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(54) **CELL SPECIFIC SOUNDING REFERENCE
SIGNAL SUB-FRAME CONFIGURATION**

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(57) **ABSTRACT**

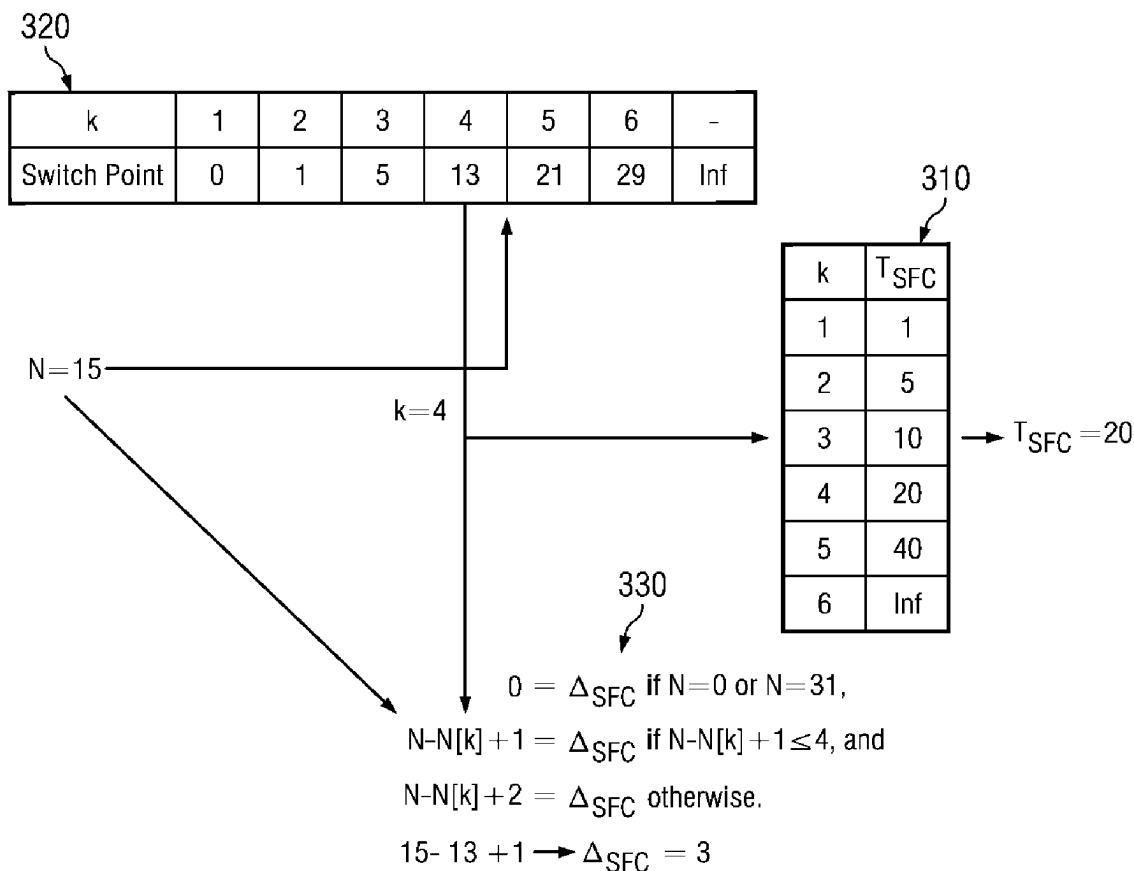
(21) Appl. No.: **12/432,031**

A method of wireless communication including a plurality of fixed base stations and a plurality of mobile user equipment with each base station transmitting to any user equipment within a corresponding cell a sounding reference signal sub-frame configuration indicating sub-frames when sounding is permitted. Each user equipment recognizes the sounding reference signal sub-frame configuration and sounds only at permitted sub-frames. Differing cells may have differing sounding reference signal sub-frame configurations. There are numerous manners to encode the transmitted information.

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Related U.S. Application Data

(60) Provisional application No. 61/051,482, filed on May 8, 2008, provisional application No. 61/051,453, filed



