according to a predetermined choice of a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates 4/8, 4/8, and a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with both K and L equal to zero, 2, 4, 6 or 8, situated within a quadrant of the rectangular bounded region defined by corner pixels having co-ordinates 4/8, 4/8 and the nearest neighbouring pixel;

(b) interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6, used in the interpolation of the sub-pixels having co-ordinates with both K and L equal to 1, 3, 5 or 7, using weighted sums of the values of pixels located in rows and columns respectively; and

(c) interpolating sub-pixel values for sub-pixels having co-ordinates with both K and L equal to 2, 4 or 6, used in the interpolation of sub-pixel values for the sub-pixels

having co-ordinates with both K and L equal to 1, 3, 5 or 7, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

According to the fifteenth aspect of the invention, the disclosed embodiments are directed to an apparatus for sub-pixel value interpolation, the apparatus being operable to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being arranged in rows and columns, the pixel and sub-pixel locations being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the apparatus comprising:

(a) circuitry operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, according to a predetermined choice of a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates 1/2, 1/2, and a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of both K and L, including zero, situated within a quadrant of the rectangular bounded region defined by corner pixels having co-ordinates 1/2, 1/2 and the nearest neighbouring pixel;

(b) circuitry operable to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of both K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

(c) circuitry operable to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent bounded rectangular regions.

In one embodiment the method includes comprising using a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, wherein when the chosen weighted average is that involving the value of a nearest neighbouring pixel and the value of the sub-pixel situated at co-ordinates 1/2, 1/2, selecting the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the nearest-neighbouring pixel and the sub-pixel situated at co-ordinates 1/2, 1/2 to the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the method includes comprising using a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, wherein when the chosen weighted average is that involving the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of both K and L, selecting the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the sub-pixels having co-ordinates with even values of both K and L to the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the method includes comprising using first and second weights with equal values when the nearest-neighbouring pixel and sub-pixel situated at co-ordinates 1/2, 1/2 are equidistant from the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the method includes comprising using first and second weights with equal values when the sub-pixels having co-ordinates with even values of both K and L are equidistant from the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the method includes interpolating sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an even value and L equal to an odd value is also required.

In one embodiment the method includes comprising interpolating sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an odd value and L equal to an even value is also required.

In one embodiment the method includes comprising interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to an odd value O and L equal to an even value E, not including zero or 2^N, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to the even value O−1 and L equal to E and a second sub-pixel having co-ordinates with K equal to the even value O+1 and L equal to E.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2 and L equal to zero.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to zero.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2 and L equal to 2^N.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to 2^N.

In one embodiment the method includes comprising interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to an even value E, not including zero or 2^N, and L equal to an odd value O, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to E and L equal to the even value O−1 and a second sub-pixel having co-ordinates with K equal to E and L equal to the even value O+1.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 0 and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-2.

In one embodiment the method includes comprising interpolating a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-2.

In one embodiment the method includes comprising interpolating a sub-pixel value for the sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N-1, by taking a weighted average of the values of the four corner pixels that define the rectangular bounded region.

In one embodiment the method includes comprising selecting a value for N from a list consisting of the values 2, 3, and 4.

In one embodiment the apparatus is operable to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, wherein when the chosen weighted average is that involving the value of a nearest neighbouring pixel and the value of the sub-pixel situated at co-ordinates 1/2, 1/2, the apparatus is operable to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the nearest-neighbouring pixel and the sub-pixel situated at co-ordinates 1/2, 1/2 to the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the apparatus is operable to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, wherein when the chosen weighted average is that involving the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of both K and L, the apparatus is operable to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the sub-pixels having co-ordinates with even values of both K and L to the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the apparatus is operable to use first and second weights with equal values when the nearest-neighbouring pixel and sub-pixel situated at co-ordinates 1/2, 1/2 are equidistant from the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the apparatus is operable to use first and second weights with equal values when the sub-pixels having co-ordinates with even values of both K and L are equidistant from the sub-pixel having co-ordinates with odd values of both K and L whose value is being interpolated.

In one embodiment the apparatus is operable to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an even value and L equal to an odd value is also required.

In one embodiment the apparatus is operable to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of both K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of both K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an odd value and L equal to an even value is also required.

In one embodiment the apparatus is operable to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an odd value O and L equal to an even value E, not including zero or 2^N, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to the even value O−1 and L equal to E and a second sub-pixel having co-ordinates with K equal to the even value O+1 and L equal to E.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2 and L equal to zero.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to zero.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to 2^N, by taking an average of the value

of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2 and L equal to 2^N.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to 2^N

In one embodiment the apparatus is operable to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value E, not including zero or 2^N, and L equal to an odd value O, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to E and L equal to the even value O−1 and a second sub-pixel having co-ordinates with K equal to E and L equal to the even value O+1.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 0 and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-2.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-2.

In one embodiment the apparatus is operable to interpolate a sub-pixel value for the sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N-1, by taking a weighted average of the values of the four corner pixels that define the rectangular bounded region.

In one embodiment the apparatus includes N is set equal to 2.

In one embodiment the apparatus includes N is set equal to 3.

In one embodiment the apparatus includes a video encoder comprising an apparatus for sub-pixel value interpolation.

In one embodiment the apparatus includes a still image encoder comprising an apparatus for sub-pixel value interpolation.

In one embodiment the apparatus includes a video decoder comprising an apparatus for sub-pixel value interpolation.

In one embodiment the apparatus includes a still image decoder comprising an apparatus for sub-pixel value interpolation.

In one embodiment the apparatus includes a codec comprising a video encoder and a video decoder.

In one embodiment the apparatus includes a codec comprising a still image encoder and a still image decoder.

In one embodiment the apparatus includes a communications terminal comprising a video encoder.

In one embodiment the apparatus includes a communications terminal comprising a still image encoder.

In one embodiment the apparatus includes a communications terminal comprising a video decoder.

In one embodiment the apparatus includes a communications terminal comprising a still image decoder.

BRIEF DESCRIPTION OF THE FIGURES

An embodiment of the invention will now be described by way of example only with reference to the accompanying drawings in which:

FIG. **1** shows a video encoder according to the prior art;

FIG. **2** shows a video decoder according to the prior art;

FIG. **3** shows the types of frames used in video encoding;

FIGS. **4***a*, **4***b*, and **4***c* show steps in block-matching;

FIG. **5** illustrates the process of motion estimation to sub-pixel resolution;

FIG. **6** shows a terminal device comprising video encoding and decoding equipment in which the method of the invention may be implemented;

FIG. **7** shows a video encoder according an embodiment of the present invention;

FIG. **8** shows a video decoder according to an embodiment of the present invention;

FIGS. **9** and **10** have not been used and any such figures should be disregarded;

FIG. **11** shows a schematic diagram of a mobile telecommunications network according to an embodiment of the present invention;

FIG. **12***a* shows a notation for describing pixel and sub-pixel locations specific to TML5;

FIG. **12***b* shows interpolation of a half resolution sub-pixels;

FIG. **12***c* shows interpolation of a half resolution sub-pixels;

FIG. **13***a* shows a notation for describing pixel and sub-pixel locations specific to TML6;

FIG. **13***b* shows interpolation of a half resolution sub-pixels;

FIG. **13***c* shows interpolation of a half resolution sub-pixels;

FIG. **14***a* shows a notation for describing pixel and sub-pixel locations specific to the invention;

FIG. **14***b* shows interpolation of a half resolution sub-pixels according to the invention;

FIG. **14***c* shows interpolation of a half resolution sub-pixels according to the invention;

FIG. **15** shows possible choices of diagonal interpolation for sub-pixels;

FIG. **16** shows the half resolution sub-pixel values required to calculate other half resolution sub-pixel values;

FIG. **17***a* shows the half resolution sub-pixel values that must be calculated in order to interpolate values for quarter resolution sub-pixels in an image block using the interpolation method of TML5;

FIG. **17***b* shows the half resolution sub-pixel values that must be calculated in order to interpolate values for quarter resolution sub-pixels in an image block using the interpolation method according to the invention;

FIG. **18***a* shows the numbers of half resolution sub-pixels that must be calculated in order to obtain values for quarter resolution sub-pixels within an image block using the sub-pixel value interpolation method according to TML5;

FIG. **18***b* shows the numbers of half resolution sub-pixels that must be calculated in order to obtain values for quarter resolution sub-pixels within an image block using the sub-pixel value interpolation method according to the invention;

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FIG. **19** shows a numbering scheme for each of the 15 sub-pixel positions;

FIG. **20** shows nomenclature used to describe pixels, half resolution sub-pixels, quarter resolution sub-pixels and eighth resolution sub-pixels

FIG. **21***a* shows the diagonal direction to be used in the interpolation of each eighth resolution sub-pixel in an embodiment of the invention;

FIG. **21***b* shows the diagonal direction to be used in the interpolation of each eighth resolution sub-pixel in another embodiment of the invention; and

FIG. **22** shows nomenclature used to describe eighth resolution sub-pixels within an image.

DETAILED DESCRIPTION

FIGS. **1** to **5**, **12***a*, **12***b*, **12***c*, **13***a*, **13***b*, and **13***c* have been described in the foregoing.

FIG. **6** presents a terminal device comprising video encoding and decoding equipment which may be adapted to operate in accordance with the present invention. More precisely, the figure illustrates a multimedia terminal **60** implemented according to ITU-T recommendation H.324. The terminal can be regarded as a multimedia transceiver device. It includes elements that capture, encode and multiplex multimedia data streams for transmission via a communications network, as well as elements that receive, de-multiplex, decode and display received multimedia content. ITU-T recommendation H.324 defines the overall operation of the terminal and refers to other recommendations that govern the operation of its various constituent parts. This kind of multimedia terminal can be used in real-time applications such as conversational videotelephony, or non real-time applications such as the retrieval/streaming of video clips, for example from a multimedia content server in the Internet.

In the context of the present invention, it should be appreciated that the H.324 terminal shown in FIG. **6** is only one of a number of alternative multimedia terminal implementations suited to application of the inventive method. It should also be noted that a number of alternatives exist relating to the location and implementation of the terminal equipment. As illustrated in FIG. **6**, the multimedia terminal may be located in communications equipment connected to a fixed line telephone network such as an analogue PSTN (Public Switched Telephone Network). In this case the multimedia terminal is equipped with a modem **71**, compliant with ITU-T recommendations V.8, V.34 and optionally V.8bis. Alternatively, the multimedia terminal may be connected to an external modem. The modem enables conversion of the multiplexed digital data and control signals produced by the multimedia terminal into an analogue form suitable for transmission over the PSTN. It further enables the multimedia terminal to receive data and control signals in analogue form from the PSTN and to convert them into a digital data stream that can be demultiplexed and processed in an appropriate manner by the terminal.

An H.324 multimedia terminal may also be implemented in such a way that it can be connected directly to a digital fixed line network, such as an ISDN (Integrated Services Digital Network). In this case the modem **71** is replaced with an ISDN user-network interface. In FIG. **6**, this ISDN user-network interface is represented by alternative block **72**.

H.324 multimedia terminals may also be adapted for use in mobile communication applications. If used with a wireless communication link, the modem **71** can be replaced with any appropriate wireless interface, as represented by alternative block **73** in FIG. **6**. For example, an H.324/M multimedia terminal can include a radio transceiver enabling connection to the current 2^{nd} generation GSM mobile telephone network, or the proposed 3^{rd} generation UMTS (Universal Mobile Telephone System).

It should be noted that in multimedia terminals designed for two-way communication, that is for transmission and reception of video data, it is advantageous to provide both a video encoder and video decoder implemented according to the present invention. Such an encoder and decoder pair is often implemented as a single combined functional unit, referred to as a 'codec'.

