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(54) **POISSON MATTING FOR IMAGES**

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348/590; 348/578; 348/584; 382/284; 345/630;  
345/640

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348/598, 597, 584, 590, 578, 722; 382/284,  
382/173; 345/630, 640, 592  
See application file for complete search history.

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*Assistant Examiner*—Jean W Désir

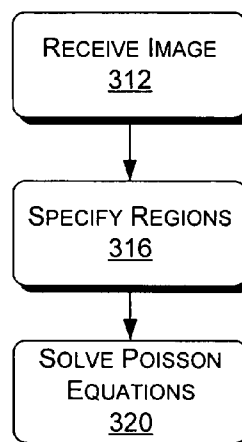
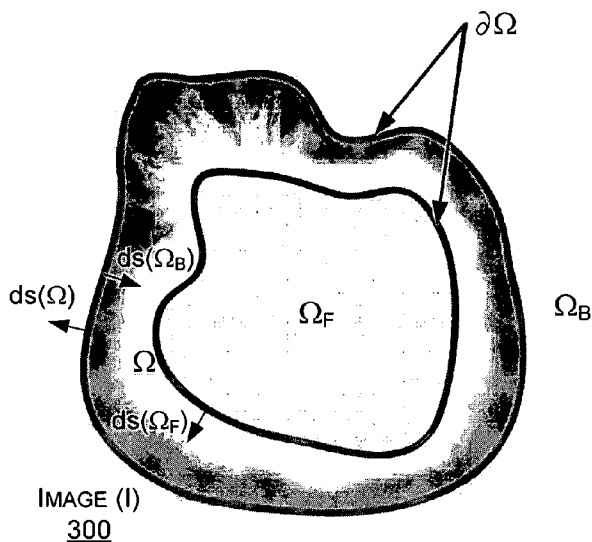
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(57) **ABSTRACT**

An exemplary method includes receiving a trimap for an image that specifies a background region, a foreground region and an unknown region for the image wherein a boundary exists between the foreground region and the unknown region and wherein another boundary exists between the unknown region and the background region, solving a set of Poisson equations having boundary conditions for the two boundaries to provide a matte that distinguishes a foreground region from a background region in the unknown region, and refining the matte by solving a set of Poisson equations for a local unknown region. Various other exemplary technologies are also presented.

**20 Claims, 11 Drawing Sheets**

**EXEMPLARY METHOD 310**



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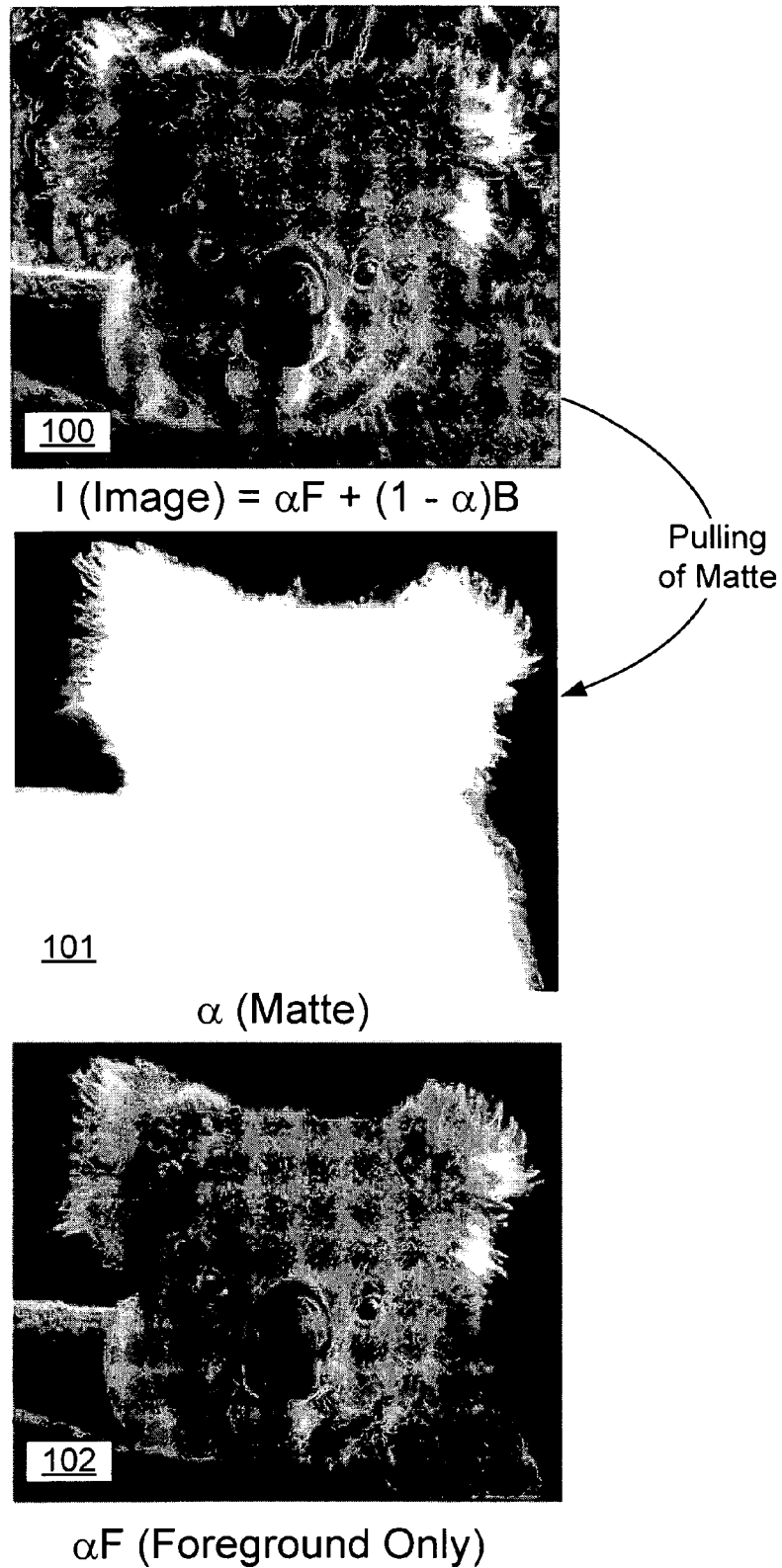