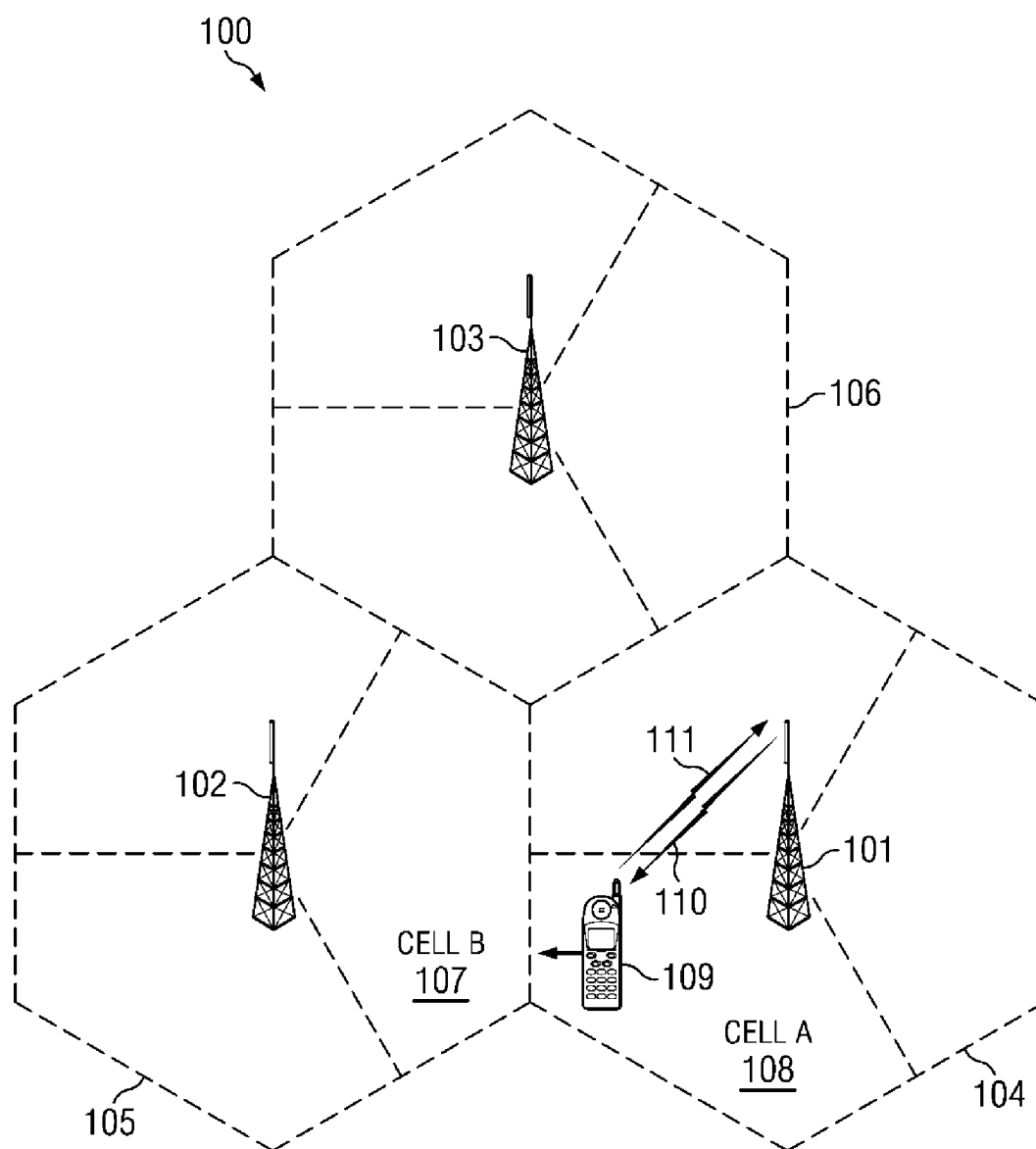


FIG. 1
(PRIOR ART)

