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Larsson

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(54) **CYCLIC DELAY DIVERSITY FOR
MITIGATING INTERSYMBOL
INTERFERENCE IN OFDM SYSTEMS**

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(*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35 U.S.C. 154(b) by 734 days.

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(21) Appl. No.: **09/667,504**

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(51) **Int. Cl.**⁷ **H04K 1/10**; H04L 27/28

Primary Examiner—Stephen Chin

(52) **U.S. Cl.** **375/260**; 455/10

Assistant Examiner—Harry Vartanian

(58) **Field of Search** 375/260, 267,
375/430, 347, 348; 455/562.1, 101

(57) **ABSTRACT**

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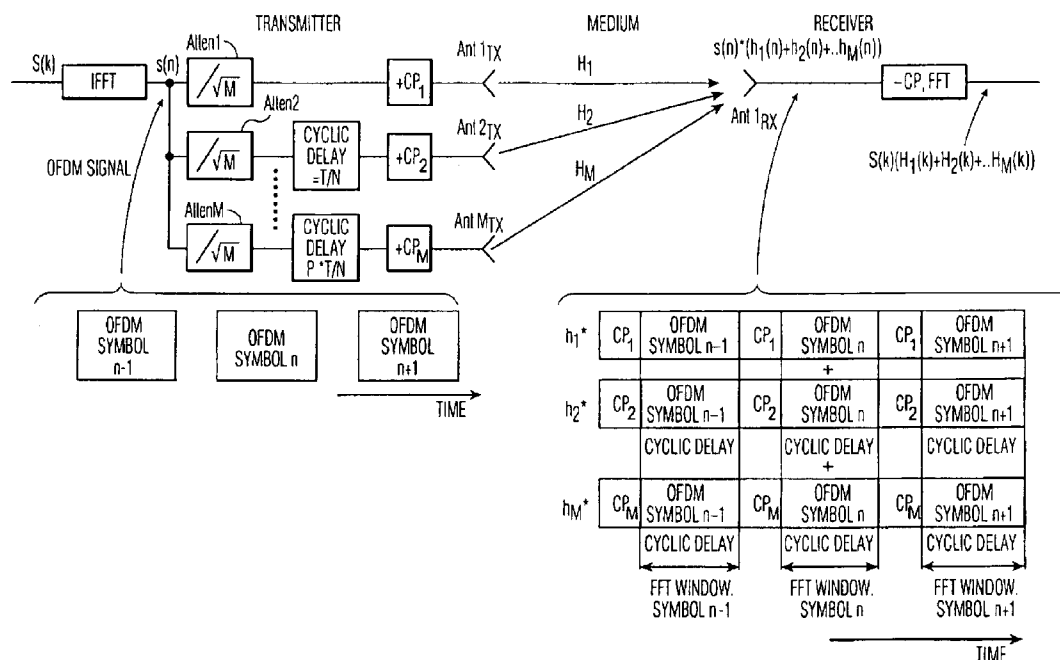
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21 Claims, 10 Drawing Sheets



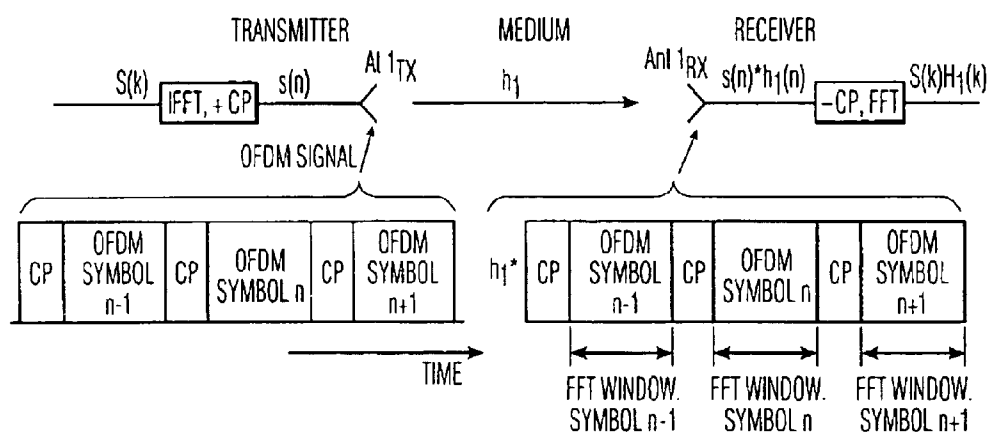


FIG. 1
(PRIOR ART)

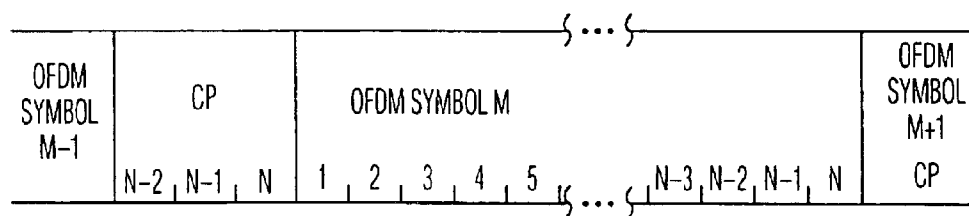


FIG. 2
(PRIOR ART)

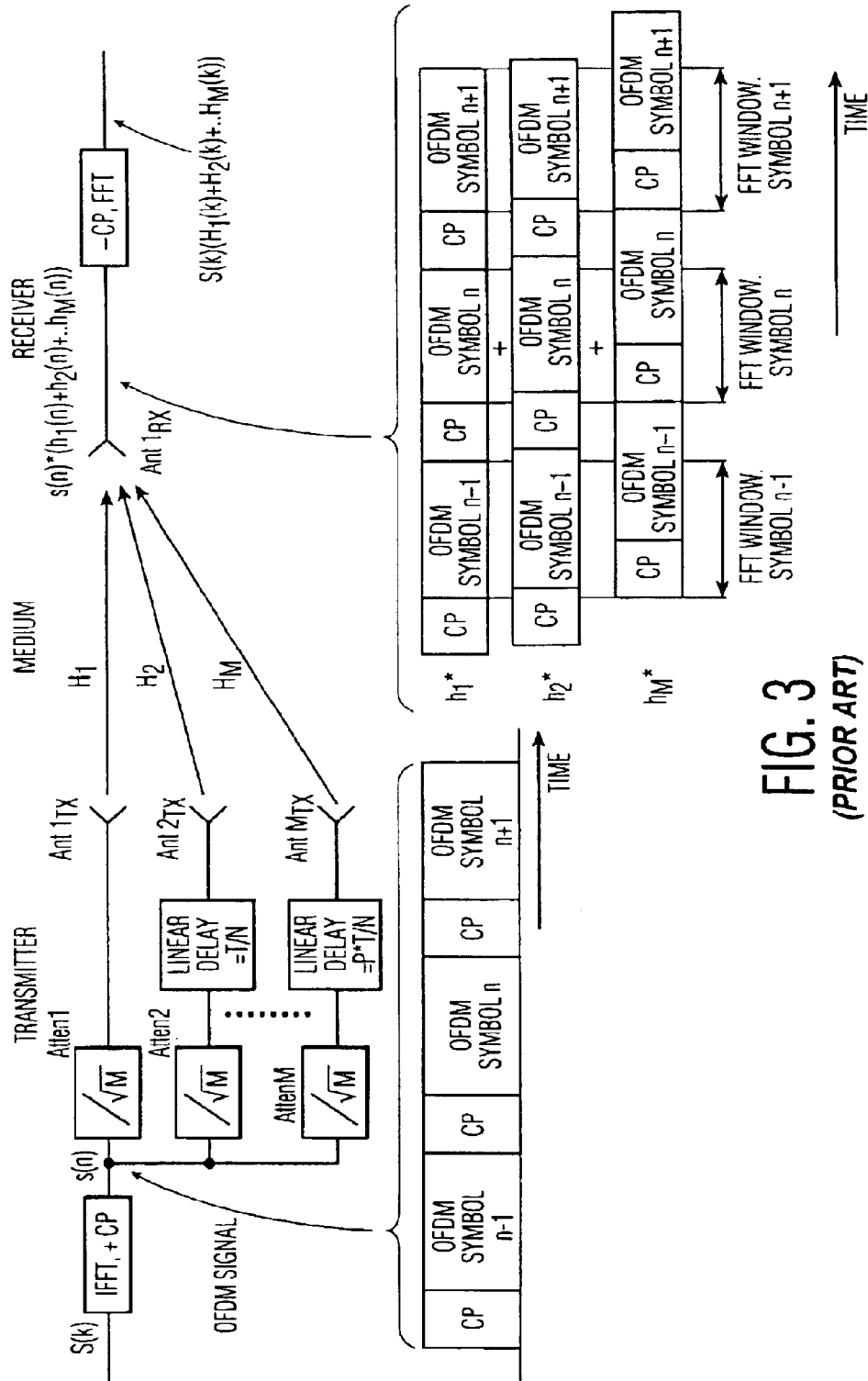


FIG. 3
(PRIOR ART)