Fig. 1

EXEMPLARY ENGINE AND METHOD 200

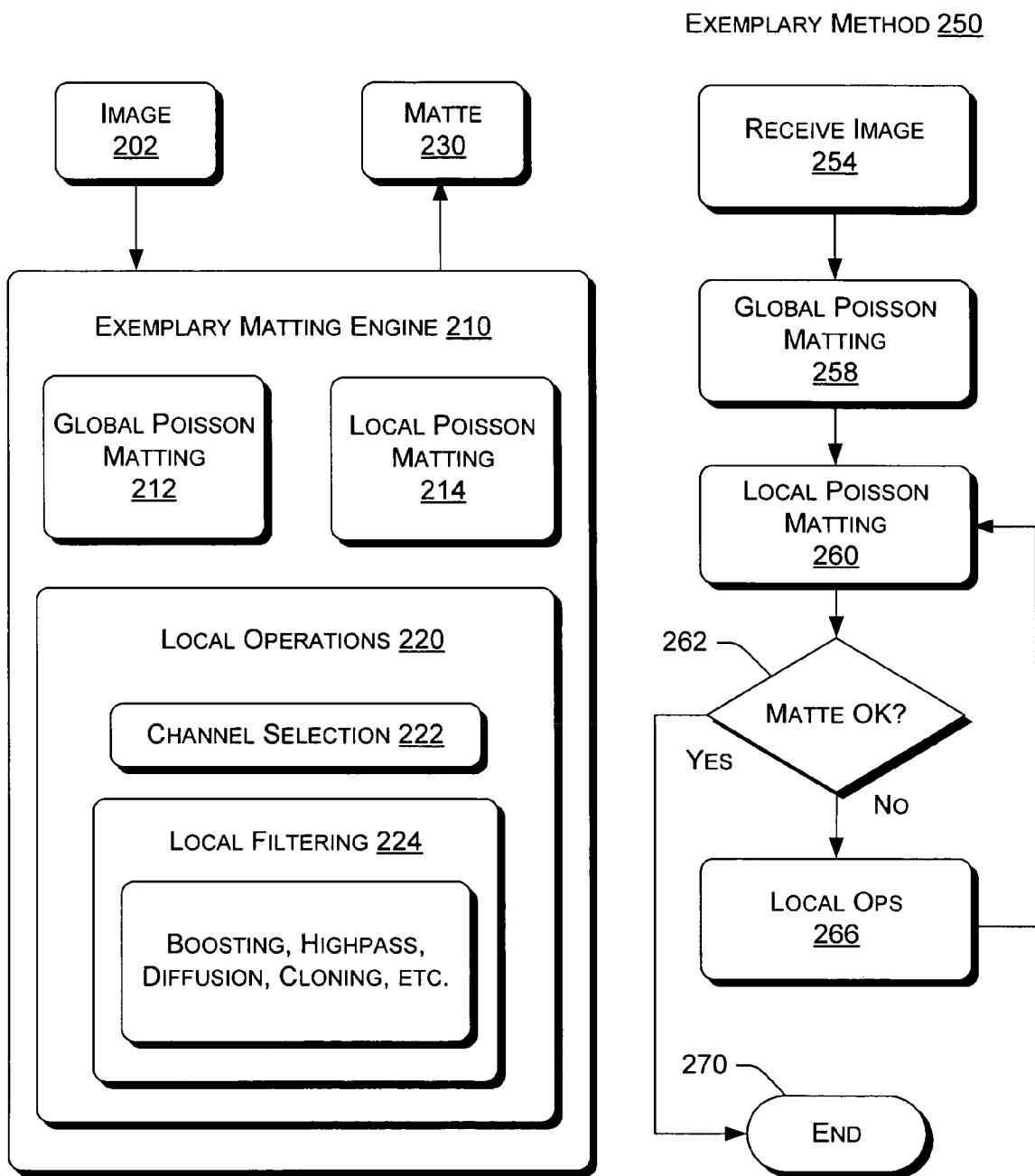
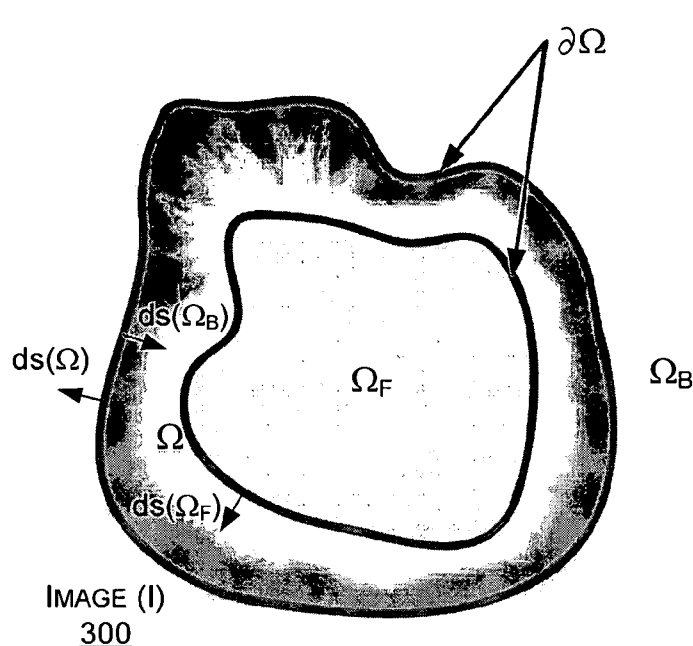


Fig. 2



EXEMPLARY METHOD 310

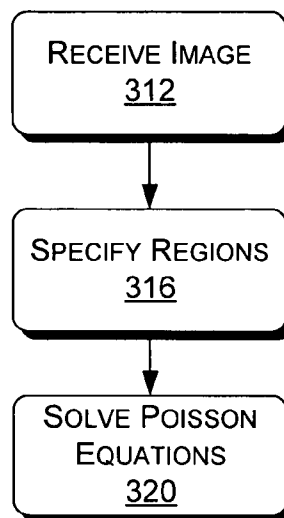
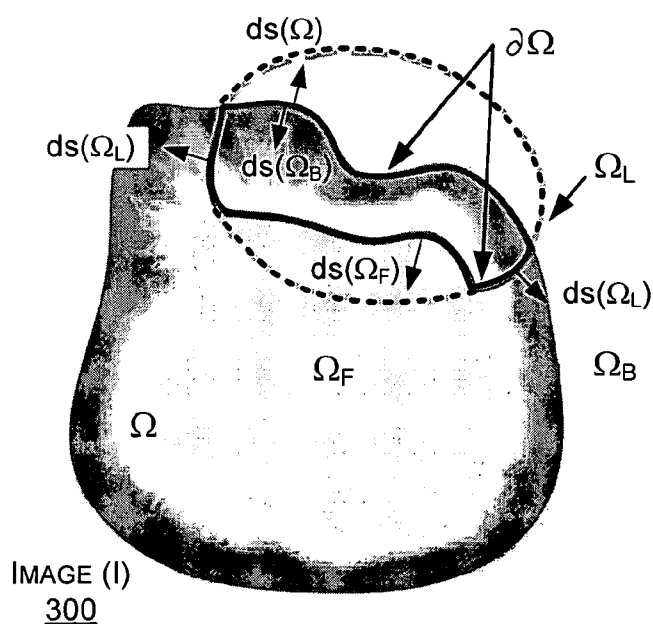