Because a video encoder according to the invention performs motion compensated video encoding to sub-pixel resolution using a specific interpolation scheme and a particular combination of before-hand and on-demand sub-pixel value interpolation, it is generally necessary for a video decoder of a receiving terminal to be implemented in a manner compatible with the encoder of the transmitting terminal which formed the compressed video data stream. Failure to ensure this compatibility may have an adverse effect on the quality of the motion compensation and the accuracy of reconstructed video frames.

A typical H.324 multimedia terminal will now be described in further detail with reference to FIG. **6**.

The multimedia terminal **60** includes a variety of elements referred to as 'terminal equipment'. This includes video, audio and telematic devices, denoted generically by reference numbers **61**, **62** and **63**, respectively. The video equipment **61** may include, for example, a video camera for capturing video images, a monitor for displaying received video content and optional video processing equipment. The audio equipment **62** typically includes a microphone, for example for capturing spoken messages, and a loudspeaker for reproducing received audio content. The audio equipment may also include additional audio processing units. The telematic equipment **63**, may include a data terminal, keyboard, electronic whiteboard or a still image transceiver, such as a fax unit.

The video equipment **61** is coupled to a video codec **65**. The video codec **65** comprises a video encoder and a corresponding video decoder both implemented according to the invention. Such an encoder and a decoder will be described in the following. The video codec **65** is responsible for encoding captured video data in an appropriate form for further transmission over a communications link and decoding compressed video content received from the communications network. In the example illustrated in FIG. **6**, the video codec is implemented according to ITU-T recommendation H.263, with appropriate modifications to implement the sub-pixel value interpolation method according to the invention in both the encoder and the decoder of the video codec.

Similarly, the terminal's audio equipment is coupled to an audio codec, denoted in FIG. **6** by reference number **66**. Like the video codec, the audio codec comprises an encoder/decoder pair. It converts audio data captured by the terminal's audio equipment into a form suitable for transmission over the communications link and transforms encoded audio data received from the network back into a form suitable for reproduction, for example on the terminal's loudspeaker. The output of the audio codec is passed to a delay block **67**. This compensates for the delays introduced by the video coding process and thus ensures synchronisation of audio and video content.

The system control block **64** of the multimedia terminal controls end-to-network signalling using an appropriate control protocol (signalling block **68**) to establish a common mode of operation between a transmitting and a receiving terminal. The signalling block **68** exchanges information

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about the encoding and decoding capabilities of the transmitting and receiving terminals and can be used to enable the various coding modes of the video encoder. The system control block **64** also controls the use of data encryption. Information regarding the type of encryption to be used in data transmission is passed from encryption block **69** to the multiplexer/de-multiplexer (MUX/DMUX unit) **70**.

During data transmission from the multimedia terminal, the MUX/DMUX unit **70** combines encoded and synchronised video and audio streams with data input from the telematic equipment **63** and possible control data, to form a single bit-stream. Information concerning the type of data encryption (if any) to be applied to the bit-stream, provided by encryption block **69**, is used to select an encryption mode. Correspondingly, when a multiplexed and possibly encrypted multimedia bit-stream is being received, MUX/DMUX unit **70** is responsible for decrypting the bit-stream, dividing it into its constituent multimedia components and passing those components to the appropriate codec(s) and/or terminal equipment for decoding and reproduction.

It should be noted that the functional elements of the multimedia terminal, video encoder, decoder and video codec according to the invention can be implemented as software or dedicated hardware, or a combination of the two. The video encoding and decoding methods according to the invention are particularly suited for implementation in the form of a computer program comprising machine-readable instructions for performing the functional steps of the invention. As such, the encoder and decoder according to the invention may be implemented as software code stored on a storage medium and executed in a computer, such as a personal desktop computer, in order to provide that computer with video encoding and/or decoding functionality.

If the multimedia terminal **60** is a mobile terminal, that is if it is equipped with a radio transceiver **73**, it will be understood by those skilled in the art that it may also comprise additional elements. In one embodiment it comprises a user interface having a display and a keyboard, which enables operation of the multimedia terminal **60** by a user, together with necessary functional blocks including a central processing unit, such as a microprocessor, which controls the blocks responsible for different functions of the multimedia terminal, a random access memory RAM, a read only memory ROM, and a digital camera. The microprocessor's operating instructions, that is program code corresponding to the basic functions of the multimedia terminal **60**, is stored in the read-only memory ROM and can be executed as required by the microprocessor, for example under control of the user. In accordance with the program code, the microprocessor uses the radio transceiver **73** to form a connection with a mobile communication network, enabling the multimedia terminal **60** to transmit information to and receive information from the mobile communication network over a radio path.

The microprocessor monitors the state of the user interface and controls the digital camera. In response to a user command, the microprocessor instructs the camera to record digital images into the RAM. Once an image is captured, or alternatively during the capturing process, the microprocessor segments the image into image segments (for example macroblocks) and uses the encoder to perform motion compensated encoding for the segments in order to generate a compressed image sequence as explained in the foregoing description. A user may command the multimedia terminal **60** to display the captured images on its display or to send the compressed image sequence using the radio transceiver **73** to another multimedia terminal, a video telephone connected to a fixed line network (PSTN) or some other telecommunications device. In a preferred embodiment, transmission of image data is started as soon as the first segment is encoded so that the recipient can start a corresponding decoding process with a minimum delay.

FIG. **11** is a schematic diagram of a mobile telecommunications network according to an embodiment of the invention. Multimedia terminals MS are in communication with base stations BTS by means of a radio link. The base stations BTS are further connected, through a so-called Abis interface, to a base station controller BSC, which controls and manages several base stations.

The entity formed by a number of base stations BTS (typically, by a few tens of base stations) and a single base station controller BSC, controlling the base stations, is called a base station subsystem BSS. Particularly, the base station controller BSC manages radio communication channels and handovers. The base station controller BSC is also connected, through a so-called A interface, to a mobile services switching centre MSC, which co-ordinates the formation of connections to and from mobile stations. A further connection is made, through the mobile service switching centre MSC, to outside the mobile communications network. Outside the mobile communications network there may further reside other network(s) connected to the mobile communications network by gateway(s) GTW, for example the Internet or a Public Switched Telephone Network (PSTN). In such an external network, or within the telecommunications network, there may be located video decoding or encoding stations, such as computers PC. In an embodiment of the invention, the mobile telecommunications network comprises a video server VSRVR to provide video data to a MS subscribing to such a service. The video data is compressed using the motion compensated video compression method as described in the foregoing. The video server may function as a gateway to an online video source or it may comprise previously recorded video clips. Typical videotelephony applications may involve, for example, two mobile stations or one mobile station MS and a videotelephone connected to the PSTN, a PC connected to the Internet or a H.261 compatible terminal connected either to the Internet or to the PSTN.

FIG. **7** shows a video encoder **700** according to an embodiment the invention. FIG. **8** shows a video decoder **800** according to an embodiment the invention.

The encoder **700** comprises an input **701** for receiving a video signal from a camera or other video source (not shown). It further comprises a DCT transformer **705**, a quantiser **706**, an inverse quantiser **709**, an inverse DCT transformer **710**, combiners **712** and **716**, a before-hand sub-pixel interpolation block **730**, a frame store **740** and an on-demand sub-pixel interpolation block **750**, implemented in combination with motion estimation block **760**. The encoder also comprises a motion field coding block **770** and a motion compensated prediction block **780**. Switches **702** and **714** are operated co-operatively by a control manager **720** to switch the encoder between an INTRA-mode of video encoding and an INTER-mode of video encoding. The encoder **700** also comprises a multiplexer unit (MUX/DMUX) **790** to form a single bit-stream from the various types of information produced by the encoder **700** for further transmission to a remote receiving terminal, or for example for storage on a mass storage medium such as a computer hard drive (not shown).

It should be noted that the presence and implementations of before-hand sub-pixel interpolation block **730** and on-demand sub-pixel value interpolation block **750** in the encoder architecture depend on the way in which the sub-pixel interpolation method according to the invention is applied. In embodiments of the invention in which before-hand sub-pixel

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value interpolation is not performed, encoder **700** does not comprise before-hand sub-pixel value interpolation block **730**. In other embodiments of the invention, only before-hand sub-pixel interpolation is performed and thus the encoder does not include on-demand sub-pixel value interpolation block **750**. In embodiments in which both before-hand and on-demand sub-pixel value interpolation are performed, both blocks **730** and **750** are present in the encoder **700**.

Operation of the encoder **700** according to the invention will now be described in detail. In the description, it will be assumed that each frame of uncompressed video, received from the video source at the input **701**, is received and processed on a macroblock-by-macroblock basis, preferably in raster-scan order. It will further be assumed that when the encoding of a new video sequence starts, the first frame of the sequence is encoded in INTRA-mode. Subsequently, the encoder is programmed to code each frame in INTER-format, unless one of the following conditions is met: 1) it is judged that the current frame being coded is so dissimilar from the reference frame used in its prediction that excessive prediction error information is produced; 2) a predefined INTRA frame repetition interval has expired; or 3) feedback is received from a receiving terminal indicating a request for a frame to be coded in INTRA format.

The occurrence of condition 1) is detected by monitoring the output of the combiner **716**. The combiner **716** forms a difference between the current macroblock of the frame being coded and its prediction, produced in the motion compensated prediction block **780**. If a measure of this difference (for example a sum of absolute differences of pixel values) exceeds a predetermined threshold, the combiner **716** informs the control manager **720** via a control line **717** and the control manager **720** operates the switches **702** and **714** so as to switch the encoder **700** into INTRA coding mode. Occurrence of condition 2) is monitored by means of a timer or frame counter implemented in the control manager **720**, in such a way that if the timer expires, or the frame counter reaches a predetermined number of frames, the control manager **720** operates the switches **702** and **714** to switch the encoder into INTRA coding mode. Condition 3) is triggered if the control manager **720** receives a feedback signal from, for example, a receiving terminal, via control line **718** indicating that an INTRA frame refresh is required by the receiving terminal. Such a condition might arise, for example, if a previously transmitted frame were badly corrupted by interference during its transmission, rendering it impossible to decode at the receiver. In this situation, the receiver would issue a request for the next frame to be encoded in INTRA format, thus re-initializing the coding sequence.

It will further be assumed that the encoder and decoder are implemented in such a way as to allow the determination of motion vectors with a spatial resolution of up to quarter-pixel resolution. As will be seen in the following, finer levels of resolution are also possible.

Operation of the encoder **700** in INTRA coding mode will now be described. In INTRA-mode, the control manager **720** operates the switch **702** to accept video input from input line **719**. The video signal input is received macroblock by macroblock from input **701** via the input line **719** and each macroblock of original image pixels is transformed into DCT coefficients by the DCT transformer **705**. The DCT coefficients are then passed to the quantiser **706**, where they are quantised using a quantisation parameter QP. Selection of the quantisation parameter QP is controlled by the control manager **720** via control line **722**. Each DCT transformed and quantised macroblock that makes up the INTRA coded image information **723** of the frame is passed from the quantiser **706** to the MUX/DMUX **790**. The MUX/DMUX **790** combines the INTRA coded image information with possible control information (for example header data, quantisation parameter information, error correction data etc.) to form a single bit-stream of coded image information **725**. Variable length coding (VLC) is used to reduce redundancy of the compressed video bit-stream, as is known to those skilled in the art.

A locally decoded picture is formed in the encoder **700** by passing the data output by the quantiser **706** through inverse quantiser **709** and applying an inverse DCT transform **710** to the inverse-quantised data. The resulting data is then input to the combiner **712**. In INTRA mode, switch **714** is set so that the input to the combiner **712** via the switch **714** is set to zero. In this way, the operation performed by the combiner **712** is equivalent to passing the decoded image data formed by the inverse quantiser **709** and the inverse DCT transform **710** unaltered.