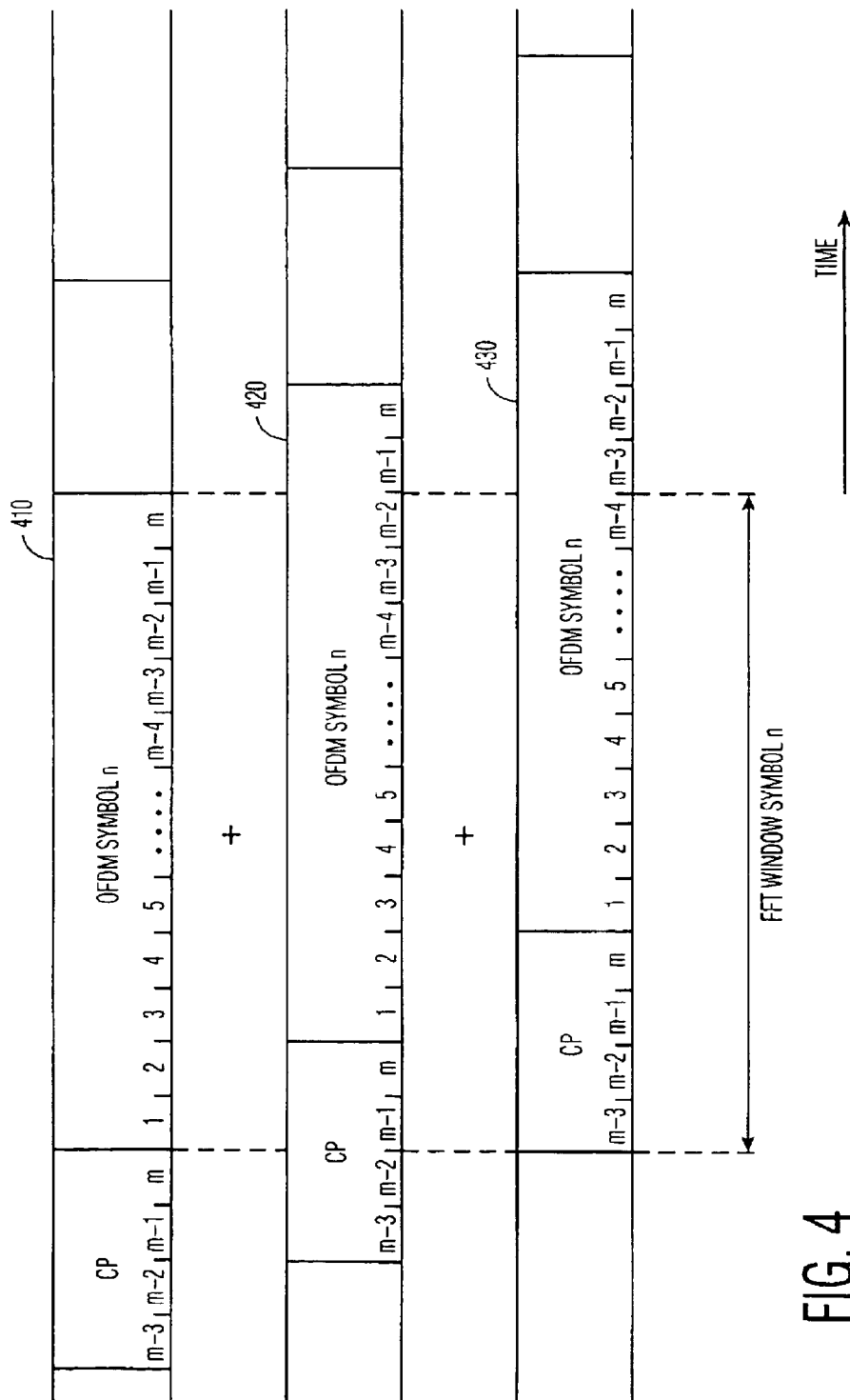


FIG. 4
(PRIOR ART)

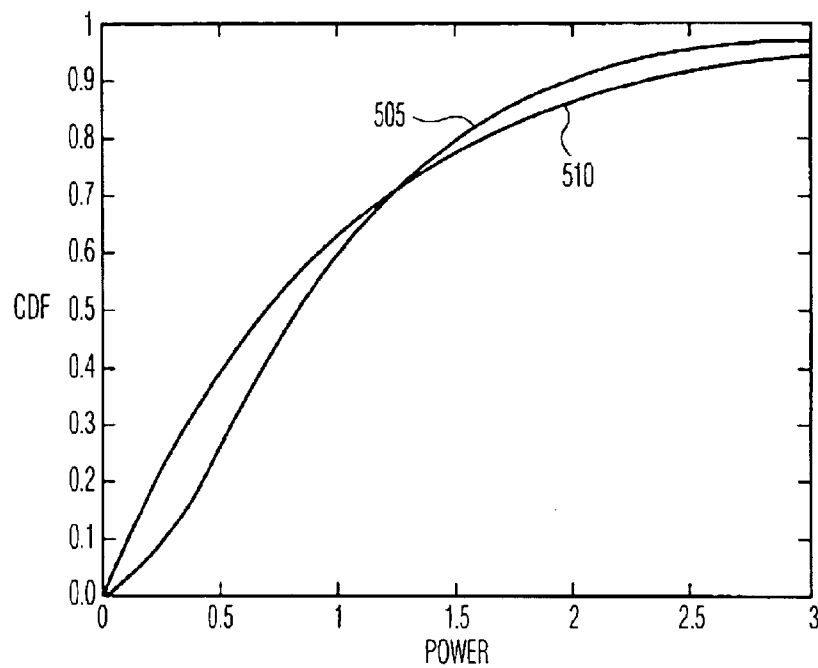


FIG. 5
(PRIOR ART)

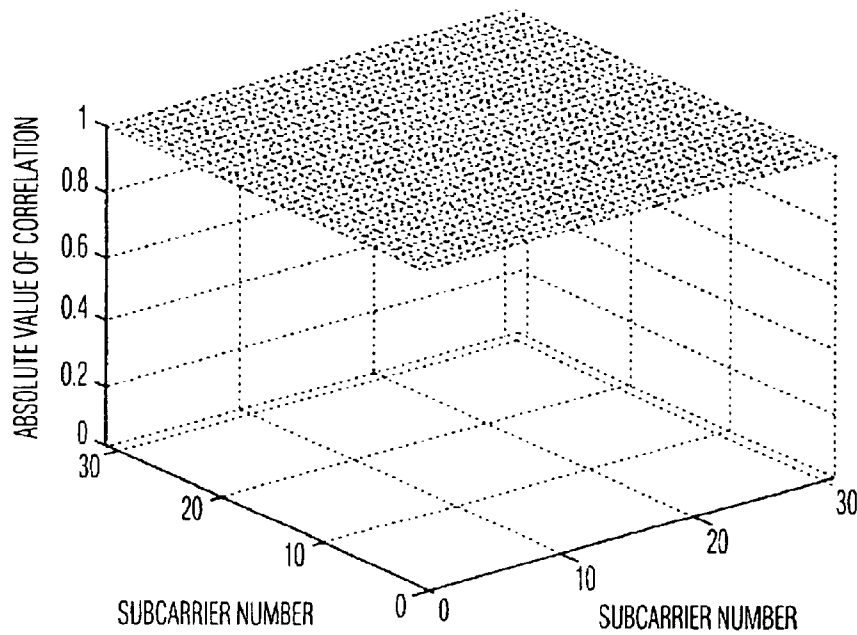


FIG. 6
(PRIOR ART)

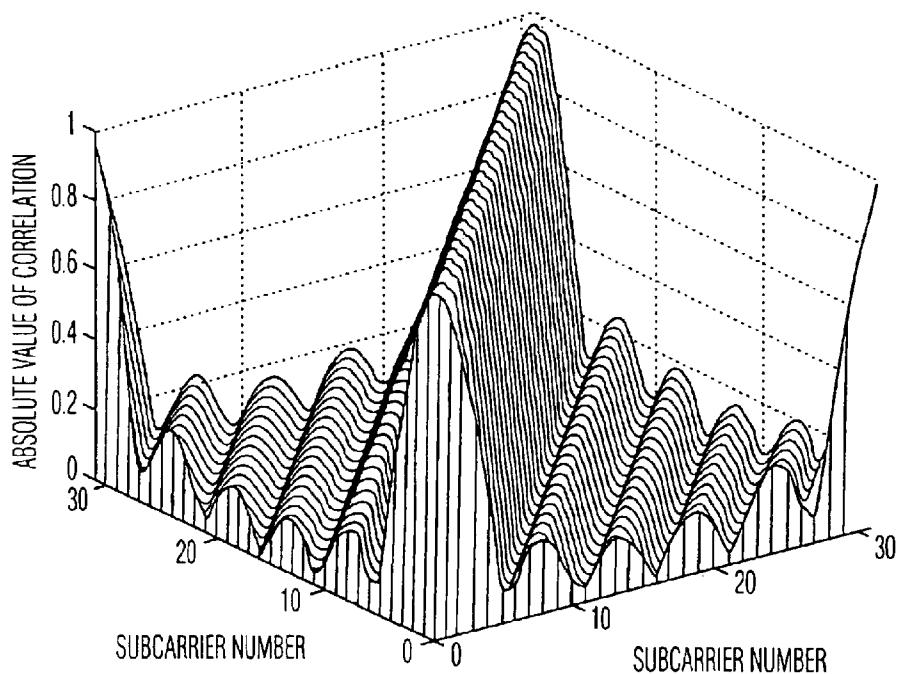


FIG. 7
(PRIOR ART)