Fig. 3A



EXEMPLARY METHOD 350

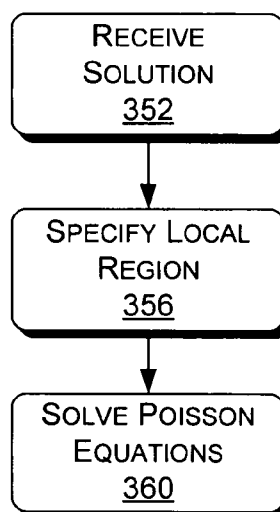


Fig. 3B

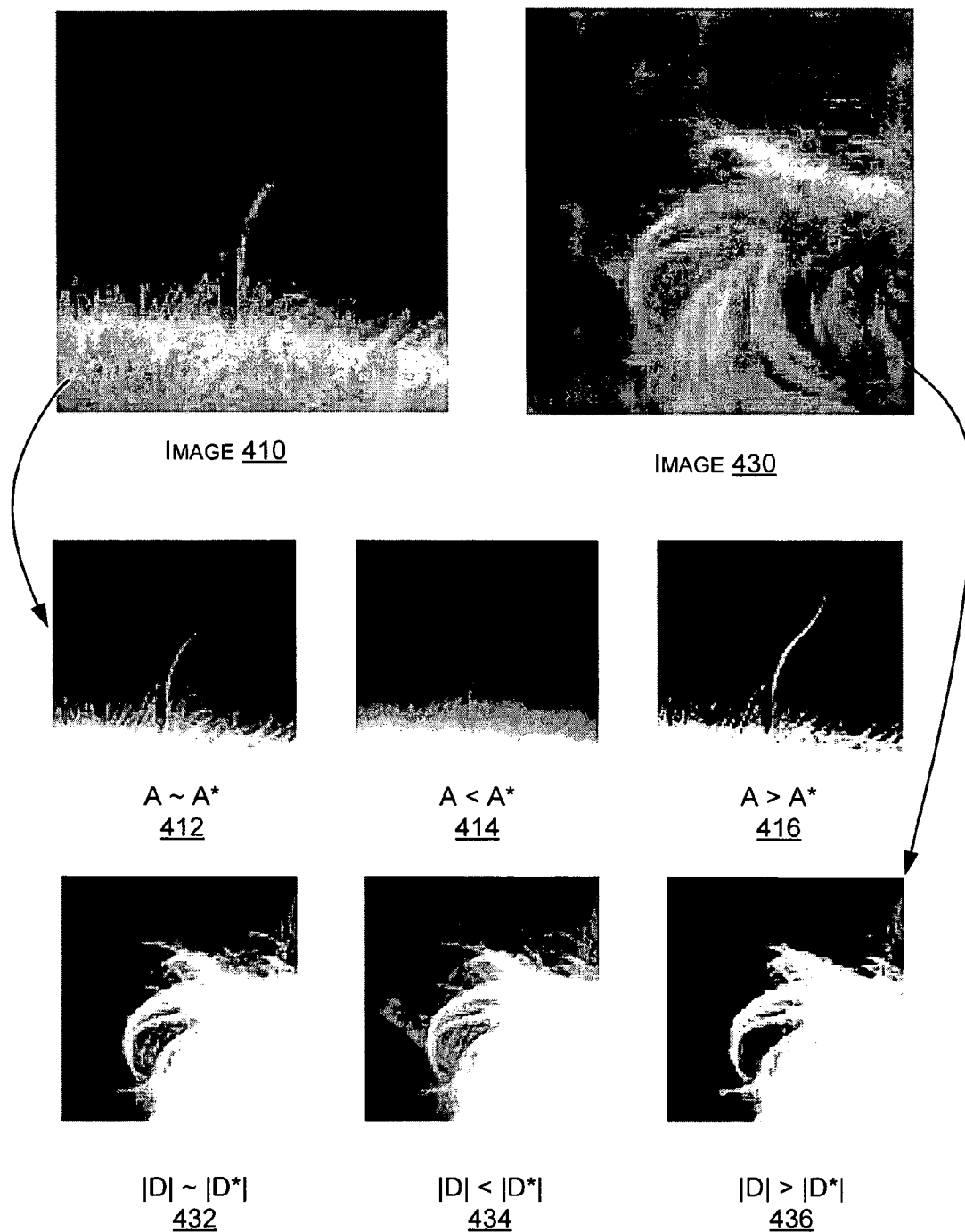
EXEMPLARY PROCESSES 400

Fig. 4

EXEMPLARY PROCESSES 500

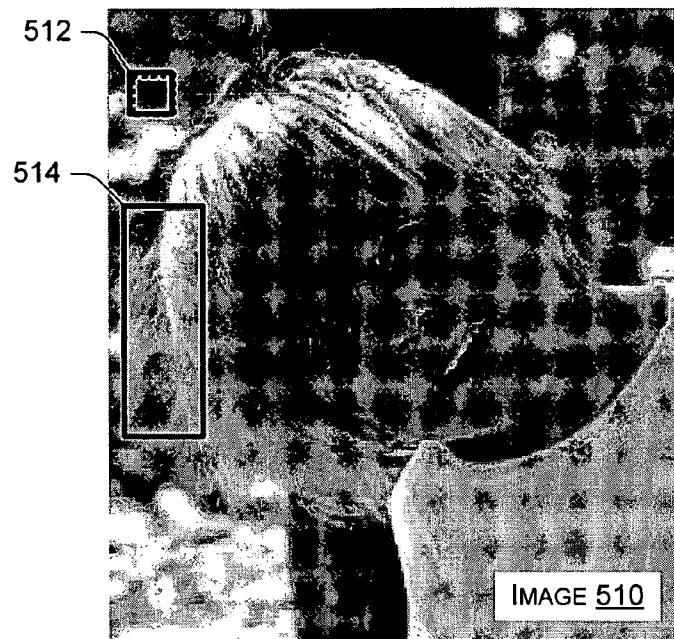
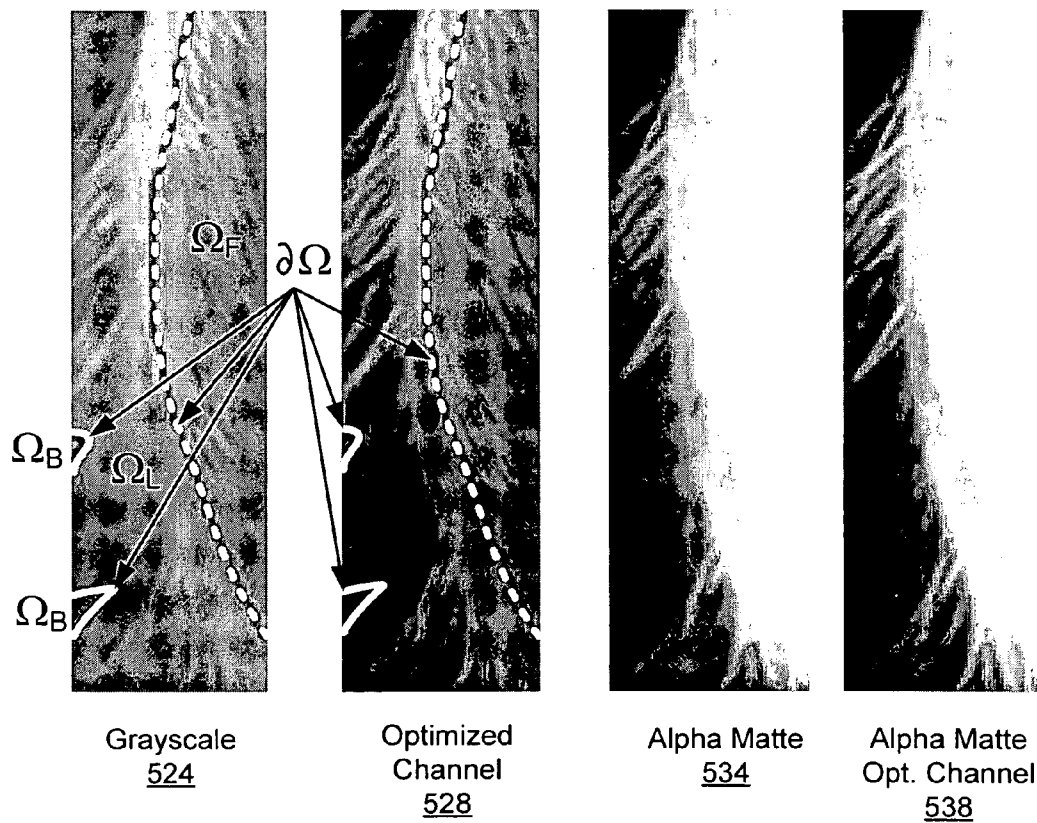