In embodiments of the invention in which before-hand sub-pixel value interpolation is performed, the output from combiner **712** is applied to before-hand sub-pixel interpolation block **730**. The input to the before-hand sub-pixel value interpolation block **730** takes the form of decoded image blocks. In the before-hand sub-pixel value interpolation block **730**, each decoded macroblock is subjected to sub-pixel interpolation in such a way that a predetermined sub-set of sub-pixel resolution sub-pixel values is calculated according to the interpolation method of the invention and is stored together with the decoded pixel values in frame store **740**.

In embodiments in which before-hand sub-pixel interpolation is not performed, before-hand sub-pixel interpolation block is not present in the encoder architecture and the output from combiner **712**, comprising decoded image blocks, is applied directly to frame store **740**.

As subsequent macroblocks of the current frame are received and undergo the previously described coding and decoding steps in blocks **705**, **706**, **709**, **710**, **712**, a decoded version of the INTRA frame is built up in the frame store **740**. When the last macroblock of the current frame has been INTRA coded and subsequently decoded, the frame store **740** contains a completely decoded frame, available for use as a prediction reference frame in coding a subsequently received video frame in INTER format. In embodiments of the invention in which before-hand sub-pixel value interpolation is performed, the reference frame held in frame store **740** is at least partially interpolated to sub-pixel resolution.

Operation of the encoder **700** in INTER coding mode will now be described. In INTER coding mode, the control manager **720** operates switch **702** to receive its input from line **721**, which comprises the output of the combiner **716**. The combiner **716** forms prediction error information representing the difference between the current macroblock of the frame being coded and its prediction, produced in the motion compensated prediction block **780**. The prediction error information is DCT transformed in block **705** and quantised in block **706** to form a macroblock of DCT transformed and quantised prediction error information. Each macroblock of DCT transformed and quantised prediction error information is passed from the quantiser **706** to the MUX/DMUX unit **790**. The MUX/DMUX unit **790** combines the prediction error information **723** with motion coefficients **724** (described in the following) and control information (for example header data, quantisation parameter information, error correction data etc.) to form a single bit-stream of coded image information, **725**.

Locally decoded prediction error information for the each macroblock of the INTER coded frame is then formed in the encoder **700** by passing the encoded prediction error infor-

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mation **723** output by the quantiser **706** through the inverse quantiser **709** and applying an inverse DCT transform in block **710**. The resulting locally decoded macroblock of prediction error information is then input to combiner **712**. In INTER-mode, switch **714** is set so that the combiner **712** also receives motion predicted macroblocks for the current INTER frame, produced in the motion compensated prediction block **780**. The combiner **712** combines these two pieces of information to produce reconstructed image blocks for the current INTER frame.

As described above when considering INTRA coded frames, in embodiments of the invention in which before-hand sub-pixel value interpolation is performed, the output from combiner **712** is applied to the before-hand sub-pixel interpolation block **730**. Thus, the input to the before-hand sub-pixel value interpolation block **730** in INTER coding mode also takes the form of decoded image blocks. In the before-hand sub-pixel value interpolation block **730**, each decoded macroblock is subjected to sub-pixel interpolation in such a way that a predetermined sub-set of sub-pixel values is calculated according to the interpolation method of the invention and is stored together with the decoded pixel values in frame store **740**. In embodiments in which before-hand sub-pixel interpolation is not performed, before-hand sub-pixel interpolation block is not present in the encoder architecture and the output from combiner **712**, comprising decoded image blocks, is applied directly to frame store **740**.

As subsequent macroblocks of the video signal are received from the video source and undergo the previously described coding and decoding steps in blocks **705**, **706**, **709**, **710**, **712**, a decoded version of the INTER frame is built up in the frame store **740**. When the last macroblock of the frame has been INTER coded and subsequently decoded, the frame store **740** contains a completely decoded frame, available for use as a prediction reference frame in encoding a subsequently received video frame in INTER format. In embodiments of the invention in which before-hand sub-pixel value interpolation is performed, the reference frame held in frame store **740** is at least partially interpolated to sub-pixel resolution.

Formation of a prediction for a macroblock of the current frame will now be described.

Any frame encoded in INTER format requires a reference frame for motion compensated prediction. This means, inter alia, that when encoding a video sequence, the first frame to be encoded, whether it is the first frame in the sequence, or some other frame, must be encoded in INTRA format. This, in turn, means that when the video encoder **700** is switched into INTER coding mode by control manager **720**, a complete reference frame, formed by locally decoding a previously encoded frame, is already available in the frame store **740** of the encoder. In general, the reference frame is formed by locally decoding either an INTRA coded frame or an INTER coded frame.

The first step in forming a prediction for a macroblock of the current frame is performed by motion estimation block **760**. The motion estimation block **760** receives the current macroblock of the frame being coded via line **727** and performs a block matching operation in order to identify a region in the reference frame which corresponds substantially with the current macroblock. According to the invention, the block-matching process is performed to sub-pixel resolution in a manner that depends on the implementation of the encoder **700** and the degree of before-hand sub-pixel interpolation performed. However, the basic principle behind the block-matching process is similar in all cases. Specifically, motion estimation block **760** performs block-matching by calculating difference values (e.g. sums of absolute differences) representing the difference in pixel values between the macroblock of the current frame under examination and candidate best-matching regions of pixels/sub-pixels in the reference frame. A difference value is produced for all possible offsets (e.g. quarter- or one eighth sub-pixel precision x, y displacements) between the macroblock of the current frame and candidate test region within a predefined search region of the reference frame and motion estimation block **760** determines the smallest calculated difference value. The offset between the macroblock in the current frame and the candidate test region of pixel values/sub-pixel values in the reference frame that yields the smallest difference value defines the motion vector for the macroblock in question. In certain embodiments of the invention, an initial estimate for the motion vector having unit pixel precision is first determined and then refined to a finer level of sub-pixel precision, as described in the foregoing.

In embodiments of the encoder in which before-hand sub-pixel value interpolation is not performed, all sub-pixel values required in the block matching process are calculated in on-demand sub-pixel value interpolation block **750**. Motion estimation block **760** controls on-demand sub-pixel value interpolation block **750** to calculate each sub-pixel value needed in the block-matching process in an on-demand fashion, as and when it is required. In this case, motion estimation block **760** may be implemented so as to perform block-matching as a one-step process, in which case a motion vector with the desired sub-pixel resolution is sought directly, or it may be implemented so as to perform block-matching as a two step process. If the two-step process is adopted, the first step may comprise a search for e.g. a full or half-pixel resolution motion vector and the second step is performed in order to refine the motion vector to the desired sub-pixel resolution. As block matching is an exhaustive process, in which blocks of n×m pixels in the current frame are compared one-by-one with blocks of n×m pixels or sub-pixels in the interpolated reference frame, it should be appreciated that a sub-pixel calculated in an on-demand fashion by the on-demand pixel interpolation block **750** may need to be calculated multiple times as successive difference values are determined. In a video encoder, this approach is not the most efficient possible in terms of computational complexity/burden.

In embodiments of the encoder which use only before-hand sub-pixel value interpolation, block-matching may be performed as a one step process, as all sub-pixel values of the reference frame required to determine a motion vector with the desired sub-pixel resolution are calculated before-hand in block **730** and stored in frame store **740**. Thus, they are directly available for use in the block-matching process and can be retrieved as required from frame store **740** by motion estimation block **760**. However, even in the case where all sub-pixel values are available from frame store **740**, it is still more computationally efficient to perform block-matching as a two-step process, as fewer difference calculations are required. It should be appreciated that while full before-hand sub-pixel value interpolation reduces computational complexity in the encoder, it is not the most efficient approach in terms of memory consumption.

In embodiments of the encoder in which both before-hand and on-demand sub-pixel value interpolation are used, motion estimation block **760** is implemented in such a way that it can retrieve sub-pixel values previously calculated in before-hand sub-pixel value interpolation block **730** and stored in frame store **740** and further control on-demand sub-pixel value interpolation block **750** to calculate any additional sub-pixel values that may be required. The block-

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matching process may be performed as a one-step or a two-step process. If a two-step implementation is used, before-hand calculated sub-pixel values retrieved from frame store **740** may be used in the first step of the process and the second step may be implemented so as to use sub-pixel values calculated by on-demand sub-pixel value interpolation block **750**. In this case, certain sub-pixel values used in the second step of the block matching process may need to be calculated multiple times as successive comparisons are made, but the number of such duplicate calculations is significantly less than if before-hand sub-pixel value calculation is not used. Furthermore, memory consumption is reduced with respect to embodiments in which only before-hand sub-pixel value interpolation is used.

Once the motion estimation block **760** has produced a motion vector for the macroblock of the current frame under examination, it outputs the motion vector to the motion field coding block **770**. Motion field coding block **770** then approximates the motion vector received from motion estimation block **760** using a motion model. The motion model generally comprises a set of basis functions. More specifically, the motion field coding block **770** represents the motion vector as a set of coefficient values (known as motion coefficients) which, when multiplied by the basis functions, form an approximation of the motion vector. The motion coefficients **724** are passed from motion field coding block **770** to motion compensated prediction block **780**. Motion compensated prediction block **780** also receives the pixel/sub-pixel values of the best-matching candidate test region of the reference frame identified by motion estimation block **760**. In FIG. **7**, these values are shown to be passed via line **729** from on-demand sub-pixel interpolation block **750**. In alternative embodiments of the invention, the pixel values in question are provided from the motion estimation block **760** itself.

Using the approximate representation of the motion vector generated by motion field coding block **770** and the pixel/sub-pixel values of the best-matching candidate test region, motion compensated prediction block **780** produces a macroblock of predicted pixel values. The macroblock of predicted pixel values represents a prediction for the pixel values of the current macroblock generated from the interpolated reference frame. The macroblock of predicted pixel values is passed to the combiner **716** where it is subtracted from the new current frame in order to produce prediction error information **723** for the macroblock, as described in the foregoing.

The motion coefficients **724** formed by motion field coding block are also passed to the MUX/DMUX unit **790**, where they are combined with prediction error information **723** for the macroblock in question and possible control information from control manager **720** to form an encoded video stream **725** for transmission to a receiving terminal.

Operation of a video decoder **800** according to the invention will now be described. Referring to FIG. **8**, the decoder **800** comprises a demultiplexing unit (MUX/DMUX) **810**, which receives the encoded video stream **725** from the encoder **700** and demultiplexes it, an inverse quantiser **820**, an inverse DCT transformer **830**, a motion compensated prediction block **840**, a frame store **850**, a combiner **860**, a control manager **870**, an output **880**, before-hand sub-pixel value interpolation block **845** and on-demand sub-pixel interpolation block **890** associated with the motion compensated prediction block **840**. In practice the control manager **870** of the decoder **800** and the control manager **720** of the encoder **700** may be the same processor. This may be the case if the encoder **700** and decoder **800** are part of the same video codec.

FIG. **8** shows an embodiment in which a combination of before-hand and on-demand sub-pixel value interpolation is used in the decoder. In other embodiments, only before-hand sub-pixel value interpolation is used, in which case decoder **800** does not include on-demand sub-pixel value interpolation block **890**. In a preferred embodiment of the invention, no before-hand sub-pixel value interpolation is used in the decoder and therefore before-hand sub-pixel value interpolation block **845** is omitted from the decoder architecture. If both before-hand and on-demand sub-pixel value interpolation are performed, the decoder comprises both blocks **845** and **890**.