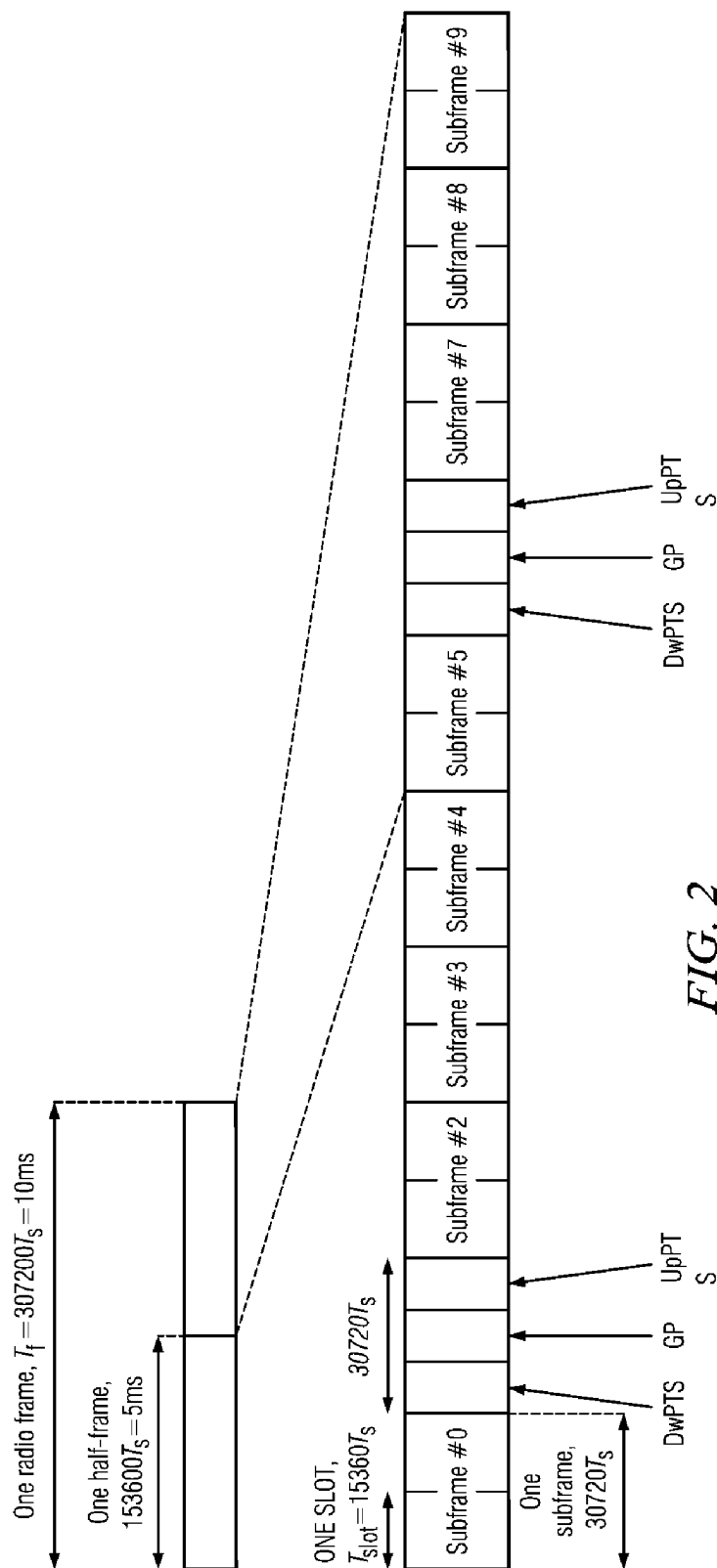


FIG. 2
(PRIOR ART)