Fig. 5

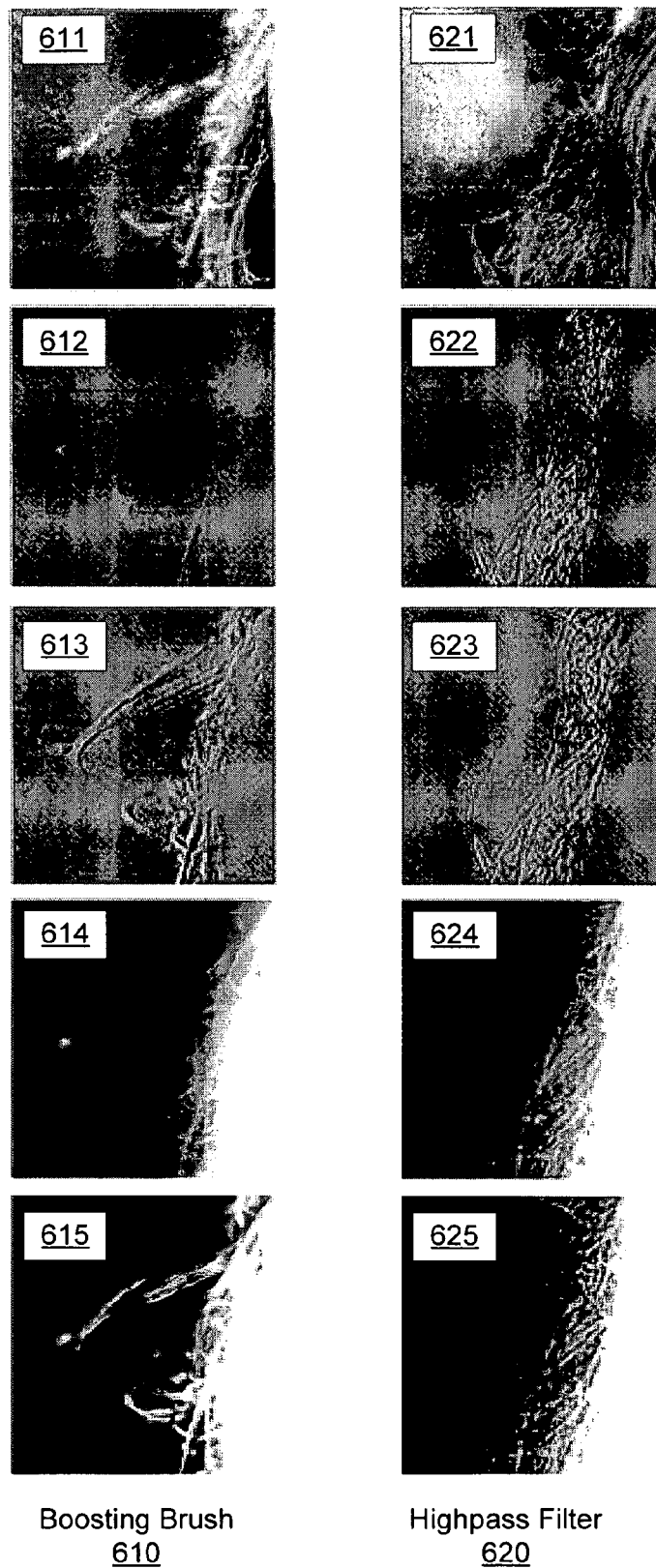


Fig. 6

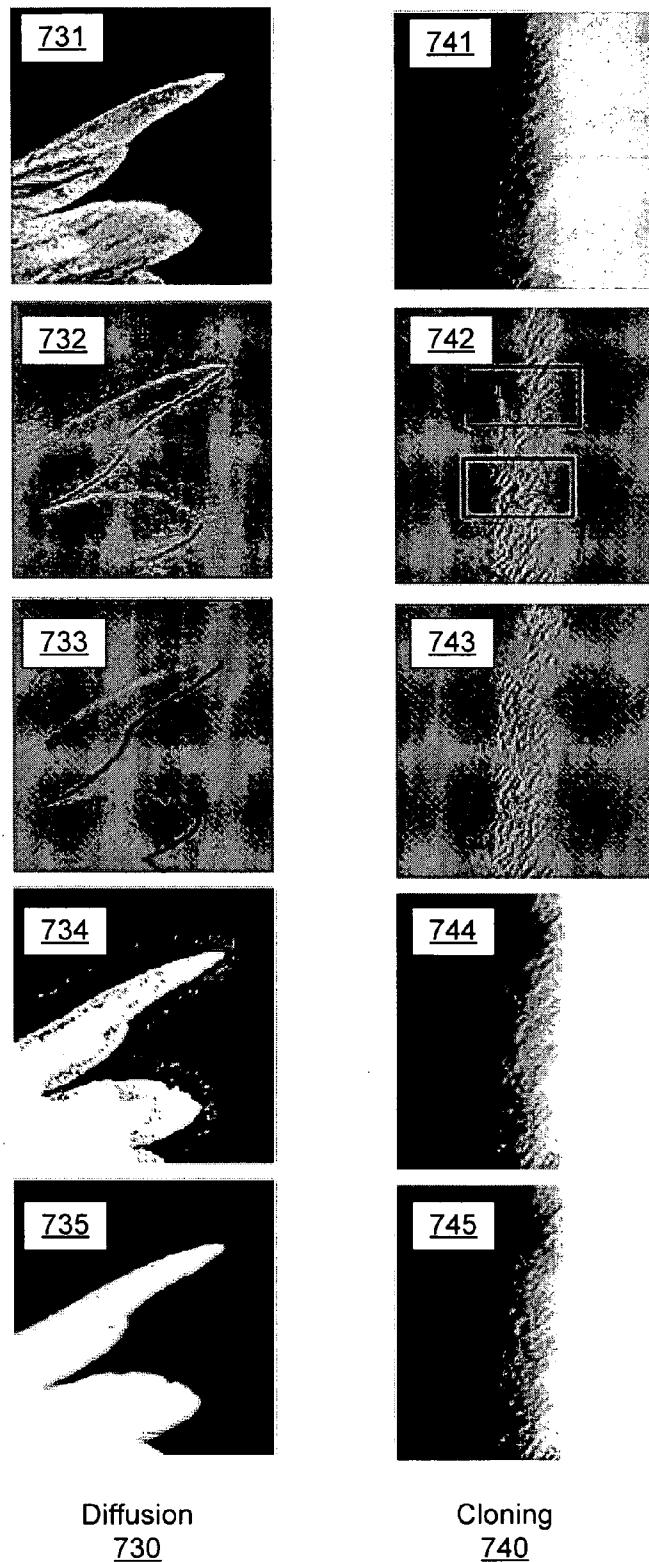


Fig. 7

Exemplary Process  
800