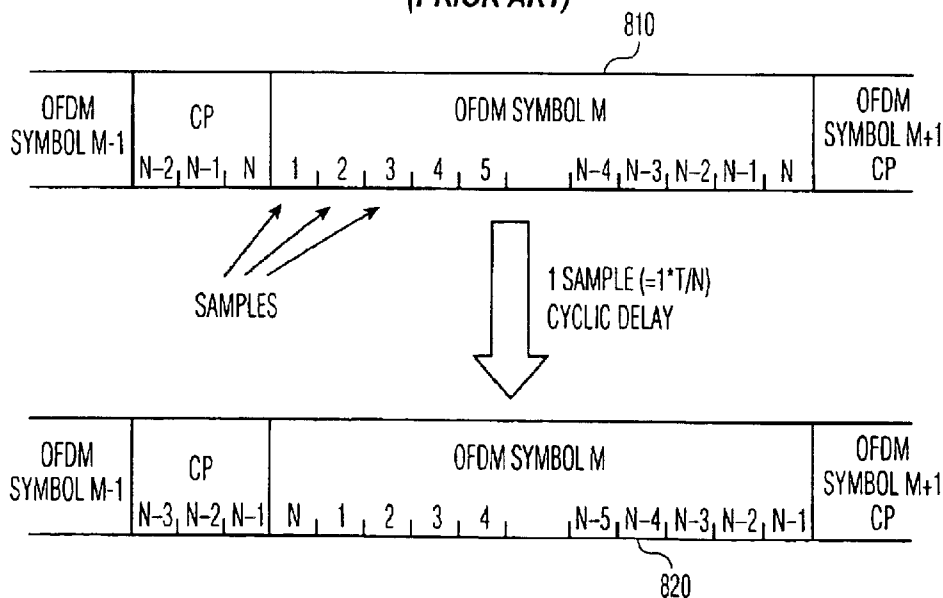


FIG. 8

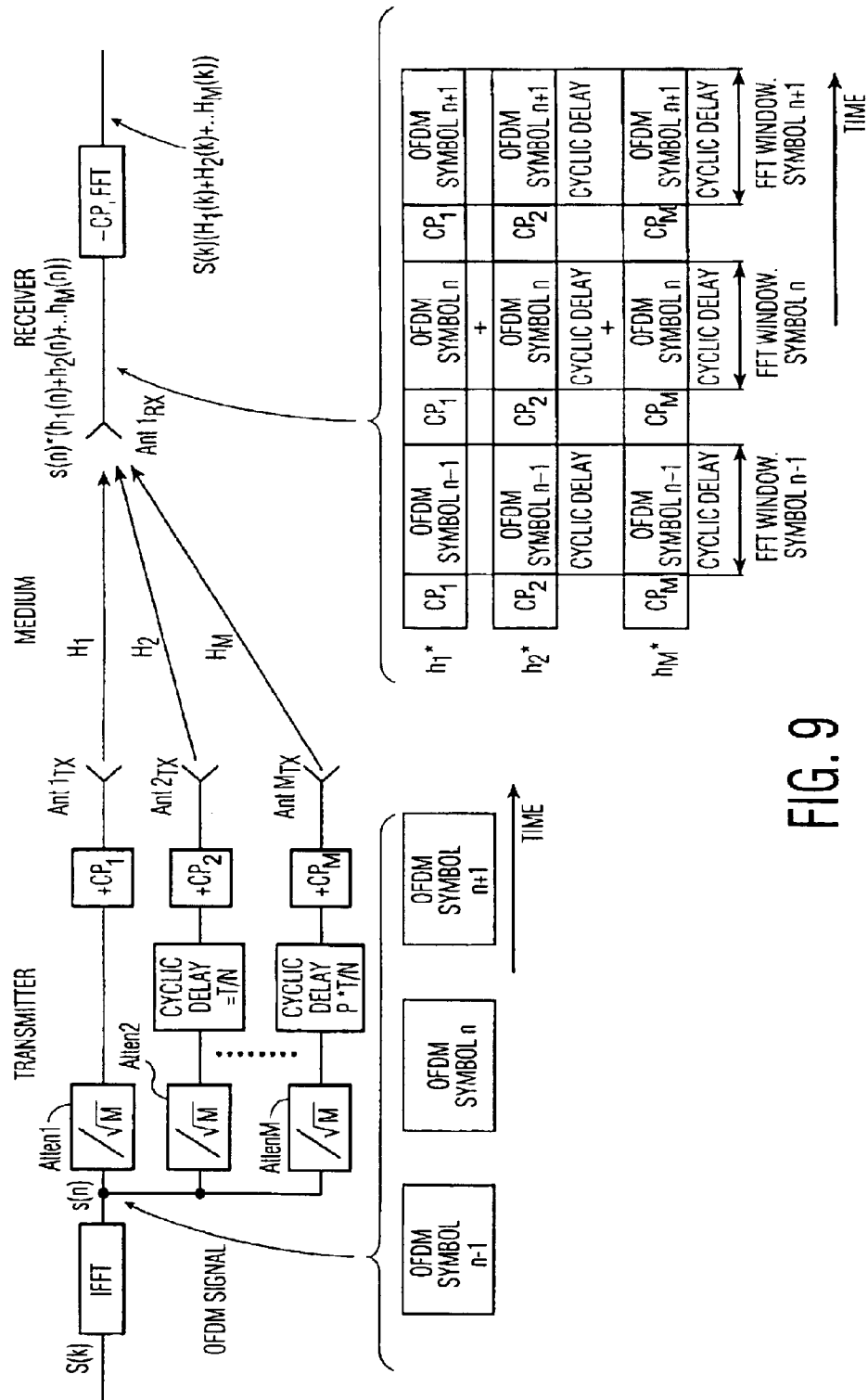


FIG. 9

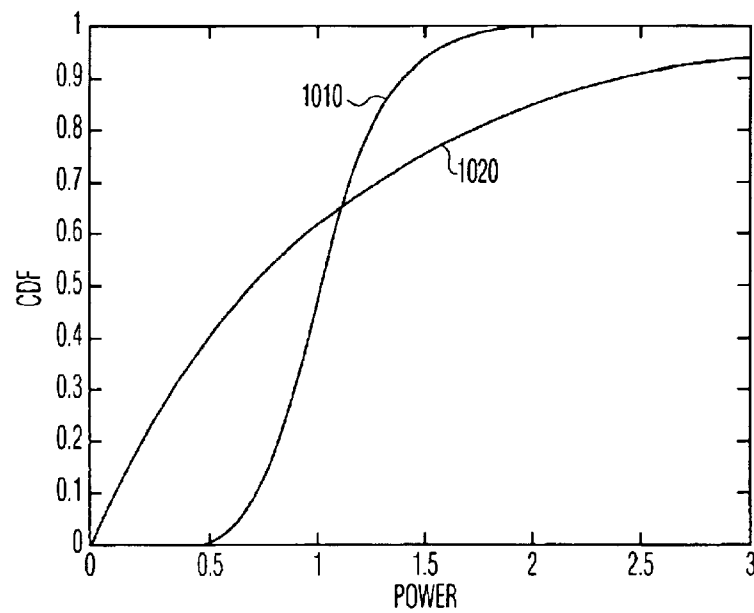


FIG. 10

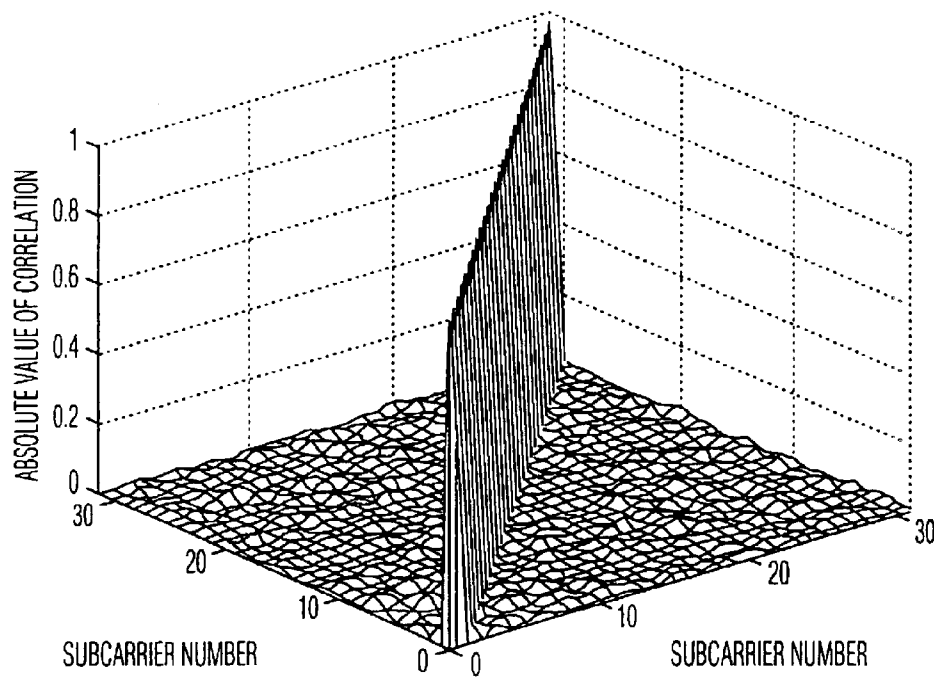


FIG. 11

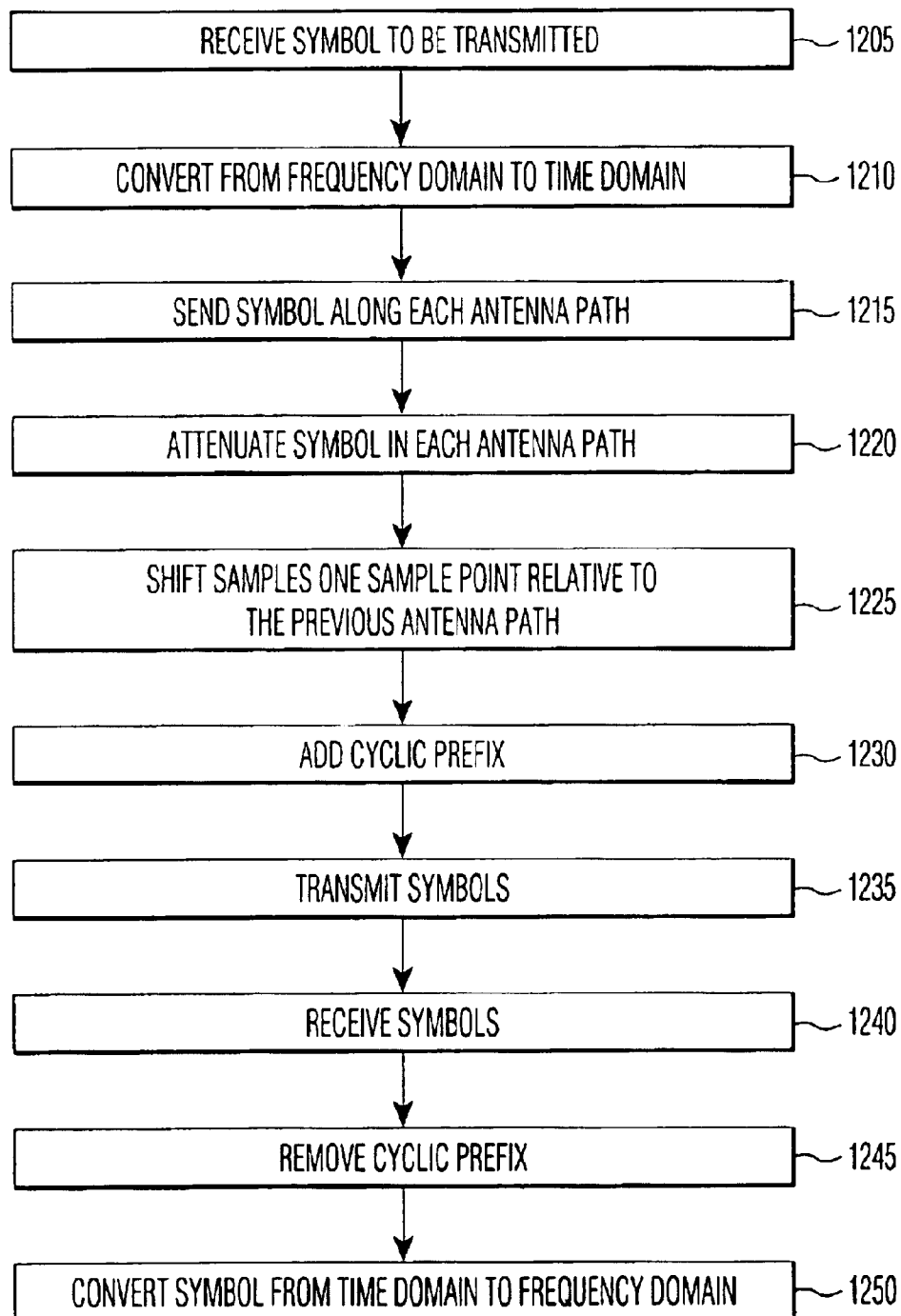


FIG. 12



FIG. 13A

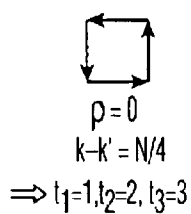


FIG. 13B

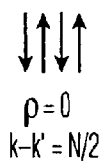


FIG. 13C

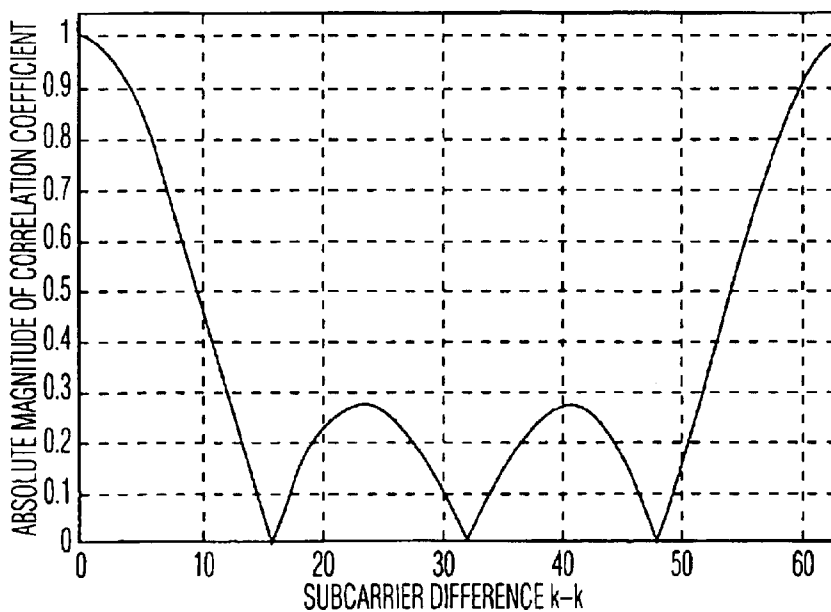