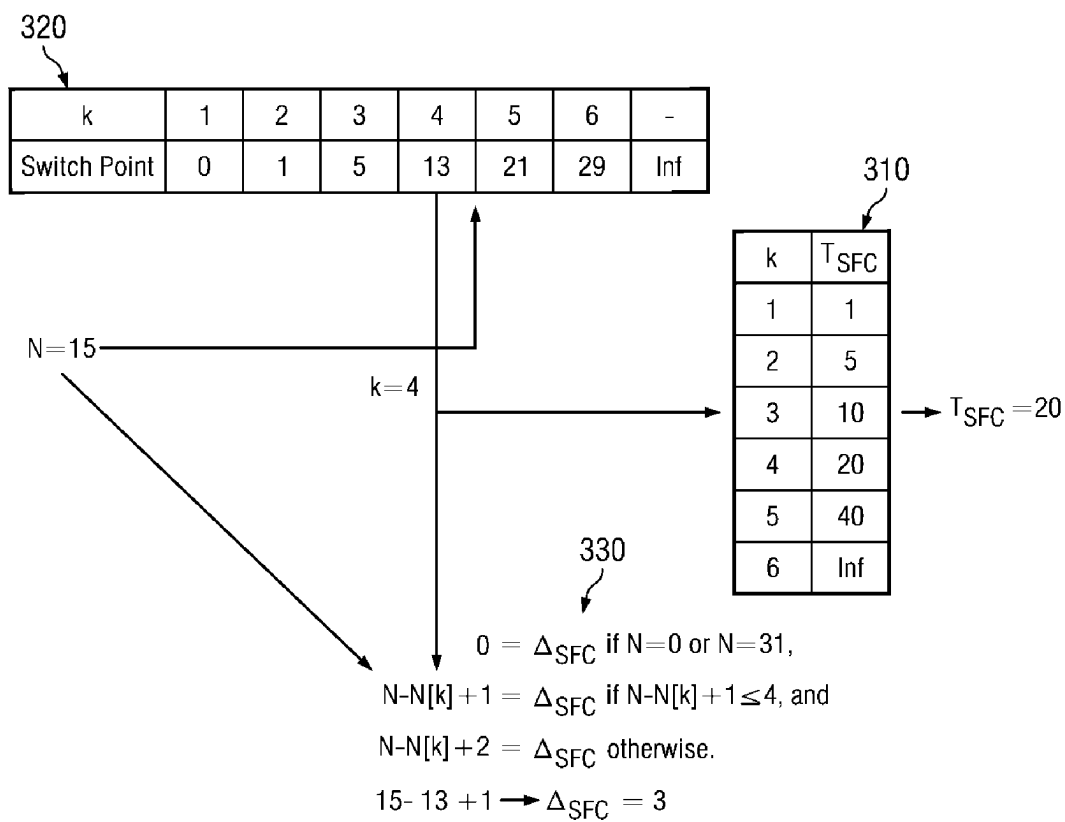


FIG. 3

CELL SPECIFIC SOUNDING REFERENCE SIGNAL SUB-FRAME CONFIGURATION

CLAIM OF PRIORITY

[0001] This application claims priority under 35 U.S.C. 119(e) (1) to U.S. Provisional Application No. 61/048,738 filed Apr. 29, 2008, U.S. Provisional Application No. 61/051,453 filed May 8, 2008 and U.S. Provisional Application No. 61/051,482 filed May 8, 2008.

TECHNICAL FIELD OF THE INVENTION

[0002] The technical field of this invention is wireless communication.

BACKGROUND OF THE INVENTION

[0003] FIG. 1 shows an exemplary wireless telecommunications network **100**. The illustrative telecommunications network includes base stations **101**, **102** and **103**, though in operation, a telecommunications network necessarily includes many more base stations. Each of base stations **101**, **102** and **103** are operable over corresponding coverage areas **104**, **105** and **106**. Each base station's coverage area is further divided into cells. In the illustrated network, each base station's coverage area is divided into three cells. Handset or other user equipment (UE) **109** is shown in Cell A **108**. Cell A **108** is within coverage area **104** of base station **101**. Base station **101** transmits to and receives transmissions from UE **109**. As UE **109** moves out of Cell A **108** and into Cell B **107**, UE **109** may be handed over to base station **102**. Because UE **109** is synchronized with base station **101**, UE **109** can employ non-synchronized random access to initiate handover to base station **102**.

[0004] Non-synchronized UE **109** also employs non-synchronous random access to request allocation of up-link **111** time or frequency or code resources. If UE **109** has data ready for transmission, which may be traffic data, measurements report, tracking area update, UE **109** can transmit a random access signal on up-link **111**. The random access signal notifies base station **101** that UE **109** requires up-link resources to transmit the UE's data. Base station **101** responds by transmitting to UE **109** via down-link **110**, a message containing the parameters of the resources allocated for UE **109** up-link transmission along with a possible timing error correction. After receiving the resource allocation and a possible timing advance message transmitted on down-link **110** by base station **101**, UE **109** optionally adjusts its transmit timing and transmits the data on up-link **111** employing the allotted resources during the prescribed time interval.

[0005] FIG. 2 shows the Evolved Universal Terrestrial Radio Access (E-UTRA) time division duplex (TDD) Frame Structure. Different sub-frames are allocated for downlink (DL) or uplink (UL) transmissions. Table 1 shows applicable DL/UL sub-frame allocations.

TABLE 1

Con-figuration	Switch-point periodicity	Sub-frame number									
		0	1	2	3	4	5	6	7	8	9
0	5 ms	D	S	U	U	U	D	S	U	U	U
1	5 ms	D	S	U	U	D	D	S	U	U	D
2	5 ms	D	S	U	D	D	D	S	U	D	D
3	10 ms	D	S	U	U	U	D	D	D	D	D

TABLE 1-continued

Con-figuration	Switch-point periodicity	Sub-frame number									
		0	1	2	3	4	5	6	7	8	9
4	10 ms	D	S	U	U	D	D	D	D	D	D
5	10 ms	D	S	U	D	D	D	D	D	D	D
6	10 ms	D	S	U	U	U	D	S	U	U	D

[0006] Sounding RS enables time and frequency domain scheduling and has been adopted as a RAN1 working assumption for EUTRA. The channel quality indicator (CQI) estimate obtained from sounding can be expired or stale because of the inevitable time delay between channel sounding and the follow-up scheduled transmission. This is more pronounced for faster user equipment (UE). Thus faster UE needs to have more frequent sounding in order to maintain the fresh CQI at the NodeB. For example a UE with a Doppler of 200 Hz requires a propagation channel for every fifth sub-frame because the sub-frame rate is 1000 Hz. In such case for channel adaptive modulation and coding (AMC) to be performed, the UE must sound nearly every sub-frame or every other sub-frame. The objective of maintaining a fresh CQI at the NodeB may be impossible for very fast UEs having a Doppler of 200 Hz or more because the channel can change substantially between sub-frames. For such fast UEs, a slow rate of infrequent sounding can be performed. Slower UEs naturally ought to sound less frequently. As the UE speed increases, the sounding period should reduce up to a point. Very fast UEs should abandon the goal of maintaining a fresh CQI and sound less frequently.