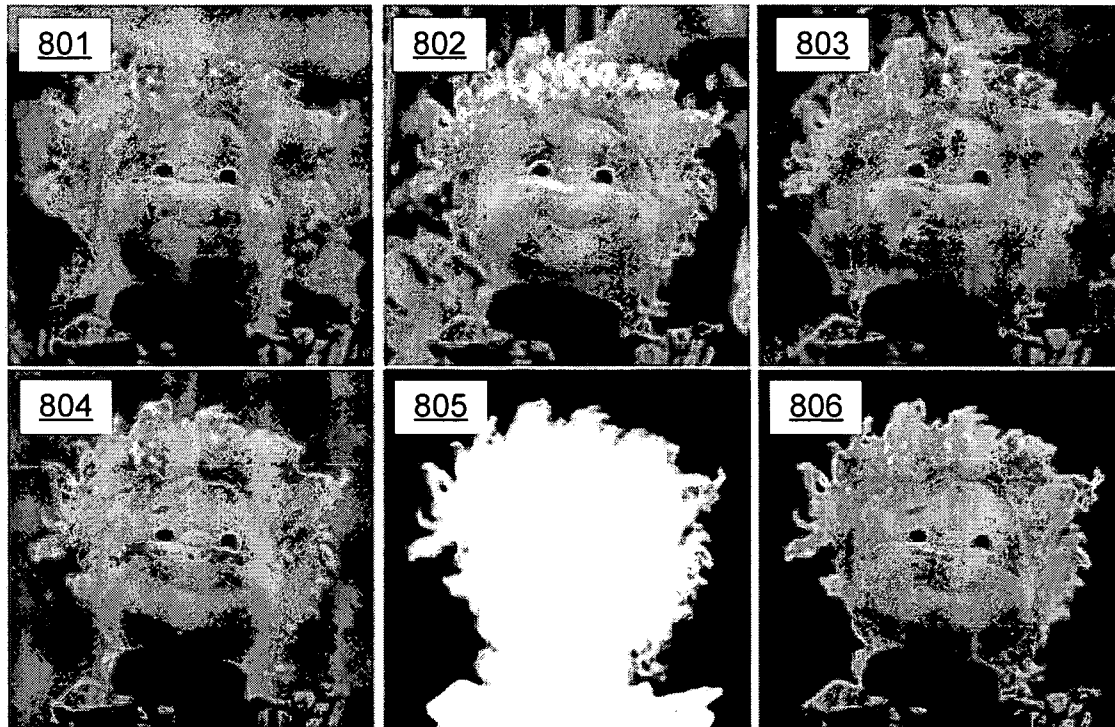


Fig. 8

Exemplary Process  
900



Fig. 9

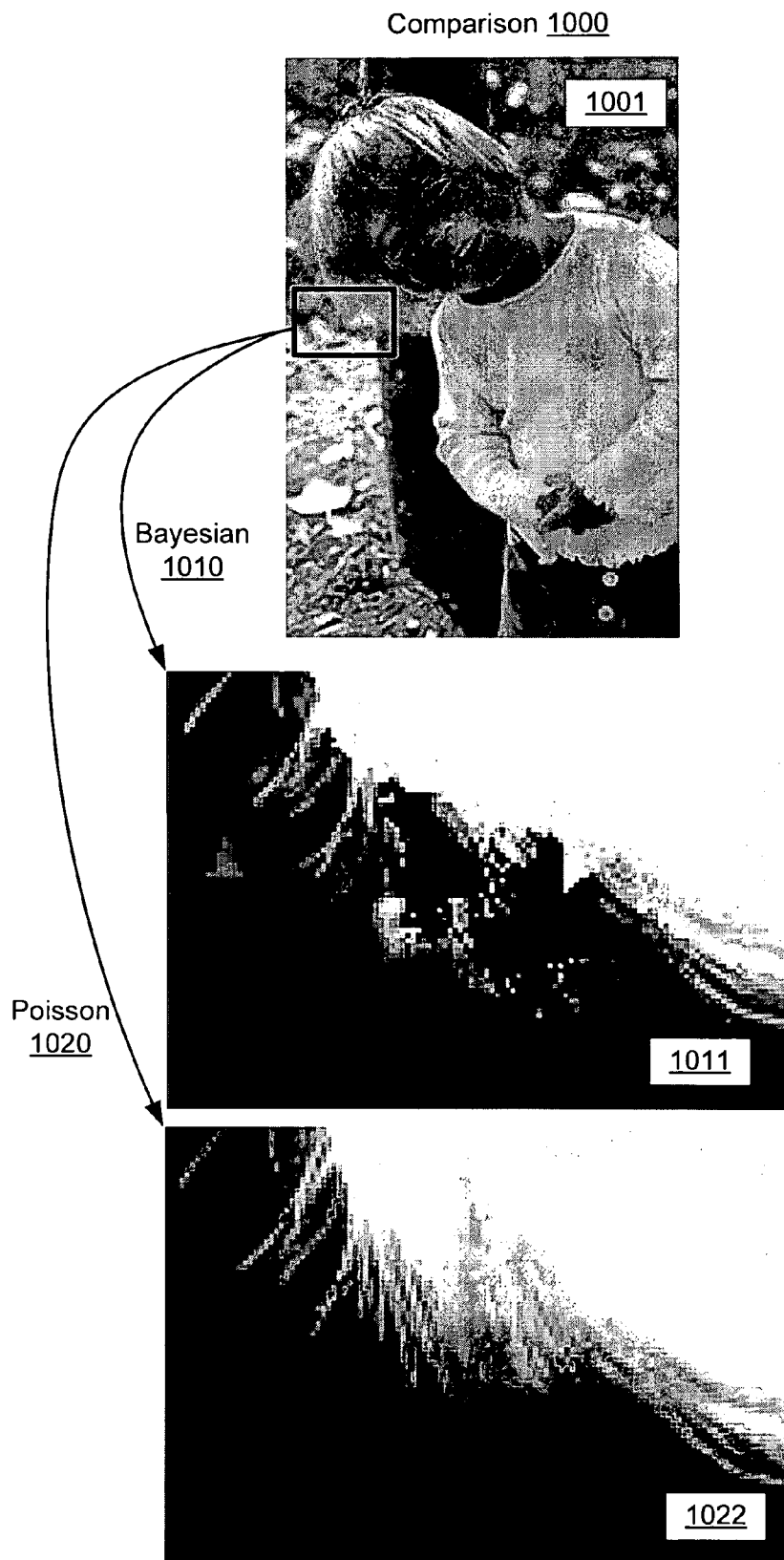
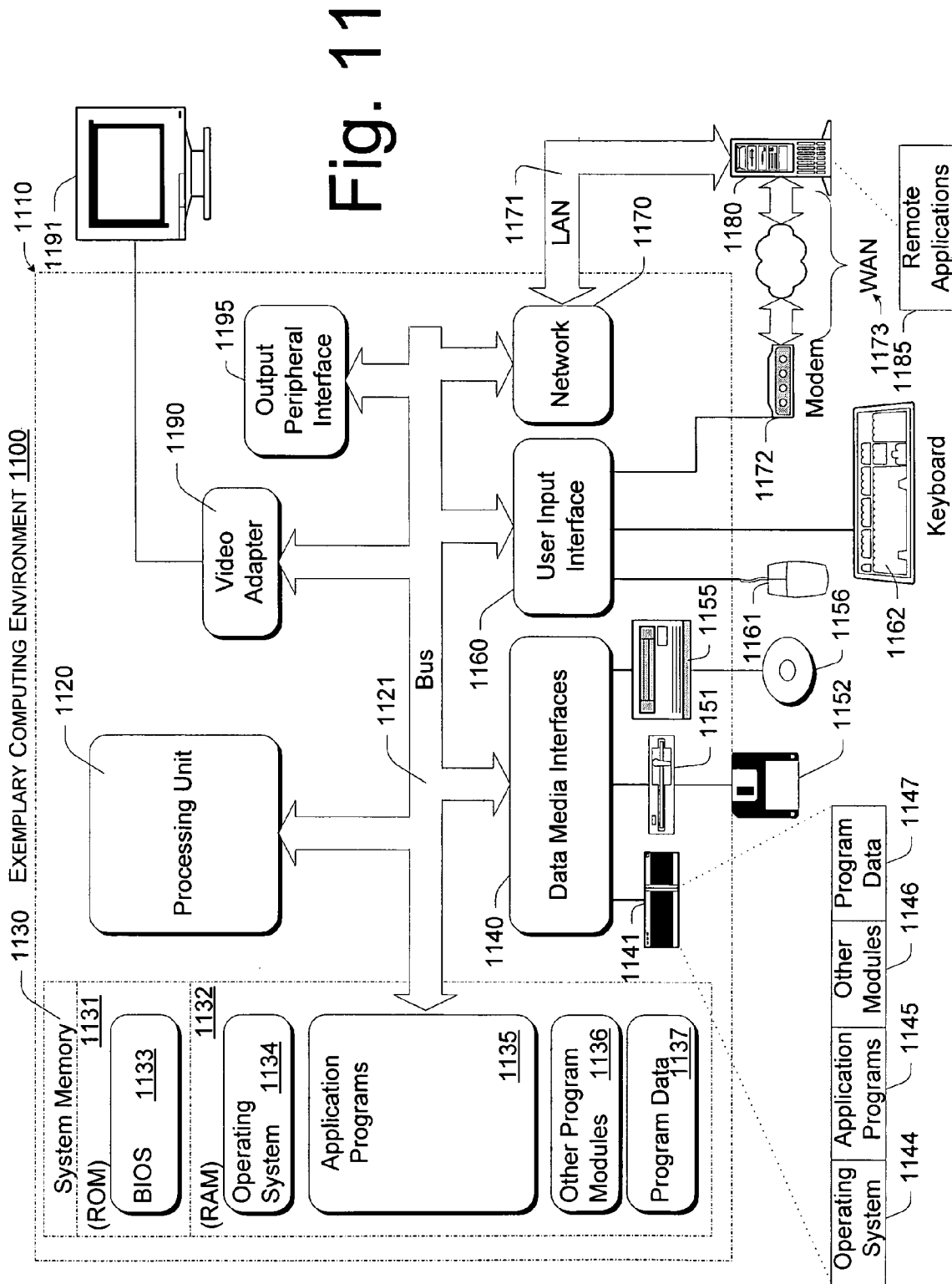