FIG. 14

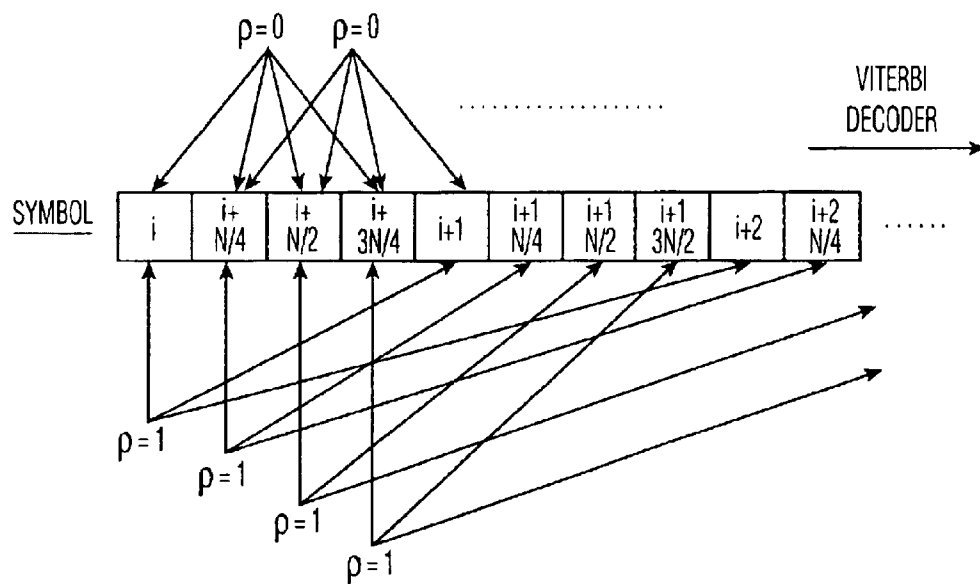


FIG. 15

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CYCLIC DELAY DIVERSITY FOR MITIGATING INTERSYMBOL INTERFERENCE IN OFDM SYSTEMS

BACKGROUND

The present invention relates to transmission diversity. More particularly, the present invention relates to mitigating intersymbol interference in systems which employ delay transmit diversity.