[0007] A simple solution is to configure each cell with a common sounding period for each UE and for each sounding resource. However, any cell may contain UEs with a spread of velocities yielding a spread of Dopplers. Allocating sounding resources to UEs corresponding to the set of UEs velocities would be efficient. This allocation enables efficient utilization of sounding resources. In another proposed allocation, very slow UEs sound only once per several sub-frames and intermediate speed UEs sound once per few sub-frames. This allocation is not straight forward and not always possible. It is mathematically impossible to share a common sounding resource between one UE sounding every 2 sub-frames and a second UE sounding every 3 sub-frames. There is a need in the art to use different sounding periods different cells while tailoring each sounding period to the velocity of a UE or subset of UEs.

SUMMARY OF THE INVENTION

[0008] A method of wireless communication including a plurality of fixed base stations and a plurality of mobile user equipment with each base station transmitting to any user equipment within a corresponding cell a sounding reference signal sub-frame configuration indicating sub-frames when sounding is permitted. Each user equipment recognizes the sounding reference signal sub-frame configuration and sounds only at permitted sub-frames. Differing cells may have differing sounding reference signal sub-frame configurations. There are numerous manners to encode the transmitted information.

BRIEF DESCRIPTION OF THE DRAWINGS

[0009] These and other aspects of this invention are illustrated in the drawings, in which:

[0010] FIG. 1 is a diagram of a communication system of the prior art related to this invention having three cells;

[0011] FIG. 2 shows the Evolved Universal Terrestrial Radio Access (E-UTRA) TDD Frame Structure of the prior art;

[0012] FIG. 3 shows an alternative manner of determining the sounding frequency in sub-frames and the sub-frame offset.

DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

[0013] Sounding involves exchange of signals between the base station and the connected user equipment. Each sounding uses a reference resource identifier selected from an available reference resource identifier map $h(t, L)$ and a portion of the spectrum selected from an available spectrum identifier map $f(t, N)$; where L is a group of shared parameters signaled to each UE from the group; and N is a group of shared parameters signaled to each UE from the group. Some examples utilize CAZAC sequences as the reference sequences. CAZAC sequences are complex-valued sequences with: constant amplitude (CA); and zero cyclic autocorrelation (ZAC). Examples of CAZAC sequences include: Chu sequences, Frank-Zadoff sequences, Zadoff-Chu (ZC) sequences and generalized chirp-like (GCL) sequences. CAZAC (ZC or otherwise) sequences are presently preferred.

[0014] Zadoff-Chu (ZC) sequences, as defined by:

$$a_m(k) = e^{j2\pi(m/N)\left[\frac{k(k+1)}{2} + qk\right]} \text{ for } N \text{ odd,}$$

$$a_m(k) = e^{j2\pi(m/N)\left[\frac{k^2}{2} + qk\right]} \text{ for } N \text{ even.}$$

An alternative convention of the ZC definition replaces j (the complex number $\sqrt{-1}$) in these formulas with $-j$. In the formula: m is the index of the root ZC sequence; N is the length of the sequence, with m and N relatively prime; q is any fixed integer, for example, $q=0$ is a good choice because it simplifies computation as $qk=0$; and k is the index of the sequence element from $\{0, 1, \dots, N-1\}$. Making N a prime number maximizes the set of root ZC sequences having optimal cross-correlation. When N is prime, there are $N-1$ possible choices for m and each choice results in a distinct root ZC CAZAC sequence. The terms: Zadoff-Chu, ZC, and ZC CAZAC, are commonly used interchangeably.

[0015] The problem of allocating sounding resources is to cover each UE with sounding fast enough to meet their requirements. The maximum sounding period is generally related the UE Doppler, a measure of how fast the UE is moving relative to the base station. We assume that the sounding requirements of the set of UEs are fixed at any point in time but may vary slowly with time. This slow time change enables computing and using repeating patterns for the sounding resource allocation.

[0016] The sounding reference signal (SRS) sub-frame configuration is broadcast by base station **101** in SIB. This sub-frame configuration indicates which sub-frames are SRS sub-frames. Broadcast of the SRS sub-frame configuration is useful even for UEs **109** which do not transmit any SRS. SRS shouldn't collide with physical uplink shared channel (PUSCH) transmission. Thus non-SRS UEs **109** can extract some of their silent symbol periods from the SRS sub-frame configuration. These silent periods are useful for performing some measurements at UE **109**. In general each cell **107** and **108** would employ a different SRS sub-frame configuration.

Ideally, base stations **101**, **102** and **103** would select SRS sub-frame configurations to minimize cross-cell interference.