Fig. 10



1

## POISSON MATTING FOR IMAGES

## BACKGROUND

In image composition, a new image can be blended from a background image and a foreground image through use of an alpha matte of the image. On the other hand, separation of the alpha matte, the foreground and the background from a given image is a more difficult process, often referred to as the pulling of matte problem, or simply matting.

For example, in blue screen matting, the alpha matte and foreground can be readily reconstructed because the background is known (e.g., from a user-controlled environment). In contrast, for natural image matting, the alpha matte, the foreground and the background need to be estimated. Further, natural image matting is inherently under-constrained due to the number of unknowns of the matting equation. Thus, a need exists for improved natural image matting techniques. Various exemplary techniques described herein aim to address this and other issues associated with matting.

## SUMMARY

Natural image matting is an important tool for digital image editing such as for cutting and pasting selected objects from one image to another image and replacing the background of the selected objects. Various exemplary techniques presented herein reconstruct a matte from a continuous matte gradient field by solving Poisson equations using boundary information, for example, from a given trimap. Refinement may occur by interactively manipulating the matte gradient field using a number of filtering tools. A local result can be seamlessly integrated into the global result.

## BRIEF DESCRIPTION OF THE DRAWINGS

Non-limiting and non-exhaustive examples are described with reference to the following figures, wherein like reference numerals generally refer to like parts throughout the various views unless otherwise specified.

FIG. 1 is a natural image, a corresponding alpha matte and an extracted image, extracted from the natural image through use of the alpha matte.

FIG. 2 is a diagram of an exemplary matting engine and an exemplary matting method that rely on solving Poisson equations.

FIG. 3A is a diagram of a trimap for an image and an exemplary method that can specify the trimap and solve Poisson equations to provide a matte for the image.

FIG. 3B is a diagram of a local trimap for a local region of an image and an exemplary method that can specify the local trimap and solve Poisson equations to provide a local matte for the local region.

FIG. 4 is a series of images and mattes for various conditions where such conditions may be used to refine a matte or a matting process.

FIG. 5 is an image with corresponding channels and corresponding mattes that demonstrate refinement or optimization via channel selection techniques.

FIG. 6 is a series of images with corresponding gradient mattes and alpha mattes that demonstrate refinement or optimization via boosting and highpass filtering.

FIG. 7 is a series of images with corresponding gradient mattes and alpha mattes that demonstrate refinement or optimization via diffusion filtering and cloning.

2

FIG. 8 is a series of images that help to demonstrate an exemplary process to handle multiple backgrounds in an image.

FIG. 9 is a foggy image and a de-fogged image that help to demonstrate an exemplary process to de-fog an image.

FIG. 10 is an image, a matte derived from exemplary Poisson matting and a matte derived from conventional matting for purposes of comparison.

FIG. 11 is a diagram of an exemplary computing environment, which may be used to implement various exemplary technologies described herein.

## DETAILED DESCRIPTION

As described herein, Poisson matting is applied to natural images, including those with complex scenes. Traditional techniques typically optimize a pixel's alpha, background and foreground colors in a statistical manner, in contrast, Poisson matting can operate directly on the gradient of a matte, which can reduce error caused by mis-classification of color samples. An exemplary method uses Poisson matting to estimate a gradient matte from an image and then reconstruct the matte by solving a set of Poisson equations. Various other exemplary techniques are also discussed.

An exemplary method for natural image matting includes solving Poisson equations with a matte gradient field. Such a method is, at times, referred to herein as Poisson matting. Such a method can generate a matte from a continuous matte gradient field by solving Poisson equations using boundary information, for example, from a user-supplied trimap (i.e., a three region map for an image). An exemplary method may include refinement of a matte gradient field using a number of tools (e.g., filtering, cloning, etc.), whereby a user can further improve Poisson matting results. Further, a modified local result may be seamlessly integrated into a final global result. Various examples are presented using complex natural images to demonstrate the quality of matting results through use of Poisson matting. Poisson matting is optionally used with other matting techniques, for example, Bayesian matting.

The discussion that follows includes various equations for purposes of illustrating how the Poisson equation may be applied to a pulling of matte problem or to matte refinement. The Poisson equation is a second-order partial differential equation (e.g., including a term of the form  $\Delta\Phi$ , where  $\Delta$  is the Laplacian operator or the vector Laplacian,  $\nabla^2$ , may be included). Various exemplary techniques may use variants of the Poisson equation or, for example, use equations that include a second-order partial differential term for an alpha matte.

For a color image, the foreground F and the background B can be specified as color components together with an alpha channel matte, for example, RGB:

$$\begin{Bmatrix} \alpha \\ F_r & F_g & F_b \\ B_r & B_g & B_b \end{Bmatrix}$$

An alpha channel has various uses, including, for example, masking objects, making them transparent, or adding specific color instructions. In the  $\{\alpha, F, B\}$  matrix, the alpha channel is a matte that distinguishes the foreground and background in an RGB image. As described herein, a user may desire con-

3

structuring such a matrix for an image through a process referred to as matting, which aims to find an appropriate  $\alpha$  and  $F$ .

Matting is inherently under-constrained because the matting equation has too many unknowns. Therefore, user interaction is often required to obtain good mattes. For example, in natural image matting, a user may be required to supply a trimap that partitions the image into three regions: “definitely foreground”, “definitely background” and “unknown region”.

Given an alpha matte, in image composition, a new image  $I(x, y)$  can be blended from a background image  $B(x, y)$  and a foreground image  $F(x, y)$  using the alpha matte  $\alpha(x, y)$ . A matting equation ( $(x, y)$  arguments deleted for clarity) may be specified as follows:

$$I = \alpha F + (1 - \alpha) B \quad (1)$$

As already mentioned, separation of  $\alpha$ ,  $F$  and  $B$  from a given image  $I$  is called the pulling of matte problem, or simply matting. In blue screen matting,  $\alpha$  and  $F$  are generally reconstructed where  $B$  is known from a user-controlled environment. In contrast, for natural image matting, all variables  $\alpha$ ,  $F$  and  $B$  need to be determined. Ease of such a determination depends on complexity of the image and the desired quality of the result. Where the highest quality result is desired, many have resorted to tedious pixel-by-pixel editing. Various exemplary techniques described herein aim to reduce or eliminate a need for such editing.

FIG. 1 shows an image **100**, an alpha matte **101** and a foreground only image **102** with a blue background. As mentioned, the process of generating the alpha matte is referred to as “pulling of matte”. Various exemplary techniques described herein are directed to this process. The image **100** is a natural image that includes a koala as a foreground object against a complex color background. To use this koala with a different background, a user needs to extract the koala from the image **100**. The fur extending from the ears of the koala complicate the process. In particular, the foreground hairs and the background branches are easily confused, especially in regions of low contrast. Various exemplary Poisson matting techniques can be used to generate a high quality matte for use in extracting the koala from the image **100**. The extracted image of the koala can then be used, for example, to form a composite image.