In radio transmissions, a transmitted signal may be deflected off buildings or other obstacles between a transmitter and a receiver. The deflection may cause a receiver to receive multiple versions of the transmitted signals with different time delays. The reception of a transmitted signal which is deflected off objects and the reception of multiple time delayed versions of the transmitted signal is known as multipath propagation. In digital transmissions, if the delay between the multiple paths exceeds the symbol duration, signal distortion known as intersymbol interference (ISI) is generated. Various transmission schemes are designed to mitigate ISI. One type of transmission scheme which is particularly suited for mitigating ISI is known as orthogonal frequency division multiplexing (OFDM). OFDM divides a bandwidth into a number of small subcarriers. Through the use of orthogonal functions, the spectrum of all subcarriers can mutually overlap, thus yielding optimum bandwidth efficiency. However, when the delay difference between multiple paths exceeds the minimum sampling interval the orthogonality between subcarriers is destroyed. To maintain the condition of perfect orthogonality between subcarriers in a multipath environment, a guard interval, or cyclic prefix (CP), is inserted before the transmission of each symbol.

FIG. 1 illustrates a conventional transmitter and receiver which operate according to OFDM. The transmitter takes a symbol $S(k)$ and performs an inverse fast Fourier transform (IFFT) to convert the symbol to be transmitted from the frequency domain into the time domain. The transmitter also adds a cyclic prefix (CP) to the symbol to be transmitted. The time domain symbol $s(n)$ is transmitted via antenna Ant 1_{TX} over a transmission medium, e.g., an air interface, to a receiver. The transmission medium convolves the transmitted symbol with the channel impulse response h_1 . The transmitted symbol is received via antenna Ant 1_{RX}. The symbol as received by the receiver can be represented in the time domain by $s(n)*h_1(n)$. The receiver then removes the cyclic prefix and performs a fast Fourier transform (FFT). The received symbol in the frequency domain can be represented by $S(k)H_1(k)$, wherein $S(k)$ is the received symbol in the frequency domain and $H_1(k)$ is the frequency representation of the channel, known as the channel transfer function.

FIG. 2 illustrates a conventional OFDM symbol M and associated cyclic prefix. OFDM symbol M, as represented in the time domain, contains sample points 1 through N. The cyclic prefix that is associated with OFDM symbol M contains sample points N+2 through N of OFDM symbol M. Since multipath delays can destroy the orthogonality of the transmitted symbol, the cyclic prefix is set to a number of sample points which is longer than the worst case multipath delay between the transmitter and the receiver. Accordingly, one skilled in the art will recognize that although the cyclic prefix illustrated in FIG. 2 contains only three sample points, N+2 through N, the number of actual sample points in a cyclic prefix will vary depending upon the worst case multipath delay.

Typically, transmitted signals in different frequencies are affected differently by the transmission medium. However, transmitted signals in different frequencies may be subject to

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flat Rayleigh fading, i.e., fading which occurs across the whole frequency domain. Further, when the delay difference between multiple paths is significantly shorter than a sample point duration the phase of the signals in the multiple paths may either add up in phase constructively or may cancel each other out. When the phase of the signals in the multiple paths cancel each other out, the quality of the received signal depends upon whether one strong direct signal is received or whether scattered signals from many directions with random phase are received. When multiple scattered signals from many directions with random phase are received with a delay spread significantly smaller than the sample point duration, flat Rayleigh fading is caused in the frequency domain. For example, a receiver may not be able to recover any of the subcarriers associated with a transmitted OFDM symbol which experiences flat Rayleigh fading. When the transmitted OFDM symbol is subject to flat Rayleigh fading, the quality of service (QOS) will be severely degraded. One method for providing a better quality of service in a flat Rayleigh fading environment is to use transmission diversity.

FIG. 3 illustrates a conventional transmitter and receiver which operate according to OFDM, wherein the transmitter transmits using transmission diversity. As illustrated in FIG. 3, transmission diversity is provided by employing a set of M of transmit antennas each of which transmit delayed versions of a symbol to be transmitted. One skilled in the art will recognize that transmission diversity is sometimes employed in a CDMA system, wherein independent delayed paths are resolved and then combined using, e.g., maximum ratio combining. When employing transmission diversity in an OFDM system, the transmit antennas should be positioned such that statistical independent channels are seen by the receiver. In other words, the transmitted symbol will be subject to individually independent flat Rayleigh fading channels. Employing a transmission diversity scheme, such as the one illustrated in FIG. 3, creates a coverage area where individual terminals experience a relatively uniform total received power without regard to position and time. Further, the transmission diversity scheme illustrated in FIG. 3 also creates pseudorandom frequency selectivity in the channel which also provides a more uniform receiving condition provided some type of coding is employed, i.e., forward error correction coding (FEC). One skilled in the art will recognize that word error rates, or OFDM symbol error rates, are lower for a FEC coded message in a fast uncorrelated Rayleigh fading channel than in a slow correlated Rayleigh fading channel. Accordingly, the delay based transmission diversity scheme illustrated in FIG. 3, is intended to introduce such uncorrelated frequency selectivity.

As illustrated in FIG. 3, the transmitter initially performs an inverse fast Fourier transform and then adds a cyclic prefix to a frequency domain symbol to be transmitted $S(k)$. The inverse fast Fourier transform converts the frequency domain symbol $S(k)$ into a time domain symbol $s(n)$. The time domain symbol $s(n)$ is sent along separate paths associated with each of the antennas. The time domain symbol $s(n)$ passes through attenuators, Atten1 through AttenM, which attenuates the power of the transmitted symbol in each antenna path by the square root of the number of antennas used in the transmission diversity scheme to normalize the overall transmitted power. Other than in the first antenna path, the attenuated time domain symbol to be transmitted is then subject to a linear delay. The linear delay in each path can be represented by the following formula:

$$p*(T/N) \text{ for } p \text{ from } 0 \text{ to } M-1$$

where p is in the range of 0 to M-1 wherein p is an index to the antenna under consideration, M represents the total number of antennas in the diversity

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system, T represents the time duration of the OFDM symbol without a cyclic prefix, and N represents the number of subcarriers present in the frequency domain. The symbols transmitted from antennas Ant 1_{TX} through Ant M_{TX} are respectively subjected to channel transfer functions H₁ through H_M of the transmission medium. At the receiver the symbols from the antennas Ant 1_{TX} through Ant M_{TX} are received by antenna Ant 1_{RX} and combined together. As illustrated in FIG. 3, after being combined in the receiver, the resultant symbol can be represented in the time domain by s(n)*(h₁(n)+h₂(n)+...+h_M(n)). The receiver then removes the cyclic prefix and performs a fast Fourier transform to convert the time domain symbol into a frequency domain symbol.

FIG. 4 illustrates in more detail three symbols respectively transmitted from three antennas with different delays. At the receiver a fast Fourier transform is performed during a set period of time known as a fast Fourier transform window. As illustrated in FIG. 4, by using a cyclic prefix the fast Fourier transform window is performed over all the sample points of the transmitted OFDM symbol n of each of the delayed versions of the transmitted symbols.

In the frequency domain, the received symbol can be represented by:

$$R(k) = \frac{S(k)}{\sqrt{M}} \cdot \sum_{i=1}^M H_i(k) = S(k) \cdot H(k)$$

wherein S(k) is the sent symbol, M is the number of antennas and H(k) is the composite frequency response of the channel where the square root factor of M is included. Thus, the standard deviation of H(k) remains constant.

The received power according to Parsevals (DFT) theorem is:

$$P = \frac{1}{N} \sum_{k=0}^{N-1} R(k) \cdot R(k)^* = \frac{1}{N} \sum_{k=0}^{N-1} |h(k)|^2 |S(k)|^2$$

where R(k) is a frequency domain representation of the received symbol and R(k)* is the complex conjugate of R(k). Assuming that S(k) uses multilevel constellations, e.g., 16 QAM or 64 QAM, for each k, the average power level per subcarrier is:

$$P = E \left(\frac{1}{N} \sum_{k=0}^{N-1} |H(k)|^2 |S(k)|^2 \right) = \frac{\sigma_s^2}{N} \sum_{k=0}^{N-1} |H(k)|^2$$

wherein E represents the expected value.