The control manager **870** controls the operation of the decoder **800** in response to whether an INTRA or an INTER frame is being decoded. An INTRA/INTER trigger control signal, which causes the decoder to switch between decoding modes is derived, for example, from picture type information provided in the header portion of each compressed video frame received from the encoder. The INTRA/INTER trigger control signal is passed to control manager **870** via control line **815**, together with other video codec control signals demultiplexed from the encoded video stream **725** by the MUX/DMUX unit **810**.

When an INTRA frame is decoded, the encoded video stream **725** is demultiplexed into INTRA coded macroblocks and control information. No motion vectors are included in the encoded video stream **725** for an INTRA coded frame. The decoding process is performed macroblock-by-macroblock. When the encoded information **723** for a macroblock is extracted from video stream **725** by MUX/DMUX unit **810**, it is passed to inverse quantiser **820**. The control manager controls inverse quantiser **820** to apply a suitable level of inverse quantisation to the macroblock of encoded information, according to control information provided in video stream **725**. The inverse quantised macroblock is then inversely transformed in the inverse DCT transformer **830** to form a decoded block of image information. Control manager **870** controls combiner **860** to prevent any reference information being used in the decoding of the INTRA coded macroblock. The decoded block of image information is passed to the video output **880** of the decoder.

In embodiments of the decoder which employ before-hand sub-pixel value interpolation, the decoded block of image information (i.e. pixel values) produced as a result of the inverse quantisation and inverse transform operations performed in blocks **820** and **830** is passed to before-hand sub-pixel value interpolation block **845**. Here, sub-pixel value interpolation is performed according to the method of the invention, the degree of before-hand sub-pixel value interpolation applied being determined by the details of the decoder implementation. In embodiments of the invention in which on-demand sub-pixel value interpolation is not performed, before-hand sub-pixel value interpolation block **845** interpolates all sub-pixelvalues. In embodiments that use a combination of before-hand and on-demand sub-pixel value interpolation, before-hand sub-pixel value interpolation block **845** interpolates a certain sub-set of sub-pixel values. This may comprise, for example, all sub-pixels at half-pixel locations, or a combination of sub-pixels at half-pixel and one quarter-pixel locations. In any case, after before-hand sub-pixel value interpolation, the interpolated sub-pixel values are stored in frame store **850**, together with the original decoded pixel values. As subsequent macroblocks are decoded, before-hand interpolated and stored, a decoded frame, at least partially interpolated to sub-pixel resolution is progressively assembled in the frame store **850** and becomes available for use as a reference frame for motion compensated prediction.

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In embodiments of the decoder which do not employ before-hand sub-pixel value interpolation, the decoded block of image information (i.e. pixel values) produced as a result of the inverse quantisation and inverse transform operations performed on the macroblock in blocks **820** and **830** is passed directly to frame store **850**. As subsequent macroblocks are decoded and stored, a decoded frame, having unit pixel resolution is progressively assembled in the frame store **850** and becomes available for use as a reference frame for motion compensated prediction.

When an INTER frame is decoded, the encoded video stream **725** is demultiplexed into encoded prediction error information **723** for each macroblock of the frame, associated motion coefficients **724** and control information. Again, the decoding process is performed macroblock-by-macroblock. When the encoded prediction error information **723** for a macroblock is extracted from the video stream **725** by MUX/DMUX unit **810**, it is passed to inverse quantiser **820**. Control manager **870** controls inverse quantiser **820** to apply a suitable level of inverse quantisation to the macroblock of encoded prediction error information, according to control information received in video stream **725**. The inverse quantised macroblock of prediction error information is then inversely transformed in the inverse DCT transformer **830** to yield decoded prediction error information for the macroblock.

The motion coefficients **724** associated with the macroblock in question are extracted from the video stream **725** by MUX/DMUX unit **810** and passed to motion compensated prediction block **840**, which reconstructs a motion vector for the macroblock using the same motion model as that used to encode the INTER-coded macroblock in encoder **700**. The reconstructed motion vector approximates the motion vector originally determined by motion estimation block **760** of the encoder. The motion compensated prediction block **840** of the decoder uses the reconstructed motion vector to identify the location of a block of pixel/sub-pixel values in a prediction reference frame stored in frame store **850**. The reference frame may be, for example, a previously decoded INTRA frame, or a previously decoded INTER frame. In either case, the block of pixel/sub-pixel values indicated by the reconstructed motion vector, represents the prediction of the macroblock in question.

The reconstructed motion vector may point to any pixel or sub-pixel. If the motion vector indicates that the prediction for the current macroblock is formed from pixel values (i.e. the values of pixels at unit pixel locations), these can simply be retrieved from frame store **850**, as the values in question are obtained directly during the decoding of each frame. If the motion vector indicates that the prediction for the current macroblock is formed from sub-pixel values, these must either be retrieved from frame store **850**, or calculated in on-demand sub-pixel interpolation block **890**. Whether sub-pixel values must be calculated, or can simply be retrieved from the frame store, depends on the degree of before-hand sub-pixel value interpolation used in the decoder.

In embodiments of the decoder that do not employ before-hand sub-pixel value interpolation, the required sub-pixel values are all calculated in on-demand sub-pixel value interpolation block **890**. On the other hand, in embodiments in which all sub-pixel values are interpolated before-hand, motion compensated prediction block **840** can retrieve the required sub-pixel values directly from the frame store **850**. In embodiments that use a combination before-hand and on-demand sub-pixel value interpolation, the action required in order to obtain the required sub-pixel values depends on which sub-pixel values are interpolated before-hand. Taking as an example an embodiment in which all sub-pixel values at half-pixel locations are calculated before-hand, it is evident that if a reconstructed motion vector for a macroblock points to a pixel at unit location or a sub-pixel at half-pixel location, all the pixel or sub-pixel values required to form the prediction for the macroblock are present in the frame store **850** and can be retrieved from there by motion compensated prediction block **840**. If, however, the motion vector indicates a sub-pixel at a quarter-pixel location, the sub-pixels required to form the prediction for the macroblock are not present in frame store **850** and are therefore calculated in on-demand sub-pixel value interpolation block **890**. In this case, on-demand sub-pixel value interpolation block **890** retrieves any pixel or sub-pixel required to perform the interpolation from frame store **850** and applies the interpolation method described below. Sub-pixel values calculated in on-demand sub-pixel value interpolation block **890** are passed to motion compensated prediction block **840**.

Once a prediction for a macroblock has been obtained, the prediction (that is, a macroblock of predicted pixel values) is passed from motion compensated prediction block **840** to combiner **860** where it combined with the decoded prediction error information for the macroblock to form a reconstructed image block which, in turn, is passed to the video output **880** of the decoder.

It should be appreciated that in practical implementations of encoder **700** and decoder **800**, the extent to which frames are before-hand sub-pixel interpolated, and thus the amount of on-demand sub-pixel value interpolation that is performed, can be chosen according to, or dictated by, the hardware implementation of the video encoder **700**, or the environment in which it is intended to be used. For example, if the memory available to the video encoder is limited, or memory must be reserved for other functions, it is appropriate to limit the amount of before-hand sub-pixel value interpolation that is performed. In other cases, where the microprocessor performing the video encoding operation has limited processing capacity, e.g. the number of operations per second that can be executed is comparatively low, it is more appropriate to restrict the amount of on-demand sub-pixel value interpolation that is performed. In a mobile communications environment, for example, when video encoding and decoding functionality is incorporated in a mobile telephone or similar wireless terminal for communication with a mobile telephone network, both memory and processing power may be limited. In this case a combination of before-hand and on-demand sub-pixel value interpolation may be the best choice to obtain an efficient implementation in the video encoder. In video decoder **800**, use of before-hand sub-pixel value is generally not preferred, as it typically results in the calculation of many sub-pixel values that are not actually used in the decoding process. However, it should be appreciated that although different amounts of before-hand and on-demand interpolation can be used in the encoder and decoder in order to optimise the operation of each, both encoder and decoder can be implemented so as to use the same division between before-hand and on-demand sub-pixel value interpolation.

Although the foregoing description does not describe the construction of bi-directionally predicted frames (B-frames) in the encoder **700** and the decoder **800**, it should be understood that in embodiments of the invention, such a capability may be provided. Provision of such capability is considered within the ability of one skilled in the art.

An encoder **700** or a decoder **800** according to the invention can be realised using hardware or software, or using a suitable combination of both. An encoder or decoder implemented in software may be, for example, a separate program or a soft-

ware building block that can be used by various programs. In the above description and in the drawings, the functional blocks are represented as separate units, but the functionality of these blocks can be implemented, for example, in one software program unit.

The encoder **700** and decoder **800** can further be combined in order to form a video codec having both encoding and decoding functionality. In addition to being implemented in a multimedia terminal, such a codec may also be implemented in a network. A codec according to the invention may be a computer program or a computer program element, or it may be implemented at least partly using hardware.

The sub-pixel interpolation method used in the encoder **700** and decoder **800** according to the invention now be described in detail. The method will first be introduced at a general conceptual level and then two preferred embodiments will be described. In the first preferred embodiment, sub-pixel value interpolation is performed to ¼ pixel resolution and in the second the method is extended to⅛ pixel resolution.

It should be noted that interpolation must produce identical values in the encoder and the decoder, but its implementation should be optimized for both entities separately. For example, in an encoder according to the first embodiment of the invention in which sub-pixel value interpolation is preformed to ¼ pixel resolution, it is most efficient to calculate ½ resolution pixels before-hand and to calculate values for ¼ resolution sub-pixels in an on-demand fashion, only when they are needed during motion estimation. This has the effect of limiting memory usage while keeping the computational complexity/burden at an acceptable level. In the decoder, on the other hand, it is advantageous not to pre-calculate any of the sub-pixels. Therefore, it should be appreciated that a preferred embodiment of the decoder does not include before-hand sub-pixel value interpolation block **845** and all sub-pixel value interpolation is performed in on-demand sub-pixel value interpolation block **890**.

In the description of the interpolation method provided below, references are made to the pixel positions depicted in FIG. **14***a*. In this figure pixels labelled A represent original pixels (that is, pixels residing at unit horizontal and vertical locations). Pixels labelled with other letters represent sub-pixels that are to be interpolated. The description that follows will adhere to the previously introduced conventions regarding the description of pixel and sub-pixel locations.

Next, the steps required to interpolate all sub-pixel positions are described:

Values for the ½ resolution sub-pixels labelled b are obtained by first calculating an intermediate value b using a Kth order filter, according to:

$$b = \sum_{i=1}^{K} x_i A_i \tag{9}$$

where x_i is a vector of filter coefficients, A_i is a corresponding vector of original pixel values A situated at unit horizontal and unit vertical locations, and K is an integer which defines the order of the filter. Thus, equation 9 can be re-expressed as:

$$b = x_1A_1 + x_2A_2 + x_3A_3 + \ldots + x_{K-1}A_{K-1} + x_KA_K \tag{10}$$

The values of the filter coefficients x_i and the order of the filter K may vary from embodiment to embodiment. Equally, different coefficient values may be used in the calculation of different sub-pixels within an embodiment. In other embodiments, the values of filter coefficients x_i and the order of the filter may depend on which of the ½ resolution b sub-pixels is being interpolated. Pixels A_i are disposed symmetrically with respect to the ½ resolution sub-pixel b being interpolated and are the closest neighbours of that sub-pixel. In the case of the ½ resolution sub-pixel b situated at half horizontal and unit vertical location, pixels A_i are disposed horizontally with respect to b (as shown in FIG. **14***b*). If the ½ resolution sub-pixel b situated at unit horizontal and half vertical location is being interpolated, pixels A_i are disposed vertically with respect to b (as shown in FIG. **14***c*).

A final value for ½ resolution sub-pixel b is calculated by dividing intermediate value b by a constant $scale_1$, truncating it to obtain an integer number and clipping the result to lie in the range $[0, 2^n-1]$. In alternative embodiments of the invention rounding may be performed instead of truncation. Preferably, constant $scale_1$ is chosen to be equal to the sum of filter coefficients x_i.