Various exemplary techniques described herein rely on one or more assumptions. For example, an initial assumption can be that intensity change in the foreground and background of an image gradient is smooth. Given this assumption and a trimap for the image, an exemplary method uses global Poisson matting to approximate a matte from an image gradient. Accordingly, foreground and background colors can be robustly estimated.

In instances where global Poisson matting fails to produce high quality mattes, for example, due to a complex background, an exemplary technique uses local Poisson matting, which can be used to manipulate a continuous gradient field in a local region.

Local Poisson matting optionally relies on user input or interaction into a “pulling the matte” loop. In most cases, image gradients caused by foreground and background colors are visually distinguishable locally. Knowledge from a user can be integrated into Poisson matting using, for example, a set of tools that can operate on the gradient field of the matte.

Local Poisson matting can maintain continuities of thin long threadlike shapes of foreground objects in a complex scene, such as that of the image **100** of FIG. 1. Moreover, after

4

local operations, modifications in a gradient field can be seamlessly propagated into a global matte.

FIG. 2 shows an exemplary matting engine and an associated method **200**. The exemplary matting engine **210** includes a global matting component **212** and a local matting component **214** along with various other components. The other components include components for one or more local operations **220**. In the example of FIG. 2, the local operations **220** include a channel selection component **222** and a local filtering component **224**. The local filtering component **224** provides for one or more operations such as boosting, highpass filtering, diffusion filtering, cloning, etc., some of which are described in detail further below.

The exemplary matting engine **210** operates to receive an image **202** and to generate a matte **230**. Again, the matte **230** may be an alpha matte that allows for extracting an object or foreground from the image **202**. The exemplary matting engine **210** typically allows for iterative operation, for example, where a user may examine the matte **230** and, in turn, use one or more local operations to refine or otherwise increase the quality of the matte **230**. Such operations may require recalculation of the matte **230** using the global or local matting components **212**, **214**.

An exemplary method for matting **250** also appears in FIG. 2. The exemplary method **250** may rely on the exemplary matting engine **210** or one or more components included therein. According to the exemplary method **250**, a reception block **254** acts to receive an image or information about an image. A global matting block **258** uses the image or image information to formulate and solve a set of Poisson equations to thereby provide a global matte.

After the global Poisson matting operation **258**, the method **250** enters a local matting block **260** that uses information from the global matting operation **258** together with information about a local region of the received image to generate a local matting solution by solving a set of Poisson equation with boundary conditions pertaining to the local region. This local operation may be repeated one or more times for the same, overlapping or different local regions of the received image.

A decision block **262** decides if the matte result produced using global Poisson matting and local Poisson matting is acceptable. If the matte is acceptable (i.e., OK), then the method **250** terminates in an end block **270**. However, if the matte is unacceptable (i.e., not OK), then the method **250** continues in a local operations block **266** where one or more local operations are used to refine the matte. After applying the one or more local operations, in this example, the method **250** returns to the local Poisson matting block **260**.

As already mentioned, a result from local Poisson matting can be incorporated into a global result. Further, a plurality of local results may be incorporated into a global result.

Details and examples follow whereby Poisson matting and related techniques are used for matting. For example, a technique is mentioned for use in solving a set of Poisson equations with associated boundary conditions. Further, various local operations are mentioned. Again, such examples are given to demonstrate the exemplary techniques as other solvers and other local operations may be used, as appropriate.

An exemplary technique uses Poisson matting where an approximate gradient field of matte is computed from an input image and then a resulting matte is obtained from its gradient field by solving Poisson equations.

A general relationship between a matte ( $\alpha$ ) and a matte gradient ( $g$ ) may be specified depending on the whether one wishes to derive a matte ( $\alpha$ ) from a matte gradient ( $g$ ) or vice versa. For example,  $g = -\nabla\alpha$  or  $\Delta\alpha = \text{div}(g)$  where  $\nabla = (\partial/\partial x,$

5

$\partial/\partial y$ ) is the gradient operator,  $\Delta=(\partial^2/\partial x^2+\partial^2/\partial y^2)$  is the Laplacian operator and  $\text{div}=(\partial g_x/\partial x+\partial g_y/\partial y)$  is the divergence operator. The equation for deriving a matte ( $\alpha$ ) from a matte gradient ( $g$ ) is in the form of a Poisson equation.

Various boundary conditions may be specified for a Poisson equation, where the surface vector ( $ds$ ) is directed outwardly from a region  $\Omega$ . For example, a Dirichlet boundary condition may specify a value for  $\alpha$  at the boundary  $\partial\Omega$ ; whereas a Neumann boundary condition may specify a value for the derivative of  $\alpha$  with respect to the surface vector ( $ds$ ). Other boundary conditions may be used as appropriate or a combination of boundary values (e.g., Dirichlet, Neumann, Cauchy, etc.).

FIG. 3A shows an exemplary trimap image **300** that corresponds to the image **100** of FIG. 1 and an exemplary method **310** for global Poisson matting. The image **300** shows various regions and boundary conditions for use in Poisson matting (e.g., global or local). The image **300** of FIG. 3A shows the trimap  $\{\Omega_F, \Omega_B, \Omega\}$  as, for example, specified by a user, where  $\partial\Omega$  is the exterior boundary of unknown region  $\Omega$ . Various outward normal vectors  $ds$  are shown for the various regions including  $ds(\Omega_B)$ ,  $ds(\Omega_F)$  and  $ds(\Omega)$ . Such an example may be used for global Poisson matting.

The exemplary method **310** includes a reception block **312** where a matting engine receives an image. An operation block **316** follows that divides the image into a three regions: a background region, a foreground region and an unknown region. Such an operation block may specifying a background region, a foreground region and an unknown region wherein a boundary exists between the foreground region and the unknown region and wherein another boundary exists between the unknown region and the background region. A solution block **320** solves a set of Poisson equations having boundary conditions for the two boundaries to provide a matte that distinguishes a foreground region from a background region in the unknown region.

FIG. 3B shows the exemplary trimap image **300** with an additional region  $\Omega_L$ , which suitable for use in exemplary local Poisson matting, as described below, where selection of a local region  $\Omega_L$  occurs (e.g., interactively by a user, automatically, etc.) and where  $\partial\Omega$  is the exterior boundary of local unknown region  $\Omega \cap \Omega_L$ . FIG. 3B also shows outward normal vectors  $ds(\Omega_L)$  for the local region where it boundaries extend between the foreground region  $\Omega_F$  and the background region  $\Omega_B$ .

Yet further, FIG. 3B shows an exemplary method **350** for local Poisson matting. The exemplary method **350** includes a reception block **352** that receives a matte, for example, from the solution block **320** as provided by global Poisson matting. An operation block **356** follows that specifies a local unknown region wherein a boundary exists between a foreground region and the local unknown region and wherein another boundary exists between the local unknown region and a background region. A solution block **350** solves a set of Poisson equations having boundary conditions for the two boundaries to provide a matte that distinguishes a foreground region from a background region in the local unknown region.

As described herein, various exemplary techniques use gradient manipulation. Gradient manipulation may occur locally or globally. For Poisson matting, a differential matting equation can be used, depending on various conditions or assumptions. In order to get an approximate gradient field of matte and, hence, a differential matting equation, one takes the partial derivatives of both sides of the matting equation, which results in Equation 2:

$$\nabla I = (F-B)\nabla\alpha + \alpha\nabla F + (1-\alpha)\nabla B \quad (2)$$

6

This is the differential form of the matting equation. For color images or other multi-component images, channels, etc., may be specified (e.g.,  $F_r$ ,  $F_g$  and  $F_b$ , etc.).