If it is assumed that transmission diversity system employs two antennas, wherein each antenna transmits over a path which is affected by a complex Gaussian attenuation variable H_r, i.e., a flat Rayleigh fading channel, and that the second diversity path is delayed by, e.g., one OFDM sampling point, the resulting transfer function then becomes:

$$H(k) = H_0 + H_1 \cdot e^{-j \frac{2\pi k}{N}}$$

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Solving now for the received power results in the following:

$$\begin{aligned} P &= \frac{\sigma_s^2}{N} \sum_{k=0}^{N-1} |H_0|^2 + |H_1|^2 + 2 \cdot |H_0| \cdot |H_1| \cos(\arg(H_0) - \arg(H_1)) \\ &= \frac{\sigma_s^2}{N} \left(N \cdot |H_0|^2 + N \cdot |H_1|^2 + 2 \cdot |H_0| \cdot |H_1| \cdot \sum_{k=0}^{N-1} \cos\left(\frac{-2 \cdot \pi \cdot k}{N}\right) \right) \\ &= \sigma_s^2 (|H_0|^2 + |H_1|^2) \\ &= \sigma_s^2 (H_{re0}^2 + H_{im0}^2 + H_{re1}^2 + H_{im1}^2) \end{aligned}$$

where H_{re} represents the real portion of the complex valued H and H_{im} represents the imaginary portion of the complex valued H.

As seen above, the received power is a centrally distributed chi-square variable of degree four. If, however, there was no delay between the two transmitted symbols H₀ and H₁, the symbols can be merged together as H' before power summation over all subcarriers. The net result is then a chi-square variable of degree two, i.e., Rayleigh distributed. Although the example given above relates to a system employing two antennas, one skilled in the art will recognize that the degree n of the chi-square variable is equal to two times the number of antennas with different delays, i.e., n=2M.

The average value and standard deviation of a chi-square variable is:

$$E(P) = n\sigma^2, \text{ and } \sigma_P = \sqrt{2n} \cdot \sigma^2,$$

where σ is the standard deviation of each Gaussian distributed variable that compose the chi-square distributed variable.

It should be noted that the relative spread, i.e., the stochastic deviation around the mean value of the power P, is reduced when the degree n is increased as:

$$\sigma_P / E(P) = \sqrt{2/n}$$

FIG. 5 illustrates the power carrier distribution function (CDF) for M=2 antennas. Curve 505 illustrates the power carrier distribution function for two antennas with different delays, while curve 510 illustrates power carrier distribution function for transmission on two antennas with no delay. As can be seen from FIG. 5, using different delays for each antenna results in a steeper carrier distribution function curve. It will be recognized that carrier distribution function which is a vertical line indicates that there are no variations around the mean value, and hence, the symbol is deterministic, i.e., non-random. Accordingly, a steeper curve indicates that the overall power level is more deterministic.

FIG. 6 illustrates the subcarrier covariance matrix for transmission over six antennas without any delay of the symbol transmitted over the six antennas. As can be seen from FIG. 6, each subcarrier channel is correlated with all the other subcarrier channels when the antennas transmit the same symbol without a delay difference between the antennas. If the transmission channel subjects the transmitted symbol to a flat Rayleigh fading, the transmitted symbol of the six antennas will be similarly affected by the channel transfer function.

FIG. 7 illustrates the subcarrier covariance matrix for the transmission of a symbol over six antennas with six different delays assuming a flat Rayleigh fading channel. As can be seen from FIG. 7, the subcarriers have a low value of correlation, i.e., most subcarriers have an absolute correlation value of less than 0.2. Accordingly, if the transmission medium subjected the symbols transmitted by the six antennas to a flat Rayleigh channel, most subcarriers would be affected differently by the channel.

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Although the transmission of OFDM symbols using a plurality of antennas each with a different delay helps prevent the symbol being transmitted from being corrupted by flat Rayleigh fading, the total delay spread between all of the antenna paths can be no more than the duration of the cyclic prefix minus the duration of the inherent channel delay spread. It will be recognized that the delay spread is a measure of how distributed the different delays are with respect to each other. Introducing a greater delay would result in intersymbol interference, and subsequently the subcarriers would lose their mutual orthogonality. Accordingly, since the longer the cyclic prefix the less usable bandwidth is available for transmission of data, cyclic prefixes are typically kept as short as possible.

Accordingly, it would be desirable to provide a transmission diversity scheme using OFDM which is not limited by the duration of the cyclic prefix minus the duration of the inherent channel delay spread.

SUMMARY

These and other problems, drawbacks and limitations of conventional techniques are overcome according to the present invention by a method and/or an apparatus for transmitting a symbol, wherein the symbol is split among a plurality of antenna paths. In each antenna path the samples of the symbol are cyclically shifted a predetermined number of positions. The predetermined number of positions depends upon the relation of a particular antenna path with respect to the other antenna paths. Samples which are shifted out of the end of the symbol are inserted into the beginning of the symbol. Thereafter a cyclic prefix is formed by copying a predetermined number of samples from the end of the symbol.

In accordance with one embodiment of the present invention a signal is split along a plurality of antenna paths, wherein the signal includes a number of positions, each of the number of positions including a sample. The signal is received in an antenna path. The samples of the signal are shifted a predetermined number of positions, wherein samples shifted beyond the number of positions in the signal are shifted into a number of positions at a beginning or the end of the signal. A number of samples from an end of the signal in a guard interval and the signal and the guard interval are transmitted.

BRIEF DESCRIPTION OF THE DRAWINGS

The objects and advantages of the invention will be understood by reading the following detailed description in conjunction with the drawings in which:

FIG. 1 illustrates a conventional transmitter and receiver employing a OFDM transmission scheme;

FIG. 2 illustrates a conventional OFDM symbol and associated cyclic prefix;

FIG. 3 illustrates a conventional transmitter and receiver which operate according to a OFDM transmission scheme using transmission diversity;

FIG. 4 illustrates a plurality of conventional OFDM symbols which are received by a receiver in a system which employs transmission diversity using linear delay;

FIG. 5 illustrates a power carrier distribution function for transmission using two antennas;

FIG. 6 illustrates a subcarrier covariance matrix for a system employing transmission diversity without delays between the various antennas;

FIG. 7 illustrates a subcarrier covariance matrix for a transmission diversity scheme with delays between the symbols transmitted over each antenna;

FIG. 8 illustrates two OFDM symbols wherein there is a cyclic delay between the two symbols in accordance with exemplary embodiments of the present invention;

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FIG. 9 illustrates a transmitter and receiver employing transmission diversity and cyclic delay in accordance with exemplary embodiments of the present invention;

FIG. 10 illustrates a power carrier distribution function for the transmission over a plurality of antennas in accordance with an exemplary embodiment of the present invention;

FIG. 11 illustrates a subcarrier covariance matrix for a transmission diversity scheme employing cyclic delay in accordance with an exemplary embodiment of the present invention;

FIG. 12 illustrates an exemplary method for employing cyclic delay in accordance with the present invention;

FIGS. 13A–13C illustrate the subcarrier channel correlation between subcarriers in accordance with an exemplary embodiment of the present invention;

FIG. 14 illustrates the absolute magnitude of correlation between two subcarriers in a system transmitting 64 subcarriers in accordance with an exemplary embodiment of the present invention; and

FIG. 15 illustrates the input stream to a convolutional FEC decoder in the receiver in accordance with an exemplary embodiment of the present invention.

DETAILED DESCRIPTION

The present invention is directed to transmission diversity, and more specifically to mitigating ISI by employing a cyclic delay in a transmission diversity system.

In the following, the present invention is described as being implemented in a system which communicates according to the OFDM protocol. However, one skilled in the art will recognize that the present invention is equally applicable to other protocols which employ cyclic prefixes or guard intervals. Further, although exemplary embodiments of the present invention are described below as employing a specific number of antennas, the present invention is equally applicable to systems with more antennas or less antennas than those described below.

FIG. 8 illustrates two OFDM symbols wherein a cyclic delay is implemented between the two symbols being transmitted in a transmission diversity scheme. Assume that OFDM symbol M 810 is transmitted over the antenna that has no cyclic delay and that OFDM symbol M 820 is transmitted over an antenna which has a cyclic delay of one sample. As can be seen by comparing OFDM symbols 810 and 820, the cyclic delay is implemented by shifting samples from the end of the OFDM symbol into the beginning of the OFDM symbol and adding a cyclic prefix by copying the last n samples of the OFDM symbol. For example, if a cyclic delay of three samples were implemented, the OFDM symbol transmitted over the third antenna would have the last three samples of the OFDM symbol shifted into the first three slots of the OFDM symbol and the remaining samples in the OFDM symbol would be shifted three places to the right. Then the last n samples of the OFDM symbol are copied and placed in the cyclic prefix, wherein n represents the number of samples in the cyclic prefix for a particular system.