A value for the ½ resolution sub-pixel labelled c is also obtained by first calculating an intermediate value c using an Mth order filter, according to:

$$c = \sum_{i=1}^{M} y_i b_i \tag{11}$$

where y_i is a vector of filter coefficients, b_i is a corresponding vector of intermediate values b_i in the horizontal or vertical direction. i.e.:

$$c = y_1b_1 + y_2b_2 + y_3b_3 + \ldots + y_{M-1}b_{M-1} + y_Mb_M \tag{12}$$

The values of the filter coefficients y_i and the order of the filter M may vary from embodiment to embodiment. Equally, different coefficient values may be used in the calculation of different sub-pixels within an embodiment. Preferably, the b values are intermediate values for ½ resolution sub-pixels b which are disposed symmetrically with respect to ½ resolution sub-pixel c and are the closest neighbours of sub-pixel c. In an embodiment of the invention, the ½ resolution sub-pixels b are disposed horizontally with respect to sub-pixel c, in an alternative embodiment they are disposed vertically with respect to sub-pixel c.

A final value of ½ resolution sub-pixel c is computed by dividing intermediate value c by a constant $scale_2$, truncating it to obtain an integer number and clipping the result to lie in the range $[0, 2^n-1]$. In alternative embodiments of the invention rounding may be performed instead of truncation. Preferably, constant $scale_2$ is equal to $scale_1$*$scale_1$.

It should be noted that the use of intermediate values b in the horizontal direction leads to the same result as using intermediate values b in the vertical direction.

There are two alternatives for interpolating values for the ¼ resolution sub-pixels labelled h. Both involve linear interpolation along a diagonal line linking ½ resolution sub-pixels neighbouring the ¼ resolution sub-pixel h being interpolated. In a first embodiment, a value for sub-pixel h is calculated by averaging the values of the two ½ resolution sub-pixels b closest to sub-pixel h. In a second embodiment, a value for sub-pixel h is calculated by averaging the values of the closest pixel A and the closest ½ resolution sub-pixel c. It should be appreciated that this provides the possibility of using different combinations of diagonal interpolations to determine the values for sub-pixels h within the confines of different groups of 4 image pixels A. However, it should also be realised that the same combination should be used in both the encoder and the decoder in order to produce identical interpolation results.

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FIG. **15** depicts 4 possible choices of diagonal interpolation for sub-pixels h in adjacent groups of 4 pixels within an image. Simulations in the TML environment have verified that both embodiments result in similar compression efficiency. The second embodiment has higher complexity, since calculation of sub-pixel c requires calculation of several intermediate values. Therefore the first embodiment is preferred.

Values for ¼ resolution sub-pixels labelled d and g are calculated from the values of their nearest horizontal neighbours using linear interpolation. In other words, a value for ¼ resolution sub-pixel d is obtained by averaging values of its nearest horizontal neighbours, original image pixel A and ½ resolution sub-pixel b. Similarly, a value for ¼ resolution sub-pixel g is obtained by taking the average of its two nearest horizontal neighbours, ½ resolution sub-pixels b and c.

Values for ¼ resolution sub-pixels labelled e, f and i are calculated from the values of their nearest neighbours in the vertical direction using linear interpolation. More specifically, a value for ¼ resolution sub-pixel e is obtained by averaging the values of its two nearest vertical neighbours, original image pixel A and ½ resolution sub-pixel b. Similarly, a value for ¼ resolution sub-pixel f is obtained by taking the average of its two nearest vertical neighbours, ½ resolution sub-pixels b and c. In an embodiment of the invention, a value for ¼ resolution sub-pixel i is obtained in manner identical to that just described in connection with ¼ resolution sub-pixel f. However, in an alternative embodiment of the invention, and in common with the H.26 test models TML5 and TML6 previously described, ¼ resolution sub-pixel i is determined using the values of the four closest original image pixels, according to $(A_1+A_2+A_3+A_4+2)/4$.

It should also be noted that in all cases where an average involving pixel and/or sub-pixel values is determined, the average may be formed in any appropriate manner. For example, the value for ¼ resolution sub-pixel d can be defined as d=(A+b)/2 or as d=(A+b+1)/2. The addition of 1 to the sum of values for pixel A and ½ resolution sub-pixel b has the effect of causing any rounding or truncation operation subsequently applied to round or truncate the value for d to the next highest integer value. This is true for any sum of integer values and may be applied to any of the averaging operations performed according to the method of the invention in order to control rounding or truncation effects.

It should be noted that the sub-pixel value interpolation method according to the invention provides advantages over each of TML5 and TML6.

In contrast to TML5, in which the values of some of the ¼ resolution sub-pixels depend on previously interpolated values obtained for other ¼ resolution sub-pixels, in the method according to the invention, all ¼ resolution sub-pixels are calculated from original image pixels or ½ resolution sub-pixel positions using linear interpolation. Thus, the reduction in precision of those ¼ resolution sub-pixel values which occurs in TML5 due to the intermediate truncation and clipping of the other ¼ resolution sub-pixels from which they are calculated, does not take place in the method according to the invention. In particular, referring to FIG. **14***a*, ¼ resolution sub-pixels h (and sub-pixel i in one embodiment of the invention) are interpolated diagonally in order to reduce dependency on other ¼-pixels. Furthermore, in the method according to the invention, the number of calculations (and therefore the number of processor cycles) required to obtain a value for those ¼ resolution sub-pixels in the decoder is reduced compared with TML5. Additionally, the calculation of any ¼ resolution sub-pixel value requires a number of calculations which is substantially similar to the number of calculations required to determine any other ¼ resolution sub-pixel value. More specifically, in a situation where the required ½ resolution sub-pixel values are already available, e.g. they have been calculated before-hand, the number of calculations required to interpolate a ¼ resolution sub-pixel value from the pre-calculated ½ resolution sub-pixel values is the same as the number of calculations required to calculate any other ¼ resolution sub-pixel value from the available ½ resolution sub-pixel values.

In comparison with TML6, the method according to the invention does not require high precision arithmetic to be used in the calculation of all sub-pixels. Specifically, as all of the ¼ resolution sub-pixel values are calculated from original image pixels or ½ resolution sub-pixel values using linear interpolation, lower precision arithmetic can be used in their interpolation. Consequently, in hardware implementations of the inventive method, for example in an ASIC (Application Specific Integrated Circuit), the use of lower precision arithmetic reduces the number of components (e.g. gates) that must be devoted to the calculation of ¼ resolution sub-pixel values. This, in turn, reduces the overall area of silicon that must be dedicated to the interpolation function. As the majority of sub-pixels are, in fact, ¼ resolution sub-pixels (12 out of the 15 sub-pixels illustrated in FIG. **14***a*), the advantage provided by the invention in this respect is particularly significant. In software implementations, where sub-pixel interpolation is performed using the standard instruction set of a general purpose CPU (Central Processor Unit) or using a DSP (Digital Signal Processor), a reduction in the precision of the arithmetic required generally leads to an increase in the speed at which the calculations can be performed. This is particularly advantageous in 'low cost' implementations, in which it is desirable to use a general purpose CPU rather than any form of ASIC.

The method according to the invention provides still further advantages compared with TML5. As mentioned previously, in the decoder only 1 out of the 15 sub-pixel positions is required at any given time, namely that which is indicated by received motion vector information. Therefore, it is advantageous if the value of a sub-pixel in any sub-pixel location can be calculated with the minimum number of steps that result in a correctly interpolated value. The method according to the invention provides this capability. As mentioned in the detailed description provided above, ½ resolution sub-pixel c can be interpolated by filtering in either the vertical or the horizontal direction, the same value being obtained for c regardless of whether horizontal or vertical filtering is used. The decoder can therefore take advantage of this property when calculating values for ¼ resolution sub-pixels f and g in such a way as to minimise the number of operations required in order to obtain the required values. For example, if the decoder requires a value for ¼ resolution sub-pixel f, ½ resolution sub-pixel c should interpolated in the vertical direction. If a value is required for ¼ resolution sub-pixel g, it is advantageous to interpolate a value for c in the horizontal direction. Thus, in general, it can be said that the method according to the invention provides flexibility in the way in which values are derived for certain ¼ resolution sub-pixels. No such flexibility is provided in TML5.

Two specific embodiments will now be described in detail. The first represents a preferred embodiment for calculating sub-pixels with up to ¼ pixel resolution, while in the second, the method according to the invention is extended to the calculation of values for sub-pixels having up to ⅛ pixel resolution. For both embodiments a comparison is provided between the computational complexity/burden resulting from use of the method according to the invention and that which

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would result from use of the interpolation methods according to TML5 and TML6 in equivalent circumstances.

The preferred embodiment for interpolating sub-pixels at ¼ pixel resolution will be described with reference to FIGS. **14***a*, **14***b* and **14***c*. In the following, it will be assumed that all image pixels and final interpolated values for sub-pixels are represented with 8-bits.

Calculation of ½ resolution sub-pixels at i) half unit horizontal and unit vertical locations and ii) unit horizontal and half unit vertical locations.

1. A value for the sub-pixel at half unit horizontal and unit vertical location, that is ½ resolution sub-pixel b in FIG. **14***a*, is obtained by first calculating intermediate value $b=(A_1-5A_2+20A_3+20A_4-5A_5+A_6)$ using the values of the six pixels (A_1 to A_6) which are situated at unit horizontal and unit vertical locations in either the row or the column of pixels containing b and which are disposed symmetrically about b, as shown in FIGS. **14***b* and **14***c*. A final value for ½ resolution sub-pixel b is calculated as (b+16)/32 where the operator / denotes division with truncation. The result is clipped to lie in the range [0, 255].

Calculation of ½ resolution sub-pixels at half unit horizontal and half unit vertical locations.

2. A value for the sub-pixel at half unit horizontal and half unit vertical location, that is ½ resolution sub-pixel c in FIG. **14***a*, is calculated as $c=(b_1-5b_2+20b_3+20b_4-5b_5+b_6+512)/1024$ using the intermediate values b for the six closest ½ resolution sub-pixels which are situated in either the row or the column of sub-pixels containing c and which are disposed symmetrically about c. Again, operator / denotes division with truncation and the result is clipped to lie in the range [0, 255]. As previously explained, using intermediate values b for ½ resolution sub-pixels b in the horizontal direction leads to the same result as using intermediate values b for ½ resolution sub-pixels b in the vertical direction. Thus, in an encoder according to the invention, the direction for interpolating ½ resolution sub-pixels b can be chosen according to a preferred mode of implementation. In a decoder according to the invention, the direction for interpolating sub-pixels b is chosen according to which, if any, ¼ resolution sub-pixels will be interpolated using the result obtained for ½ resolution sub-pixel c.

Calculation of ¼ resolution sub-pixels at i) quarter unit horizontal and unit vertical locations; ii) quarter unit horizontal and half unit vertical locations; iii) unit horizontal and quarter unit vertical locations; and iv) half unit horizontal and quarter unit vertical locations.

3. Values for ¼ resolution sub-pixels d, situated at quarter unit horizontal and unit vertical locations are calculated according to d=(A+b)/2 using the nearest original image pixel A and the closest ½ resolution sub-pixel b in the horizontal direction. Similarly, values for ½ resolution sub-pixels g, situated at quarter unit horizontal and half unit vertical locations are calculated according to g=(b+c)/2 using the two nearest ½ resolution sub-pixels in the horizontal direction. In a similar manner, values for ¼ resolution sub-pixels e, situated at unit horizontal and quarter unit vertical locations, are calculated according e=(A+b)/2 using the nearest original image pixel A and the closest ½ resolution sub-pixel b in the vertical direction. Values for ¼ resolution sub-pixels f, situated at half unit horizontal and quarter unit vertical locations, are determined from f=(b+c)/2 using the two nearest ½ resolution sub-pixel in the vertical direction. In all cases, operator / denotes division with truncation.