[0017] There are two main ways of signaling and interpreting the SRS sub-frame configuration parameters. Sub-frame configuration can be defined by two parameters: the sub-frame period T_{SFC} ; and the offset Δ_{SFC} . Both UEs **109** and base station **101** keep a sub-frame counter C_{SFC} permitting UE **109** and base station **101** to determine which sub-frames are configured for SRS transmission. A sub-frame is an SRS sub-frame if and only if $\Delta_{SFC} = (C_{SFC}) \bmod T_{SFC}$. The exact range of values of Δ_{SFC} and T_{SFC} need to be defined with the number of bits and encoding for each. For example, T_{SFC} could be selected from the set $\{1, 2, 3, 4, 5, \dots, 32\}$ allowing flexible system deployment Δ_{SFC} could be selected from the same set. This yields maximum flexibility, but requires 10 bits of broadcast SIB signaling, which can be very costly. A reduced overhead alternative encodes and signals T_{SFC} first. This requires greatest integer in $\log_2(T_{SFC})$ ($\text{ceil}[\log_2(T_{SFC})]$) bits. The bits required for Δ_{SFC} would be either the $\text{ceil}[\log_2(T_{SFC})]$ or the least integer in $\log_2(T_{SFC})$ ($\text{floor}[\log_2(T_{SFC})]$) because $0 \leq \Delta_{SFC} < T_{SFC}$. This reduces the number of required bits for signaling Δ_{SFC} , but only for certain scenarios where T_{SFC} is small. Another reduced overhead alternative hard codes a value for Δ_{SFC} such as zero. In that case, only T_{SFC} is signaled.

[0018] Configuration of the sounding reference signal (SRS) contains cell specific components and UE specific components. Cell specific components of the SRS configuration indicate particular subframes when the SRS transmission occurs. Cell specific components of the SRS configuration may include T_{SFC} , the SRS sub-frame period and Δ_{SFC} SRS sub-frame offset. The UE keeps a sub-frame counter C_{SFC} .

[0019] SRS sub-frames are those for which the counter C_{SFC} satisfies the condition $\Delta_{SFC} = (C_{SFC}) \bmod T_{SFC}$. These quantities T_{SFC} and Δ_{SFC} must be signaled to the UEs. This is generally preformed by through SIB signaling. This invention includes a specific bit-map table for this signaling. This invention supports a very wide range of T_{SFC} and the Δ_{SFC} values with 5-bit signaling. This invention supports values for T_{SFC} in the set of $\{1, 2, 5, 10, 20, 40, \text{Inf}\}$ ms. This invention also includes a proposed bit-map tables allowing a wide range of Δ_{SFC} .

[0020] Table 2 shows the 5 bits signaled via SIB designating T_{SFC} and Δ_{SFC} in time division duplex (TDD) applications according to one embodiment of this invention. For Δ_{SFC} of values 1 or 6 (i.e. UpPTS), either one or both SC-OFDM symbols in UpPTS are used for SRS. The number of SC-OFDM symbols in UpPTS is broadcasted by another field in SIB. In other words, if UpPTS consists of 2 SC-OFDM symbols and is configured for SRS transmission, then both SC-OFDM symbols are used for SRS transmission. In TDD, sounding employs UpPTS resources except occupied by short RACH are default for SRS. SRS is transmitted only in configured UL subframes or UpPTS.

TABLE 2

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	00000	1	0
1	00001	5	1
2	00010	5	2
3	00011	5	3
4	00100	5	4
5	00101	10	1
6	00110	10	2
7	00111	10	3
8	01000	10	4

TABLE 2-continued

Decimal	Binary	T_{SFC}	Δ_{SFC}
9	01001	10	6
10	01010	10	7
11	01011	10	8
12	01100	10	9
13	01101	20	1
14	01110	20	2
15	01111	20	3
16	10000	20	4
17	10001	20	6
18	10010	20	7
19	10011	20	8
20	10100	20	9
21	10101	40	1
22	10110	40	2
23	10111	40	3
24	11000	40	4
25	11001	40	6
26	11010	40	7
27	11011	40	8
28	11100	40	9
29	11101	Reserved	Reserved
30	11110	Reserved	Reserved
31	11111	Inf.	0

For the signaled number decimal **31** and binary 11111 Inf. indicates infinity. This means that there are no soundings thus the interval between soundings is infinite. In this case the offset Δ_{SFC} is 0. For the signaled number decimal **29**, binary 11101 and for the signaled number decimal **30**, binary 11110 the code are reserved.