FIG. 9 illustrates a transmitter and receiver which operate according to a OFDM transmission scheme employing transmission diversity. The transmitter performs an inverse fast Fourier transform on a frequency domain symbol $S(k)$ to convert the symbol to the time domain symbol $s(n)$. The time domain symbol $s(n)$ is then passed through each antenna path of the diversity system. In each antenna path the time domain symbol $s(n)$ is passed through an attenuator which preferably attenuates each symbol by a factor of the square root of the number of antennas being used to transmit

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to normalize the power. One skilled in the art will recognize that other weighting factors can be implemented using, for example, power amplifiers. When the FEC code and the interleaver design are fixed optimum performance of the system can be achieved by selecting both the cyclic delay as well as the weighting factors.

After the signal has been attenuated, the first antenna path adds the cyclic prefix and transmits the symbol from the antenna. Each subsequent antenna path performs the cyclic delay on the symbol and then adds the cyclic prefix to the symbol to be transmitted. The symbol is then transmitted through the respective antennas. As the symbols pass through the transmission medium, they are each subjected to the respective channel transfer functions H_1 through H_M .

The receiver receives each of the symbols being transmitted from the antennas as a combined symbol and reconstructs the transmitted OFDM symbol. Accordingly, in the time domain the receiver has a symbol which comprises the transmitted symbol $s(n)$ which is combined with a sum of the channel transfer function caused by the transmission medium $h_1(n)$ through $h_M(n)$. The receiver then removes the cyclic prefix and performs a fast Fourier transform to convert the symbol from the time domain into the frequency domain. By performing the fast Fourier transform the cyclic delay is converted into a phase factor. One skilled in the art will recognize that subsequent equalization of the received symbol removes the phase factor.

Comparing FIG. 3 and FIG. 9, wherein FIG. 3 illustrates a linear delay for a transmit diversity scheme and FIG. 9 illustrates a cyclic delay for a transmit diversity scheme, it can be seen that the cyclic delay is not limited by the size of the cyclic prefix. Accordingly, where a system which employs a linear delay is limited to using a number of antennas which correspond with the number of samples in the cyclic prefix, a system which uses a cyclic delay is only limited to using a number of antennas equal to the number of samples in the OFDM symbol. Further, by using a cyclic delay, intersymbol interference is not generated, and hence, the orthogonality between the subcarriers remains intact.

FIG. 10 illustrates the power carrier density function for diversity transmission using M antennas. Curve 1010 illustrates the power carrier density function for the transmission using a cyclic delay of 16, i.e., a transmission diversity employing 16 antennas and 15 different cyclic delays. Curve 1020 illustrates the power carrier density function for a transmission employing 16 antennas and no delay. As illustrated in FIG. 10, the implementation of a cyclic delay results in a steeper curve which indicates that the overall power level is more deterministic, i.e., non-random.

FIG. 11 illustrates the subcarrier covariance matrix for a transmission diversity system which employs 32 cyclic delays. As illustrated in FIG. 11, all of the subcarriers are uncorrelated with each other. Since each subcarrier channel transfer function is made up of a summation of complex Gaussian variables, the resulting subcarrier channel will have the same statistics, but any other subcarrier will be independently fading, i.e., each subcarrier reacts independently to the fast Rayleigh fading.

FIG. 12 illustrates an exemplary method for employing cyclic delay in accordance with the present invention. The transmitter receives the symbol to be transmitted (step 1205). The symbol is converted from the frequency domain to the time domain by performing an inverse fast Fourier transform (step 1210). The time domain symbol is sent along each antenna path (step 1215). In each antenna path the symbol is attenuated by the square root of the number of antennas (step 1220). In each antenna path the samples are shifted one sample point, relative to the previous antenna path, to the right in the OFDM symbol (step 1225). For example, in the first antenna path the samples are not shifted,

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while in the sixth antenna path the samples are shifted five spaces. In each antenna path after the samples have been shifted, a cyclic prefix is added (step 1230). The cyclic prefix added in each antenna path includes the last n samples of the end of the OFDM symbol. The transmitter then transmits the symbols from the various antennas (step 1235). The receiver receives the combined symbols (step 1240) and removes the cyclic prefix (step 1245). The received symbol is then converted from the time domain to the frequency domain using a fast Fourier transform (step 1250).

It will be recognized that to reduce the effects of channel impairments on a transmitted signal forward error correction (FEC) coding and interleaving can be performed on the transmitted signal. To understand how coding and interleaving can be performed in accordance with the present invention, the correlation between subcarriers should be examined. Accordingly, the correlation between subcarrier k and k' when implementing a transmit delay diversity method using two transmit antennas, can be illustrated by the equation below:

$$\begin{aligned}\rho(k, k') &= E\left\{\left(H_1 + H_2 \cdot e^{-\frac{i2\pi kt}{N}}\right) \cdot \left(H_1 + H_2 \cdot e^{-\frac{i2\pi k't}{N}}\right)^*\right\} \\ \rho(k, k') &= E\left\{|H_1|^2 + |H_2|^2 \cdot e^{-\frac{i2\pi(k-k')t}{N}} + \right. \\ &\quad \left. H_1 \cdot H_2^* \cdot e^{\frac{i2\pi k't}{N}} + H_1^* \cdot H_2 \cdot e^{-\frac{i2\pi kt}{N}}\right\} \\ \rho(k, k') &= \sigma_1^2 + \sigma_2^2 \cdot e^{-\frac{i2\pi(k-k')t}{N}}\end{aligned}$$

wherein k and k' are the subcarrier indexes, t is a fixed cyclic delay, H_1 and H_2 represent the channel impairments for each subcarrier, N is the total number of subcarriers, σ is the standard deviation and E is the expectation value (i.e., the average over all possible channel realizations). One skilled in the art will recognize that the correlation illustrated above is not normalized for the number of antennas. For multiple antennas the correlation between subcarriers k and k' can be represented by the equation below:

$$\rho(k, k') = \sigma_1^2 + \sigma_2^2 \cdot e^{-\frac{i2\pi(k-k')t_1}{N}} + \sigma_3^2 \cdot e^{-\frac{i2\pi(k-k')t_2}{N}} + \dots$$

One skilled in the art will recognize that the correlation described by the formula above is similar to the frequency response of a finite impulse response (FIR) digital filter with all weights identically set. Apart from various cyclic delays, other weights can be employed for each antenna. Accordingly, the desired characteristic of $\rho(k, k')$ can be designed in a similar fashion to the manner in which an FIR digital filter is designed, e.g., using a digital filter design software package.

When transmitting it would be desirable to have a stream of symbols where adjacent symbols are uncorrelated which improves the FEC decoding process and so that the channel transfer function and impairments should affect the subcarriers differently. To determine uncorrelated subcarriers, the following formula could be used:

$$\rho(k, k') = \frac{1}{M} \left(1 + e^{-\frac{i2\pi(k-k')t_1}{N}} + e^{-\frac{i2\pi(k-k')t_2}{N}} + \dots \right)$$

In the formula above each antenna uses an amplitude weight of 1 so that the correlation value is normalized with respect to the number of antenna used.

FIGS. 13A–13C illustrate the subcarrier channel correlation between subcarriers k and k' in a transmit diversity

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system which employs four antennas. Each arrow illustrated in FIGS. 13A–13C represents an output of one of the four antennas in the subcarrier correlation between subcarriers k and k' . As can be seen from FIGS. 13B and 13C, the cyclic delays t_1 , t_2 and t_3 are chosen such that subcarriers separated with $k-k'=N/4$ and $k-k'=N/2$ have a zero correlation. Furthermore, as illustrated by FIG. 13A, when $k-k'=0$ the subcarriers are completely correlated. Although FIGS. 13A–13C illustrate a system which employs four antennas, it will be recognized that the approach described above in connection with FIGS. 13A–13C can be implemented with an arbitrary number of antennas.

FIG. 14 illustrates the correlation characteristic for all subcarrier differences using the same cyclic delays selected above in connection with FIGS. 13A–13C for $N=64$ subcarriers. It will be recognized that FIG. 14 shows a more comprehensive picture of the subcarrier correlations compared to FIGS. 13A–13C. Based upon the subcarrier correlation characteristic illustrated in FIGS. 13A–13C and FIG. 14, it will be recognized that the convolutional code applied to the transmitted signal should be preceded by an interleaver which provides symbols from subcarrier i , $i+N/4$, $i+N/2$, $i+3N/4$, $i+1$, $i+1+N/4$, $i+1+N/2$, $i+1+3N/4$, $i+2$, $i+2+N/4$, $i+2+N/2$, $i+2+3N/4$, $i+3$, $i+3+N/4$, $i+3+N/2$, $i+3+3N/4$, $i+4$, $i+4+N/4$, $i+4+N/2$, $i+4+3N/4$, $i+5$, $i+5+N/4$, $i+5+N/2$, $i+5+3N/4$, $i+6$, $i+6+N/4$, $i+6+N/2$, $i+6+3N/4$, $i+7$, $i+7+N/4$, $i+7+N/2$, $i+7+3N/4$, $i+8$, $i+8+N/4$, $i+8+N/2$, $i+8+3N/4$, $i+9$, $i+9+N/4$, $i+9+N/2$, $i+9+3N/4$, $i+10$, $i+10+N/4$, $i+10+N/2$, $i+10+3N/4$, $i+11$, $i+11+N/4$, $i+11+N/2$, $i+11+3N/4$, $i+12$, $i+12+N/4$, $i+12+N/2$, $i+12+3N/4$, $i+13$, $i+13+N/4$, $i+13+N/2$, $i+13+3N/4$, $i+14$, $i+14+N/4$, $i+14+N/2$, $i+14+3N/4$, $i+15$, $i+15+N/4$, $i+15+N/2$, $i+15+3N/4$, $i+16$, $i+16+N/4$, $i+16+N/2$, $i+16+3N/4$, $i+17$, $i+17+N/4$, 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receiving the signal in each of the plurality of antenna paths;

for each antenna path, shifting the samples of the signal a predetermined direction and number of positions, wherein the predetermined direction and/or number of positions predetermined of position are different for at least two of the antenna paths, and the predetermined number of positions corresponds to whether the signal is being retransmitted, said shifting step including:

- when shifting samples toward the end of the signal, shifting samples that are shifted beyond the number of positions in the signal into a corresponding number of positions at a beginning of the signal; and
- when shifting samples toward the beginning of the signal, shifting samples that are shifted beyond the number of positions in the signal into a corresponding number of positions at the end of the signal;

in each antenna path, including a number of samples from the beginning or the end of the signal in a cyclic prefix; and

transmitting the signal and the cyclic prefix from each of the plurality of antenna paths.

4. The method of claim 1, wherein the signal is an orthogonal frequency division multiplexed symbol.

5. The method of claim 1, further comprising the steps of:

- applying error protection coding to the signal;
- interleaving the samples, wherein the samples are interleaved such that after de-interleaving, subcarriers with a lowest correlation are placed in positions next to each other;

performing an inverse fast Fourier transform on the interleaved coded symbols to form a resultant signal; and

providing the resultant signal to each of the antenna paths.

6. The method of claim 1, further comprising the steps of:

- performing an inverse fast Fourier transform on the signal; and
- attenuating the signal in each antenna path.

7. An apparatus for transmitting signals comprising:

- an input for receiving a signal to be transmitted, wherein the signal to be transmitted includes a number of positions, each of the number of positions including a sample;
- a first antenna path;
- a second antenna path, wherein the second antenna path shifts the samples of the signal a predetermined number of positions, wherein samples shifted beyond the number of positions in the signal are shifted the predetermined number of positions into a beginning or an end of the signal;
- a transmitter for transmitting the signal from the first antenna path and the shifted signal from the second antenna path in a first transmission attempt; and
- means for determining whether the signal needs to be retransmitted due to fading of the first transmission attempt;

wherein, in response to a determination the signal needs to be retransmitted the second antenna path shifts the sample of the signal a different number of positions than were utilized in the first transmission attempt, and the transmitter retransmits the signal from the first antenna path and the differently shifted signal from the second antenna path in a second transmission attempt.

8. The apparatus of claim 7, further comprising:

- a third antenna path, wherein the third antenna path shifts the samples of the signal another predetermined number of positions,

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wherein samples shifted beyond the number of positions in the signal are shifted the another predetermined number of positions into a beginning or an end of the signal.

9. The apparatus of claim 8, wherein the predetermined number of positions corresponds to a position of the second antenna path with respect to the first and third antenna paths and the another predetermined number of positions corresponds to a position of the third antenna path with respect to the first and second antenna paths.

10. The apparatus of claim 7, wherein the samples are shifted toward the end of the signal and wherein samples shifted beyond the end of the signal are shifted into the beginning of the signal.

11. The apparatus of claim 7, wherein the samples are shifted toward the beginning of the signal and wherein samples shifted beyond the beginning of the signal are shifted into the end of the signal.

12. The apparatus of claim 7, further comprising:

- means for applying an error correction code to signal; and
- an interleaver.

13. The apparatus of claim 7, wherein the first and second antenna paths include means for adding a guard interval to the signal in the respective antenna path prior to transmission of the signal from each antenna path.

14. The apparatus of claim 13, wherein the guard interval is added to the beginning of the signal.

15. The apparatus of claim 13, wherein the guard interval is added to the end of the signal.

16. A radio communication system comprising:

- a transmission portion including:

- an input for receiving a signal to be transmitted, wherein the signal to be transmitted includes a number of positions, each of the number of positions including a sample;

- a first antenna path;

- a second antenna path, wherein the second antenna path shifts the samples of the signal a predetermined number of positions, wherein samples shifted beyond the number of positions in the signal are shifted the predetermined number of positions into a beginning or an end of the signal; and

- a transmitter for transmitting the signal from the first antenna path and the shifted signal from the second antenna path in a first transmission attempt; and

- a receiving portion including:

- a receiver that includes a first and second antenna path, wherein the receiver enhances signal quality by combining signals received on the first and second antenna paths;

- means for reporting to the transmission portion whether the signal needs to be transmitted due to fading of the first transmission attempt;

wherein, in response to receiving a report that the signal needs to be retransmitted, the second antenna path shifts the samples of the signal a different number of positions than were utilized in the first transmission attempt, and the transmitter retransmits the signal from the first antenna path and the differently shifted signal from the second antenna path in a second transmission attempt.

17. The system of claim 16, wherein the samples are shifted toward the end of the signal and wherein samples shifted beyond the end of the signal are shifted into the beginning of the signal.

18. The system of claim 16, wherein the samples are shifted toward the beginning of the signal and wherein samples shifted beyond the beginning of the signal are shifted into the end of the signal.

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19. The system of claim 16, wherein
the transmitter further includes
means for performing an inverse fast Fourier transform;
and
means for adding a prefix to the signal in each antenna path; and
the receiver further includes
means for removing the prefix; and
means for performing a fast Fourier transform.

20. The system of claim 16 wherein
the transmitter further includes
means for applying error protection coding to the signal
to form coded symbols; and

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means for interleaving the coded symbols;
the receiver further includes
means for removing de-interleaving received subcarriers; and
means for decoding the de-interleaved subcarriers,
wherein the coded symbols are interleaved such that after de-interleaving, subcarriers with a lowest correlation are placed in positions next to each other.

21. The system of claim **16**, wherein the signal quality enhancing combining is a maximum ratio combining.

* * * * *

UNITED STATES PATENT AND TRADEMARK OFFICE
CERTIFICATE OF CORRECTION

PATENT NO. : 6,842,487 B1
APPLICATION NO. : 09/667504
DATED : January 11, 2005
INVENTOR(S) : Larsson

Page 1 of 1

It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

In Column 3 Line 54, insert -- where $\sigma_s^2 = E(|S(k)|^2)$ -- before paragraph “wherein E ...value.”.

In Column 4, Line 11, delete “ $\sigma_s^2(H_{re0}^2 + H_{im0}^2 + H_{re1}^2 + H_{im1}^2)$ ”

and insert -- $\sigma_s^2(H_{re0}^2 + H_{im0}^2 + H_{re1}^2 + H_{im1}^2)$ -- therefor.

In Column 10, Line 34, in Claim 1, delete “sampler” and insert -- samples --, therefor.

In Column 11, Line 6, in Claim 3, after “positions” delete “predetermined of position”.

In Column 11, Line 57, in Claim 7, after “determination” insert -- that --.

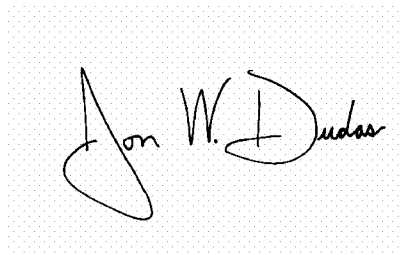
In Column 11, Line 59, in Claim 7, delete “sample” and insert -- samples --, therefor.

In Column 12, Line 42, in Claim 16, delete “shitted” and insert -- shifted --, therefor.

In Column 12, Line 50, in Claim 16, delete “transmitted” and insert -- retransmitted --, therefor.

Signed and Sealed this

Thirtieth Day of October, 2007

A handwritten signature in black ink on a light gray dotted background. The signature is written in a cursive style and appears to read "Jon W. Dudas".

JON W. DUDAS

Director of the United States Patent and Trademark Office

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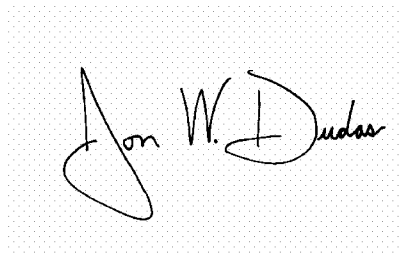
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Signed and Sealed this

Twenty-seventh Day of November, 2007

A handwritten signature in black ink on a light gray dotted background. The signature is written in a cursive style and reads "Jon W. Dudas".

JON W. DUDAS

Director of the United States Patent and Trademark Office