Calculation of ¼ resolution sub-pixels at quarter unit horizontal and quarter unit vertical locations.

4. Values for ¼ resolution sub-pixels h, situated at quarter unit horizontal and quarter unit vertical locations are calculated according to $h=(b_1+b_2)/2$, using the two nearest ½ resolution sub-pixels b in the diagonal direction. Again, operator / denotes division with truncation.
5. A value for the ¼ resolution sub-pixel labeled i is computed from $i=(A_1+A_2+A_3+A_4+2)/4$ using the four nearest original pixels A. Once more, operator / denotes division with truncation.

An analysis of the computational complexity of the first preferred embodiment of the invention will now be presented.

In the encoder, it is likely that the same sub-pixel values will be calculated multiple times. Therefore, and as previously explained, the complexity of the encoder can be reduced by pre-calculating all sub-pixel values and storing them in memory. However, this solution increases memory usage by a large margin. In the preferred embodiment of the invention, in which motion vector accuracy is ¼ pixel resolution in both the horizontal and vertical dimensions, storing pre-calculated sub-pixel values for the whole image requires 16 times the memory required to store the original, non-interpolated image. To reduce memory usage, all ½ resolution sub-pixels can be interpolated before-hand and ¼ resolution sub-pixels can be calculated on-demand, that is, only when they are needed. According to the method of the invention, on-demand interpolation of values for ¼ resolution sub-pixels only requires linear interpolation from ½ resolution sub-pixels. Four times the original picture memory is required to store the pre-calculated ½ resolution sub-pixels since only 8 bits are necessary to represent them.

However, if the same strategy of pre-calculating all ½ resolution sub-pixels using before-hand interpolation is used in conjunction with the direct interpolation scheme of TML6, the memory requirements increase to 9 times the memory required to store the original non-interpolated image. This results from the fact that a larger number of bits is required to store the high precision intermediate values associated with each ½ resolution sub-pixel in TML6. In addition, the complexity of sub-pixel interpolation during motion estimation is higher in TML6, since scaling and clipping has to be performed for every ½ and ¼ sub-pixel location.

In the following, the complexity of the sub-pixel value interpolation method according to the invention, when applied in a video decoder, is compared with that of the interpolation schemes used in TML5 and TML6. Throughout the analysis which follows, it is assumed that in each method the interpolation of any sub-pixel value is performed using only the minimum number of steps required to obtain a correctly interpolated value. It is further assumed that each method is implemented in a block based manner, that is, intermediate values common for all the sub-pixels to be interpolated in a particular N×M block are calculated only once. An illustrative example is provided in FIG. **16**. Referring to FIG. **16**, it can be seen that in order to calculate a 4×4 block of ½ resolution sub-pixels c, a 9×4 block of ½ resolution sub-pixels b is first calculated.

Compared with the sub-pixel value interpolation method used in TML5, the method according to the invention has a lower computational complexity for the following reasons:

1. Unlike the sub-pixel value interpolation scheme used in TML5, according to the method of the invention, a value for ½ resolution sub-pixel c can be obtained by filtering in either the vertical or the horizontal direction. Thus, in order to reduce the number of operations, ½ resolution sub-pixel c can be interpolated in the vertical direction if a value for ¼ resolution sub-pixel f is required and in the horizontal direction if a value for ¼ resolution sub-pixel pixel g is

required. As an example, FIG. **17** shows all the ½ resolution sub-pixel values that must be calculated in order to interpolate values for ¼ resolution sub-pixels g in an image block defined by 4×4 original image pixels using the interpolation method of TML5 (FIG. **17***a*) and using the method according to the invention (FIG. **17***b*). In this example, the sub-pixel value interpolation method according to TML5 requires a total of 88½ resolution sub-pixels to be interpolated, while the method according to the invention requires the calculation of 72½ resolution sub-pixels. As can be seen from FIG. **17***b*, according to the invention, ½ resolution sub-pixels c are interpolated in the horizontal direction in order to reduce the number of calculations required.

2. According to the method of the invention, ¼ resolution sub-pixel h is calculated by linear interpolation from its two closest neighbouring ½ resolution sub-pixels in the diagonal direction. The respective numbers of ½ resolution sub-pixels that must be calculated in order to obtain values for ¼ resolution sub-pixels h within a 4×4 block of original image pixels using the sub-pixel value interpolation method according to TML5 and the method according to the invention are shown in FIGS. **18**(*a*) and **18**(*b*), respectively. Using the method according to TML5 it is necessary to interpolate a total of 56½ resolution sub-pixels, while according to the method of the invention it is necessary to interpolate 40½ resolution sub-pixels.

Table 1 summarizes the decoder complexities of the three sub-pixel value interpolation methods considered here, that according to TML5, the direct interpolation method used in TML6 and the method according to the invention. Complexity is measured in terms of the number of 6-tap filtering and linear interpolation operations performed. It is assumed that Interpolation of ¼ resolution sub-pixel i is calculated according to $i=(A_1+A_2+A_3+A_4+2)/4$ which is bilinear interpolation and effectively comprises two linear interpolation operations. The operations needed to interpolate sub-pixel values with one 4×4 block of original image pixels are listed for each of the 15 sub-pixel positions which, for convenience of reference, are numbered according to the scheme shown in FIG. **19**. Referring to FIG. **19**, location **1** is the location of an original image pixel A and locations **2** to **16** are sub-pixel locations. Location **16** is the location of ¼ resolution sub-pixel i. In order to compute the average number of operations it has been assumed that the probability of a motion vector pointing to each sub-pixel position is the same. The average complexity is therefore the average of the 15 sums calculated for each sub-pixel location and the single full-pixel location.

TABLE 1

Complexity of ¼ resolution sub-pixel interpolation in TML5, TML6 and the method according to the invention.

	TML5		TML6		Inventive Method	
Location	linear.	6-tap	linear.	6-tap	linear.	6-tap
1	0	0	0	0	0	0
3, 9	0	16	0	16	0	16
2, 4, 5, 13	16	16	0	16	16	16
11	0	52	0	52	0	52
7, 15	16	52	0	52	16	52
10, 12	16	68	0	52	16	52
6, 8, 14	48	68	0	52	16	32
16	32	0	32	0	32	0
Average	19	37	2	32	13	28.25

It can be seen from Table 1 that the method according to the invention requires fewer 6-tap filter operations than the sub-pixel value interpolation method according to TML6 and only a few additional linear interpolation operations. Since 6-tap filter operations are much more complex than linear interpolation operations the complexity of the two methods is similar. The sub-pixel value interpolation method according to TML5 has a considerably higher complexity.

The preferred embodiment for interpolating sub-pixels with up to ⅛ pixel resolution will now be described with reference to FIGS. **20**, **21** and **22**.

FIG. **20** presents the nomenclature used to describe pixels, ½ resolution sub-pixels, ¼ resolution sub-pixels and ⅛ resolution sub-pixels in this extended application of the method according to the invention.

1. Values for the ½ resolution and ¼ resolution sub-pixels labelled b^1, b^2 and b^3 in FIG. **20** are obtained by first calculating intermediate values $b^1=(-3A_1+12A_2-37A_3+229A_4+71A_5-21A_6+6A_7-A_8)$; $b^2=(-3A_1+12A_2-39A_3+158A_4+158A_5-39A_6+12A_7-3A_8)$; and $b^3=(-A_1+6A_2-21A_3+71A_4+229A_5-37A_6+13A_7-3A_8)$ using the values of the eight nearest image pixels (A_1 to A_8) situated at unit horizontal and unit vertical locations in either the row or the column containing b^1, b^2 and b^3 and disposed symmetrically about ½ resolution sub-pixel b^2. The asymmetries in the filter coefficients used to obtain intermediate values b^1 and b^3 account for the fact that pixels A_1 to A_8 are not symmetrically located with respect to ¼ resolution sub-pixels b^1 and b^3. Final values for sub-pixels b^i, i=1, 2, 3 are calculated according to $b^i=(b^i+128)/256$ where the operator / denotes division with truncation. The result is clipped to lie in the range [0, 255].
2. Values for the ½ resolution and ¼ resolution sub-pixels labelled c^{ij}, i, j=1, 2, 3, are calculated according to $c^{1j}=(-3b_1^j+12b_2^j-37b_3^j+229b_4^j+71b_5^j-21b_6^j+6b_7^j-b_8^j+32768)/65536$, $c^{2j}=(-3b_1^j+12b_2^j-39b_3^j+158b_4^j+158b_5^j-39b_6^j+12b_7^j-3b_8^j+32768)/65536$ and $c^{3j}=(-b_1^j+6b_2^j-21b_3^j+71b_4^j+229b_5^j-37b_6^j+13b_7^j-3b_8^j+32768)/65536$ using the intermediate values b^1, b^2 and b^3 calculated for the eight closest sub-pixels (b_1^j to b_8^j) in the vertical direction, sub-pixels b^j being situated in the column comprising the ½ resolution and ¼ resolution sub-pixels c^{ij} being interpolated and disposed symmetrically about the ½ resolution sub-pixel c^{2j}. The asymmetries in the filter coefficients used to obtain values for sub-pixels c^{1j} and c^{3j} account for the fact that sub-pixels b_1^j to b_8^j are not symmetrically located with respect to ¼ resolution sub-pixels c^{1j} and c^{3j}. Once more, operator / denotes division with truncation. Before the interpolated values for sub-pixels c^{ij} are stored in the frame memory they are clipped to lie in the range [0, 255]. In an alternative embodiment of the invention, ½ resolution and ¼ resolution sub-pixels c^{ij} are calculated using in an analogous manner using intermediate values b^1, b^2 and b^3 in the horizontal direction.
3. Values for ⅛ resolution sub-pixels labelled d are calculated using linear interpolation from the values of their closest neighbouring image pixel, ½ resolution or ¼ resolution sub-pixels in the horizontal or vertical direction. For example, upper leftmost ⅛ resolution sub-pixel d is calculated according to $d=(A+b^1+1)/2$. As before, operator / indicates division with truncation.
4. Values for ⅛ resolution sub-pixels labelled e and f are calculated using linear interpolation from the values of image pixels, ½ resolution or ¼ resolution sub-pixels in the diagonal direction. For example, referring to FIG. **20**, upper leftmost pixel ⅛ resolution sub-pixel e is calculated according to $e=(b^1+b^1+1)/2$. The diagonal direction to be used in the interpolation of each ⅛ resolution sub-pixel in a first preferred embodiment of the invention, hereinafter

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referred to as 'preferred method 1', is indicated in FIG. **21**(*a*). Values for ⅛ resolution sub-pixels labelled g are calculated according to $g=(A+3c^{22}+3)/4$. As always, operator / denotes division with truncation. In an alternative embodiment of the invention, hereinafter referred to as 'preferred method 2', computational complexity is further reduced by interpolating ⅛ resolution sub-pixels f using linear interpolation from ½ resolution sub-pixels b^2, that is, according to the relationship $f=(3b^2+b^2+2)/4$. The b^2 sub-pixel which is closer to f is multiplied by 3. The diagonal interpolation scheme used in this alternative embodiment of the invention is depicted in FIG. **21**(*b*). In further alternative embodiments, different diagonal interpolation schemes can be envisaged.

It should be noted that in all cases where an average involving pixel and/or sub-pixel values is used in the determination of ⅛ resolution sub-pixels, the average may be formed in any appropriate manner. The addition of 1 to the sum of values used in calculating such an average has the effect of causing any rounding or truncation operation subsequently applied to round or truncate the average in question to the next highest integer value. In alternative embodiments of the invention, the addition of 1 is not used.