[0021] FIG. 3 illustrates an alternative formulation of this SRS selection. The set of possible SRS possible periods T_{SFC} is defined in an ordered list $T_{SFC}[1]$ to $T_{SFC}[k]m$ where $T_{SFC}[1] < T_{SFC}[2] < \dots < T_{SFC}[k]$. In FIG. 3 this is set **310** {1, 5, 10, 20, 40, Inf.} ms, where $k=6$. A set of switch-point numbers $N[1]$ to $N[k+1]$ are formed in an ordered list where $N[1] < N[2] < \dots < N[k] < N[k+1]$. In FIG. 3 these switch-point numbers are set **320** {0, 1, 5, 13, 21, 29, Inf.}. The base station signals via SIB a configuration index N . The UE may then finds the unique index k for which $N[k] \leq N < N[k+1]$. The sub-frame period is then $T_{SFC} = T_{SFC}[k]$. The offset Δ_{SFC} is calculated using formula **330**:

$$\Delta_{SFC} = 0 \text{ if } N=0 \text{ or } N=31,$$

$$\Delta_{SFC} = N - N[k] + 1 \text{ if } N - N[k] + 1 \leq 4, \text{ and}$$

$$\Delta_{SFC} = N - N[k] + 2 \text{ otherwise.}$$

FIG. 3 illustrates this process for $N=15$. If $N=15$ is broadcast in SIB, the UE determines that 15 is greater than or equal to $N[4]$ which is 13 and less than $N[5]$ which is 21. This designates an index k of 4. UE then selects $T_{SFC} = T_{SFC}[4] = 20$ ms. For the offset Δ_{SFC} , the UE notes that $N - N[k] + 1 = 15 - 13 + 1 = 3$ is less than or equal to 4. Thus Δ_{SFC} is 3.

[0022] Table 3 shows the 4 bits signaled via SIB designating T_{SFC} and Δ_{SFC} in time division duplex (TDD) applications according to yet another embodiment of this invention.

TABLE 3

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	0000	5	{1}
1	0001	5	{1, 2}
2	0010	5	{1, 3}
3	0011	5	{1, 4}

TABLE 3-continued

Decimal	Binary	T_{SFC}	Δ_{SFC}
4	0100	5	{1, 2, 3}
5	0101	5	{1, 2, 4}
6	0110	5	{1, 3, 4}
7	0111	5	{1, 2, 3, 4}
8	1000	10	{1, 2, 6}
9	1001	10	{1, 3, 6}
10	1010	10	{1, 6, 7}
11	1011	20	{1, 2, 6, 11, 16}
12	1100	20	{1, 3, 6, 11, 16}
13	1101	20	{1, 6, 7, 11, 16}
14	1110	Inf.	NA
15	1111	reserved	reserved

[0023] In Table 3 T_{SFC} is selected from the set including {5, 10, 20, Inf.}. There may be plural offsets Δ_{SFC} for each value of T_{SFC} . For the signaled number decimal **12** and binary 1110 Inf. indicates infinity. This means that there are no soundings thus the interval between soundings is infinite. In this case the offset Δ_{SFC} is not applicable (NA). For signaled number decimal **15** and binary 1111 the code is reserved. For TDD, sounding reference signal is transmitted only in configured UL sub-frames or UpPTS.

[0024] Table 4 shows the 4 bits signaled via SIB designating T_{SFC} and Δ_{SFC} in time division duplex (TDD) applications according to still another embodiment of this invention.

TABLE 4

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	0000	5	{1}
1	0001	5	{1, 2}
2	0010	5	{1, 3}
3	0011	5	{1, 4}
4	0100	5	{1, 2, 3}
5	0101	5	{1, 2, 4}
6	0110	5	{1, 3, 4}
7	0111	5	{1, 2, 3, 4}
8	1000	10	{1, 2, 6}
9	1001	10	{1, 3, 6}
10	1010	10	{1, 6, 7}
11	1011	10	{1, 2, 6, 7}
12	1100	10	{1, 3, 6, 8}
13	1101	10	{1, 4, 6, 9}
14	1110	Inf	NA
15	1111	reserved	reserved

[0025] In Table 4 T_{SFC} is selected from the set including {10, 20, Inf.}. There may be plural offsets Δ_{SFC} for each value of T_{SFC} . For the signaled number decimal **14** and binary 1110 Inf. indicates infinity. This means that there are no soundings thus the interval between soundings is infinite. In this case the offset Δ_{SFC} is not applicable (NA). For signaled number decimal **15** and binary 1111 the code is reserved.

[0026] This invention describes a manner to encode the SRS sub-frame configuration. This could either be table based or described in text as described above.

What is claimed is:

1. A method of wireless communication including a plurality of fixed base stations and a plurality of mobile user equipment comprising the steps of:

each base station transmitting to any user equipment within a corresponding cell a sounding reference signal sub-frame configuration indicating sub-frames when sounding is permitted using jointly coding periodicity T_{SFC}

and offset Δ_{SFC} , wherein differing base stations may transmit differing sounding reference signal sub-frame configurations;

each user equipment within said corresponding cell recognizing said sounding reference signal sub-frame configuration; and

each user equipment sounding only at sub-frames when sounding is permitted according to said recognized sounding reference signal sub-frame configuration.

2. The method of claim 1, wherein:

said step of jointly coding said periodicity T_{SFC} and said offset Δ_{SFC} codes in 4 bits suitable for use in time division duplex systems as follows:

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	00000	1	0
1	00001	5	1
2	00010	5	2
3	00011	5	3
4	00100	5	4
5	00101	10	1
6	00110	10	2
7	00111	10	3
8	01000	10	4
9	01001	10	6
10	01010	10	7
11	01011	10	8
12	01100	10	9
13	01101	20	1
14	01110	20	2
15	01111	20	3
16	10000	20	4
17	10001	20	6
18	10010	20	7
19	10011	20	8
20	10100	20	9
21	10101	40	1
22	10110	40	2
23	10111	40	3
24	11000	40	4
25	11001	40	6
26	11010	40	7
27	11011	40	8
28	11100	40	9
29	11101	Reserved	Reserved
30	11110	Reserved	Reserved
31	11111	Inf.	0

where: codings 29, binary 11101 and decimal 30, binary 11110 are reserved; and coding decimal 31 and binary 11111 indicates no SRS thus T_{SFC} is infinite and Δ_{SFC} is 0.

3. The method of claim 1, wherein:

said step of jointly coding said periodicity T_{SFC} and said offset Δ_{SFC} codes in 4 bits suitable for use in time division multiplex systems as follows:

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	0000	5	{1}
1	0001	5	{1, 2}
2	0010	5	{1, 3}
3	0011	5	{1, 4}
4	0100	5	{1, 2, 3}
5	0101	5	{1, 2, 4}
6	0110	5	{1, 3, 4}
7	0111	5	{1, 2, 3, 4}
8	1000	10	{1, 2, 6}
9	1001	10	{1, 3, 6}
10	1010	10	{1, 6, 7}
11	1011	20	{1, 2, 6, 11, 16}

-continued

Decimal	Binary	T_{SFC}	Δ_{SFC}
12	1100	20	{1, 3, 6, 11, 16}
13	1101	20	{1, 6, 7, 11, 16}
14	1110	Inf.	NA
15	1111	reserved	reserved

where: coding decimal 14, binary 1110 indicates no SRS thus T_{SFC} is infinite and Δ_{SFC} is thus not applicable (NA); and coding 15, binary 1111 is reserved.

4. The method of claim 1, wherein:

said step of jointly coding said periodicity T_{SFC} and said offset Δ_{SFC} codes in 4 bits suitable for use in time division multiplex systems as follows:

Decimal	Binary	T_{SFC}	Δ_{SFC}
0	0000	5	{1}
1	0001	5	{1, 2}
2	0010	5	{1, 3}
3	0011	5	{1, 4}
4	0100	5	{1, 2, 3}
5	0101	5	{1, 2, 4}
6	0110	5	{1, 3, 4}
7	0111	5	{1, 2, 3, 4}
8	1000	10	{1, 2, 6}
9	1001	10	{1, 3, 6}
10	1010	10	{1, 6, 7}
11	1011	10	{1, 2, 6, 7}
12	1100	10	{1, 3, 6, 8}
13	1101	10	{1, 4, 6, 9}
14	1110	Inf	NA
15	1111	reserved	reserved

where: coding decimal 14, binary 1110 indicates no SRS thus T_{SFC} is infinite and Δ_{SFC} is thus not applicable (NA); and coding 15, binary 1111 is reserved.

5. The method of claim 1, wherein:

said step of each user equipment sounding only at sub-frames when sounding is permitted includes maintaining a sub-frame count C_{SFC} , and sounding only if $\Delta_{SFC} = (C_{SFC}) \bmod T_{SFC}$.

6. The method of claim 1, wherein:

said step of jointly coding said periodicity T_{SFC} and said offset Δ_{SFC} includes

determining a set of k possible periodicities T_{SFC} , disposing said set of possible periodicities T_{SFC} in a monotonically increasing array of k elements $T_{SFC}(k)$,

recessively defining a set of switch points N where $N(0) = 0$ and $N(k+1) = N(k) + T_{SFC}(k)$, and

transmitting an configuration index N; and

said step of recognizing said sounding reference signal sub-frame configuration includes

finding a unique index k for which $N(k) \leq N < N(k+1)$,

determining the periodicity T_{SFC} to be $T_{SFC}(k)$, and

determining the offset Δ_{SFC} to be 0 if is $N=0$ or $N=31$, $N-N[k]+1$ if $N-N[k]+1 \leq 4$ and $N-N[k]+2$ otherwise.

7. The method of claim 6, wherein:

said monotonically increasing array of k elements $T_{SFC}(k)$ consists of {1, 5, 10, 20, 40, Inf.} ms, where k is 6; and said switch-point numbers are 0, 1, 5, 13, 21, 29 and infinity.

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