As in the case of sub-pixel value interpolation to ¼ pixel resolution previously described, memory requirements in the encoder can be reduced by pre-calculating only a part of the sub-pixel values to be interpolated. In the case of sub-pixel value interpolation to ⅛ pixel resolution, it is advantageous to calculate all ½ resolution and ¼ resolution sub-pixels beforehand and to compute values for ⅛ resolution sub-pixels in an on-demand fashion, only when they are required. When this approach is taken, both the interpolation method according to TML5 and that according to the invention require 16 times the original picture memory to store the ½ resolution and ¼ resolution sub-pixel values. However, if the direct interpolation method according to TML6 is used in the same way, intermediate values for the ½ resolution and ¼ pixel resolution sub-pixels must be stored. These intermediate values are represented with 32-bit precision and this results in a memory requirement 64 times that for the original, non-interpolated image.

In the following, the complexity of the sub-pixel value interpolation method according to the invention, when applied in a video decoder to calculate values for sub-pixels at up to ⅛ pixel resolution, is compared with that of the interpolation schemes used in TML5 and TML6. As in the equivalent analysis for ¼ pixel resolution sub-pixel value interpolation described above, it is assumed that in each method the interpolation of any sub-pixel value is performed using only the minimum number of steps required to obtain a correctly interpolated value. It is also assumed that each method is implemented in a block based manner, such that intermediate values common for all the sub-pixels to be interpolated in a particular N×M block are calculated only once.

Table 2 summarizes complexities of the three interpolation methods. Complexity is measured in terms of the number of 8-tap filter and linear interpolation operations performed in each method. The table presents the number of operations required to interpolate each of the 63⅛ resolution sub-pixels within one 4×4 block of original image pixels, each sub-pixel location being identified with a corresponding number, as illustrated in FIG. **22**. In FIG. **22**, location **1** is the location of an original image pixel and locations **2** to **64** are sub-pixel locations. When computing the average number of operations, it has been assumed that the probability of a motion vector pointing to each sub-pixel position is the same. The average complexity is thus the average of the 63 sums calculated for each sub-pixel location and the single full-pixel location.

TABLE 2

Complexity of ⅛ resolution sub-pixel interpolation in TML5, TML6 and the method according to the invention. (Results shown separately for Preferred Method 1 and Preferred Method 2).

	TML5		TML6		Preferred Method 1		Preferred Method 2	
Location	linear.	8-tap	linear.	8-tap	linera.	8-tap	linear.	8-tap
1	0	0	0	0	0	0	0	0
3, 5, 7, 17, 33, 49	0	16	0	16	0	16	0	16
19, 21, 23, 35, 37, 39, 51, 53, 55	0	60	0	60	0	60	0	60
2, 8, 9, 57	16	16	0	16	16	16	16	16
4, 6, 25, 41	16	32	0	16	16	32	16	32
10, 16, 58, 64	32	76	0	60	16	32	16	32
11, 13, 15, 59, 61, 63	16	60	0	60	16	60	16	60
18, 24, 34, 40, 50, 56	16	76	0	60	16	60	16	60
12, 14, 60, 62	32	120	0	60	16	32	16	32
26, 32, 42, 48	32	108	0	60	16	32	16	32
20, 22, 36, 38, 52, 54	16	120	0	60	16	76	16	76
27, 29, 31, 43, 45, 47	16	76	0	60	16	76	16	76
28, 30, 44, 46	32	152	0	60	16	60	16	60
Average	64	290.25	0	197.75	48	214.75	48	192.75

As can be seen from Table 2, the number of 8-tap filtering operations performed according to preferred methods 1 and 2 are, respectively, 26% and 34% lower than the number of 8-tap filtering operation performed in the sub-pixel value interpolation method of TML5. The number of linear operations is 25% lower, in both preferred method 1 and preferred method 2, compared with TML5, but this improvement is of lesser importance compared to the reduction in 8-tap filtering operations. It can further be seen that the direct interpolation method used in TML6 has a complexity comparable that of both preferred methods 1 and 2 when used to interpolate values for ⅛ resolution sub-pixels.

In view of the foregoing description it will be evident to a person skilled in the art that various modifications may be made within the scope of the invention. While a number of preferred embodiments of the invention have been described

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in detail, it should be apparent that many modifications and variations thereto are possible, all of which fall within the true spirit and scope of the invention.

The invention claimed is:

1. A method for sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the method comprising causing an apparatus to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

2. A method according to claim **1**, comprising causing the apparatus to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, wherein when the chosen weighted average is that involving the value of a nearest neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, causing the apparatus to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the nearest-neighbouring pixel and the sub-pixel situated at co-ordinates ½, ½ to the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

3. A method according to claim **2**, comprising causing the apparatus to use first and second weights with equal values when the nearest-neighbouring pixel and sub-pixel pixel situated at co-ordinates ½, ½ are equidistant from the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

4. A method according to claim **1**, comprising causing the apparatus to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, wherein when the chosen weighted average is that involving the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, causing the apparatus to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the sub-pixels having co-ordinates with even values of K and L to the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

5. A method according to claim **4**, comprising causing the apparatus to use first and second weights with equal values when the sub-pixels having co-ordinates with even values of K and L are equidistant from the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

6. A method according to claim **1**, comprising causing the apparatus to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an even value and L equal to an odd value is also required.

7. A method according to claim **1**, comprising causing the apparatus to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an odd value and L equal to an even value is also required.

8. A method according to claim **1**, comprising causing the apparatus to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an odd value O and L equal to an even value E, not including zero or 2^N, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to the even value O−1 and L equal to E and a second sub-pixel having co-ordinates with K equal to the even value O+1 and L equal to E.

9. A method according to claim **1**, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2 and L equal to zero.

10. A method according to claim **1**, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to zero.

11. A method according to claim **1**, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2 and L equal to 2^N.

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12. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to 2^N.

13. A method according to claim 1, comprising causing the apparatus to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value E, not including zero or 2^N, and L equal to an odd value O, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to E and L equal to the even value O−1 and a second sub-pixel having co-ordinates with K equal to E and L equal to the even value O+1.

14. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

15. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2.

16. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-2.

17. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-2.

18. A method according to claim 1, comprising causing the apparatus to interpolate a sub-pixel value for the sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N-1, by taking a weighted average of the values of the four corner pixels that define the rectangular bounded region.

19. A method according to claim 1, in which N is one of the values 2, 3, and 4.

20. A method according to claim 1, wherein the pixels have a predetermined dynamic range, said predetermined dynamic range corresponding to the range of values said pixels can take.

21. A method according to claim 20, comprising interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and for sub-pixels having co-ordinates with K equal to zero and L equal to an even value, using weighted sums of the values of pixels located in rows and columns respectively, to produce a first intermediate value, said first intermediate value having a dynamic range equal to the predetermined dynamic range of the pixels used in said weighted sum multiplied by a value equal to the sum of the respective weights used in said weighted sum.

22. A method according to claim 21, wherein the dynamic range of said first intermediate value is defined by the number of bits used to represent the respective pixels used in said weighted sum plus the number of bits required to represent the sum of the respective weights used in said weighted sum.

23. A method according to claim 21, comprising truncating the first intermediate value by mathematically dividing the first intermediate value by a first scale factor, said first scale factor having a value equal to the sum of the respective weights used in said weighted sum, thereby forming a sub-pixel value with a dynamic range equal to the predetermined dynamic range of said pixels.

24. A method according to claim 23, comprising using a truncated first intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

25. A method according to claim 21, comprising interpolating sub-pixel values for sub-pixels having co-ordinates with even values of K and L, using a weighted sum comprising first intermediate values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and corresponding first intermediate values for sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, to produce a second intermediate value, said second intermediate value having a dynamic range equal to the dynamic range of the first intermediate values used in said weighted sum, multiplied by a value equal to the sum of the respective weights used in said weighted sum.

26. A method according to claim 25, comprising truncating the second intermediate value by mathematically dividing the second intermediate value by a second scale factor, said second scale factor having a value equal to the sum of the respective weights used in the weighted sum of claim 21 multiplied by the sum of the respective weights used in the weighted sum of claim 25, thereby forming a sub-pixel value with a dynamic range equal to the predetermined dynamic range of said pixels.

27. A method according to claim 26, comprising using a truncated second intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

28. A method according to claim 21, comprising interpolating sub-pixel values for sub-pixels having co-ordinates with even values of K and L, using a weighted sum comprising first intermediate values for sub-pixels having co-ordinates with K equal to zero and L equal to an even value and corresponding first intermediate values for sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions to produce a second intermediate value, said second intermediate value having a dynamic range equal to the dynamic range of the first intermediate values used in said weighted sum, multiplied by a value equal to the sum of the respective weights used in said weighted sum.

29. A method according to claim 28, comprising truncating the second intermediate value by mathematically dividing the second intermediate value by a second scale factor, said second scale factor having a value equal to the sum of the respective weights used in the weighted sum of claim 21 multiplied by the sum of the respective weights used in the weighted sum of claim 28, thereby forming a sub-pixel value with a dynamic range equal to the dynamic range of said pixels.

30. A method according to claim 29, comprising using a truncated second intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

31. A method for quarter resolution sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation K/4, L/4, K and L being

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positive integers having respective values between zero and 4, the method comprising causing an apparatus to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with K and L equal to 1 or 3, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ¾, ¾, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with K and L equal to zero, 2 or 4, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ¾, ¾ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to 2 and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, used in the interpolation of the sub-pixels having co-ordinates with K and L equal to 1 or 3, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate a sub-pixel value for the sub-pixel having co-ordinates with both K and L equal to 2, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with K and L equal to 1 or 3, using a predetermined choice of either a weighted sum of the values of the sub-pixel having co-ordinates with K equal to 2 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the value of the sub-pixel having co-ordinates with K equal to zero and L equal to 2 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

32. A method for eighth resolution sub-pixel value interpolation to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically with the rectangular bounded region using the co-ordinate notation K/8, L/8, K and L being positive integers having respective values between zero and 8, the method comprising causing an apparatus to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with K and L equal to 1, 3, 5 or 7, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ⅜, ⅜, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with K and L equal to zero, 2, 4, 6 or 8, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ⅜, ⅜ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6, used in the interpolation of the sub-pixels having co-ordinates with K and L equal to 1, 3, 5 or 7, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with K and L equal to 2, 4 or 6, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with K and L equal to 1, 3, 5 or 7, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

33. An interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

34. An interpolator according to claim **33**, wherein the interpolator is configured to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, wherein when the chosen weighted average is that involving the value of a nearest neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, the interpolator is configured to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the nearest-neighbouring pixel and the sub-pixel situated at co-ordinates ½, ½ to the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

35. An interpolator according to claim **34**, wherein the interpolator is configured to use first and second weights with equal values when the nearest-neighbouring pixel and sub-

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pixel situated at co-ordinates ½, ½ are equidistant from the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

36. An interpolator according to claim **33**, wherein the interpolator is configured to use a first and a second weight in the weighted average chosen to interpolate the sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, wherein when the chosen weighted average is that involving the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, the interpolator is configured to select the relative magnitudes of the first and second weights to be inversely proportional to the respective straight-line diagonal distances of the sub-pixels having co-ordinates with even values of K and L to the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

37. An interpolator according to claim **36**, wherein the interpolator is configured to use first and second weights with equal values when the sub-pixels having co-ordinates with even values of K and L are equidistant from the sub-pixel having co-ordinates with odd values of K and L whose value is being interpolated.

38. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an even value and L equal to an odd value is also required.

39. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions when the value of a sub-pixel having co-ordinates with K equal to an odd value and L equal to an even value is also required.

40. A method according to claim **33**, comprising truncating the second intermediate value by mathematically dividing the second intermediate value by a second scale factor, said second scale factor having a value equal to the sum of the respective weights used in the weighted sum of claim **63** multiplied by the sum of the respective weights used in the weighted sum of claim **67**, thereby forming a sub-pixel value with a dynamic range equal to the dynamic range of said pixels.

41. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2 and L equal to zero.

42. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to zero, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N31 2 and L equal to zero.

43. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2 and L equal to 2^N.

44. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N-2 and L equal to 2^N.

45. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value E, not including zero or 2^N, and L equal to an odd value O, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to E and L equal to the even value O−1 and a second sub-pixel having co-ordinates with K equal to E and L equal to the even value O+1.

46. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to zero, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2.

47. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to zero, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2.

48. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to zero and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to zero and L equal to 2^N-2.

49. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-1, by taking an average of the value of a pixel having co-ordinates with K equal to 2^N and L equal to 2^N, and a sub-pixel having co-ordinates with K equal to 2^N and L equal to 2^N-2.

50. An interpolator according to claim **33**, wherein the interpolator is configured to interpolate a sub-pixel value for the sub-pixel having co-ordinates with K equal to 2^N-1 and L equal to 2^N-1, by taking a weighted average of the values of the four corner pixels that define the rectangular bounded region.

51. An interpolator according to claim **33**, wherein N is set equal to 2.

52. An interpolator according to claim **33**, wherein N is set equal to 3.

53. An interpolator according to claim **33**, wherein the pixels have a predetermined dynamic range, said predetermined dynamic range corresponding to the range of values said pixels can take.

54. An interpolator according to claim **53**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value

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and L equal zero and for sub-pixels having co-ordinates with K equal to zero and L equal to an even value, using weighted sums of the values of pixels located in rows and columns respectively, to produce a first intermediate value, said first intermediate value having a dynamic range equal to the predetermined dynamic range of the pixels used in said weighted sum multiplied by a value equal to the sum of the respective weights used in said weighted sum.

55. An interpolator according to claim **54**, wherein the dynamic range of said first intermediate value is defined by the number of bits used to represent the respective pixels used in said weighted sum plus the number of bits required to represent the sum of the respective weights used in said weighted sum.

56. An interpolator according to claim **54**, wherein the interpolator is configured to truncate the first intermediate value by mathematically dividing the first intermediate value by a first scale factor, said first scale factor having a value equal to the sum of the respective weights used in said weighted sum, thereby forming a sub-pixel value with a dynamic range equal to the predetermined dynamic range of said pixels.

57. An interpolator according to claim **56**, wherein the interpolator is configured to use a truncated first intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

58. An interpolator according to claim **54**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, using a weighted sum comprising first intermediate values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and corresponding first intermediate values for sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, to produce a second intermediate value, said second intermediate value having a dynamic range equal to the dynamic range of the first intermediate values used in said weighted sum, multiplied by a value equal to the sum of the respective weights used in said weighted sum.

59. An interpolator according to claim **58**, wherein the interpolator is configured to truncate the second intermediate value by mathematically dividing the second intermediate value by a second scale factor, said second scale factor having a value equal to the sum of the respective weights used in the weighted sum of claim **54** multiplied by the sum of the respective weights used in the weighted sum of claim **58**, thereby forming a sub-pixel value with a dynamic range equal to the predetermined dynamic range of said pixels.

60. An interpolator according to claim **59**, wherein the interpolator is configured to use a truncated second intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

61. An interpolator according to claim **54**, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, using a weighted sum comprising first intermediate values for sub-pixels having co-ordinates with K equal to zero and L equal to an even value and corresponding first intermediate values for sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded region to produce a second intermediate value, said second intermediate value having a dynamic range equal to the dynamic range of the first intermediate values used in said weighted sum, multiplied by a value equal to the sum of the respective weights used in said weighted sum.

62. An interpolator according to claim **61**, wherein the interpolator is configured to truncated the second intermediate value by mathematically dividing the second intermediate value by a second scale factor, said second scale factor having a value equal to the sum of the respective weights used in the weighted sum of claim **54** multiplied by the sum of the respective weights used in the weighted sum of claim **61**, thereby forming a sub-pixel value with a dynamic range equal to the predetermined dynamic range of said pixels.

63. An interpolator according to claim **62**, wherein the interpolator is configured to use a truncated second intermediate sub-pixel value when interpolating a value for a sub-pixel having co-ordinates with odd values of K and L.

64. A video encoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent bounded rectangular regions.

65. A codec comprising a video encoder according to claim **64** and a video decoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and

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2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of a either weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co- ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

66. A communications terminal comprising a video encoder according to claim **64**.

67. A communications terminal according to claim **66**, wherein the communications terminal is a wireless terminal.

68. A still image encoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

69. A codec comprising a still image encoder according to claim **68** and a still image decoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co- ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

70. A communications terminal comprising a still image encoder according to claim **68**.

71. A video encoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to

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determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded region.

72. A communications terminal comprising a video decoder according to claim **71**.

73. A still image decoder comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

74. A communications terminal comprising a still image decoder according to claim **73**.

75. An interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator comprising:

circuitry configured to interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

circuitry configured to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

circuitry configured to interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even

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value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

76. An interpolator for quarter resolution sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation K/4, L/4, K and L being positive integers having respective values between zero and 4, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with K and L equal to 1 or 3, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ¾, ¾, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with K and L equal to zero, 2 or 4, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ¾, ¾ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to 2 and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, used in the interpolation of the sub-pixels having co-ordinates with K and L equal to 1 or 3, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate a sub-pixel value for the sub-pixel having co-ordinates with both K and L equal to 2, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with both K and L equal to 1 or 3, using a predetermined choice of either a weighted sum of the values of the sub-pixel having co-ordinates with K equal to 2 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the value of the sub-pixel having co-ordinates with K equal to zero and L equal to 2 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

77. A video encoder or still image encoder comprising an interpolator according to claim **76**.

78. A communications terminal comprising a video encoder or still image encoder according to claim **77**.

79. An interpolator for eighth resolution sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically with the rectangular bounded region using the co-ordinate notation K/8, L/8, K and L being positive integers having respective values between zero and 8, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with K and L equal to 1, 3, 5 or 7, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ⅜, ⅜, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with both K and L equal to zero, 2, 4, 6 or 8, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ⅜, ⅜ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6, used in the interpolation of the sub-pixels having co-ordinates with both K and L equal to 1, 3, 5 or 7, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with K and L equal to 2, 4 or 6, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with K and L equal to 1, 3, 5 or 7, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to 2, 4 or 6 and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to 2, 4 or 6 and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

80. A video decoder or still image decoder comprising an interpolator according to claim **79**.

81. A communications terminal comprising a video decoder or still image decoder according to claim **80**.

82. A computer program for sub-pixel value interpolation, embodied on a computer readable storage medium, the computer program being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the computer program comprising:

computer program code for interpolating a sub-pixel value for a sub-pixel having co-ordinates with odd values of both K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of both K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

computer program code for interpolating sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

computer program code for interpolating sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with

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K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

83. A network apparatus comprising an interpolator for sub-pixel value interpolation, the interpolator being configured to determine values for sub-pixels situated within a rectangular bounded region defined by four corner pixels with no intermediate pixels between the corners, the pixels and sub-pixels being configured for display in rows and columns, pixel and sub-pixel locations in the rows and columns being representable mathematically within the rectangular bounded region using the co-ordinate notation $K/2^N$, $L/2^N$, K and L being positive integers having respective values between zero and 2^N, N being a positive integer greater than one and representing a particular degree of sub-pixel value interpolation, the interpolator being configured to:

interpolate a sub-pixel value for a sub-pixel having co-ordinates with odd values of K and L, according to a predetermined choice of either a weighted average of the value of a nearest-neighbouring pixel and the value of the sub-pixel situated at co-ordinates ½, ½, or a weighted average of the values of a pair of diagonally-opposed sub-pixels having co-ordinates with even values of K and L, including zero, situated within a quadrant of the rectangular bounded region, the quadrant being defined by the sub-pixel having co-ordinates ½, ½ and the nearest neighbouring pixel;

interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an even value and L equal to zero and sub-pixels having co-ordinates with K equal to zero and L equal to an even value, used in the interpolation of the sub-pixels having co-ordinates with odd values of K and L, using weighted sums of the values of pixels located in rows and columns respectively; and

interpolate sub-pixel values for sub-pixels having co-ordinates with even values of K and L, used in the interpolation of sub-pixel values for the sub-pixels having co-ordinates with odd values of K and L, using a predetermined choice of either a weighted sum of the values of sub-pixels having co-ordinates with K equal to an even value and L equal to zero and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions, or a weighted sum of the values of sub-pixels having co-ordinates with K equal to zero and L equal to an even value and the values of sub-pixels having corresponding co-ordinates in immediately adjacent rectangular bounded regions.

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UNITED STATES PATENT AND TRADEMARK OFFICE

CERTIFICATE OF CORRECTION

PATENT NO. : 8,036,273 B2
APPLICATION NO. : 11/839205
DATED : October 11, 2011
INVENTOR(S) : Karczewicz et al.

It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

Title Page, item (75); Column 1, line 2, in the Second Inventor's Name, delete "Antti Hallapuro" and insert -- Antti Olli Hallapuro -- therefor.

Column 1, line 2, in the Second Inventor's Residence, delete "FL (US)" and insert -- (FI) -- therefor.

Column 51, line 64, in Claim 3, after -- pixel -- delete "pixel".

Column 55, line 22, in Claim 31, after -- with -- delete "both".

Column 57, line 46-53, delete Claim 40 and insert -- An interpolator according to claim 33, wherein the interpolator is configured to interpolate sub-pixel values for sub-pixels having co-ordinates with K equal to an odd value O and L equal to an even value E, not including zero or 2^N, by taking an average of the value of a first sub-pixel having co-ordinates with K equal to the even value O – 1 and L equal to E and a second sub-pixel having co-ordinates with K equal to the even value O + 1 and L equal to E. -- therefor.

Column 57, line 66, in Claim 42, delete "2^N31 2" and insert -- 2^N-2 -- therefor.

Column 59, line 1, in Claim 54, delete "equal" and insert -- equal to -- therefor.

Column 59, line 60, in Claim 61, delete "region" and insert -- regions -- therefor.

Column 59, line 67, in Claim 62, delete "truncated" and insert -- truncate -- therefor.

Column 60, line 55-56, in Claim 64, delete "bounded rectangular regions" and insert -- rectangular bounded regions -- therefor.

Column 61, line 6, in Claim 65, delete "of a either" and insert -- of either a -- therefor.

Signed and Sealed this
Sixth Day of March, 2012

David J. Kappos

David J. Kappos
Director of the United States Patent and Trademark Office

Column 61, line 13, in Claim 65, delete "co- ordinates" and insert -- co-ordinates -- therefor.

Column 61, line 54, in Claim 68, after -- of -- delete "both".

Column 62, line 41, in Claim 69, delete "co- ordinates" and insert -- co-ordinates -- therefor.

Column 62, line 66, in Claim 71, delete "encoder" and insert -- decoder -- therefor.

Column 63, line 43, in Claim 71, delete "region" and insert -- regions -- therefor.

Column 65, line 34, in Claim 76, after -- with -- delete "both".

Column 65, line 36, in Claim 76, after -- with -- delete "both".

Column 65, line 67, in Claim 79, after -- with -- delete "both".

Column 66, line 9, in Claim 79, after -- with -- delete "both".

Column 66, line 44, in Claim 82, after -- of -- delete "both".

Column 66, line 49, in Claim 82, after -- of -- delete "both".