Various assumptions may be made or conditions satisfied that allow for simplification of the differential matting equation. For example, in situations where foreground  $F$  and background  $B$  are smooth (i.e.,  $\alpha\nabla F + (1-\alpha)\nabla B$  is relatively small with respect to  $(F-B)\nabla\alpha$ ), an approximate matte gradient field may be specified as follows:

$$\nabla\alpha \approx (F-B)^{-1}\nabla I \quad (3)$$

Thus, according to Equation 3, the matte gradient is proportional to the image gradient. Others have used an approximate equation of such form for other purposes that included estimation of opacity around the boundaries of a solid object through integration of the gradient of matte along a 1D path perpendicular to the boundary of the object. Various exemplary techniques described herein use such an approximation to reconstruct a matte more efficiently through solving Poisson equations in a 2D image space directly.

Referring again to the image **300** of FIG. 3A,  $\Omega_F$ ,  $\Omega_B$  and  $\Omega$  can be defined as “definitely foreground”, “definitely background” and “unknown” regions of an image  $I$ , respectively. For each pixel  $p=(x, y)$  in the image (see, e.g., the image **100**),  $I_p$  is its intensity and  $F_p$  and  $B_p$  are the foreground and background intensity, respectively. According to an exemplary global matting approach,  $N_p$  is defined as the set of its four neighbors. Other approaches may be used as well. According to the exemplary approach, the exterior boundary of the unknown region  $\Omega$  is specified as  $\partial\Omega = \{p \in \Omega_F \cup \Omega_B \mid N_p \cap \Omega \neq \emptyset\}$ .

To recover the matte in the unknown region  $\Omega$  given an approximate  $(F-B)$  and image gradient  $\nabla I$  involves minimization of the following variational problem:

$$\alpha^* = \arg \min_{\alpha} \int \int_{p \in \Omega} \left\| \nabla \alpha_p - \frac{1}{F_p - B_p} \nabla I_p \right\|^2 dp \quad (4)$$

with Dirichlet boundary condition  $\alpha|_{\partial\Omega} = \hat{\alpha}|_{\partial\Omega}$ . These conditions are specified as follows:

$$\hat{\alpha}_p|_{\partial\Omega} = 1 \quad p \in \Omega_F; \quad 0 \quad p \in \Omega_B \quad (5)$$

Such a definition is consistent with a user-supplied trimap. The associated set of Poisson equations with the same boundary condition is as follows:

$$\Delta\alpha = \text{div}(\nabla I (F-B)^{-1}) \quad (6)$$

Obtaining the unique solution of Poisson equations is a well studied problem. For example, various examples presented herein included use of the Gauss-Seidel iteration with overrelaxation method to provide solutions. In such examples, for color images, both  $(F-B)$  and  $\nabla I$  were measured in the grayscale channel.

An exemplary technique uses iterative optimization for global Poisson matting. A particular technique involves:

1.  $(F-B)$  initialization. Absolute values of  $F$  and  $B$  are not necessary, since  $(F-B)$  provides enough information to determine the matte. Initially, for each pixel  $p$  in  $\Omega$ ,  $F_p$  and  $B_p$  are approximated by corresponding the nearest foreground pixel in  $\Omega_F$  and background pixel in  $\Omega_B$ . Then, the constructed  $(F-B)$  image is smoothed by a Gaussian filter to suppress significant changes due to noise and inaccurate estimation of  $F$  and  $B$ .
2.  $\alpha$  reconstruction.  $\alpha$  is reconstructed by solving Poisson equations (6) using the current  $(F-B)$  and  $\nabla I$ .

7

3. F, B refinement occurs, for example, by letting  $\Omega_F^+ = \{p \in \Omega | \alpha_p > 0.95, I_p \approx F_p\}$ . The condition  $\alpha_p > 0.95$  and  $I_p \approx F_p$  guarantees that the pixels in  $\Omega_F^+$  are mostly foreground. Similarly, such refinement lets  $\Omega_B^+ = \{p \in \Omega | \alpha_p < 0.05, I_p \approx B_p\}$ . Here,  $F_p$ ,  $B_p$  and  $I_p$  represent the color vectors at pixel  $p$ . In this example, update of  $F_p$  and  $B_p$  occurs according to the color of the nearest pixels in  $\Omega_F \cup \Omega_F^+$  and in  $\Omega_B \cup \Omega_B^+$ , respectively. Also, in this example, a Gaussian filter is applied to smooth (F-B).

According to this exemplary technique, iteration occurs for the above steps 2 and 3 until change in the matting results is sufficiently small or, for example, both  $\Omega_F^+$  and  $\Omega_B^+$  are empty in step 3. For many images, only a few iterations are typically needed. For each iteration, the selection of  $\Omega_F^+$  and  $\Omega_B^+$  has little associated error, which acts to guarantee that more accurate colors in these two regions are further propagated into less accurate neighboring pixels.

Global Poisson matting works well in scenes with a smooth foreground and background. However, for a complex image, Equation 3 may not be a good approximation of the matte gradient globally, where the background and foreground gradients cannot be ignored. Thus, as described herein, an exemplary technique can use local Poisson matting, for example, to locally refine the global Poisson matting result.

Equation (2) can be rewritten as:

$$\nabla \alpha = A(\nabla I - D) \quad (7)$$

where  $A = (F-B)^{-1}$  and  $D = [\alpha \nabla F + (1-\alpha) \nabla B]$ .  $A$  affects the matte gradient scale in that increasing  $A$  would sharpen boundaries (i.e., decreasing  $F-B$ ).  $D$  is a gradient field caused by the background and foreground. Hence, estimation of  $A$  and  $D$  allows one to approach the ground truth,  $A^*$  and  $D^*$ .

In an exemplary global Poisson matting process,  $A$  is automatically estimated from the image and  $D$  is assumed to be zero. When the background or foreground has strong gradients, global Poisson matting may require attention to produce a desired result.

FIG. 4 shows various exemplary processes 400 as applied to an image 410 and an image 430. The series of results 412, 414, 416 for image 410 pertains to  $A$  while the series of results 432, 434, 436 for image 430 pertains to  $D$ . These series demonstrate that resulting mattes solved by Poisson matting when  $A$  and  $D$  approximate  $A^*$  and  $D^*$  differently. The result 412 is for  $A \approx A^*$ , which is a result that quite accurately represents the image 410. The result 414 is for  $A < A^*$ , which is a result that exhibits smoothing (i.e., a smooth matte) of the image 410. The result 416 is for  $A > A^*$ , which is a result that exhibits sharpening (i.e., a sharp matte) of the image. Similarly, the most accurate matte for the image 430 occurs when  $|D| \approx |D^*|$ , the result 432. Of course, where certain effects are desirable,  $|D| < |D^*|$  or  $|D| > |D^*|$  may be used (see corresponding results 434, 436).

An exemplary process for refining a result of global Poisson matting includes local Poisson matting. For example, a user can specify a region  $\Omega_L$  for refinement or enhancement and then apply local Poisson matting. Referring to the image I 300 of FIG. 3B, for a local integral region  $\Omega_L$ , a corresponding boundary exists:  $\partial\Omega = \{p \in (\Omega_L \cap \Omega) | N_p \cap (\Omega_L \cap \Omega) \neq \emptyset\}$ . Thus, the image I 300 of FIG. 3B illustrates a manner by which a selection of  $\Omega_L$  can occur along with a corresponding boundary  $\partial\Omega$  that, in this example, includes portions of the aforementioned global boundary (see, e.g., image 300 of FIG. 3A). The variational problem to be minimized in local Poisson matting is given by:

8

$$\alpha^* = \arg \min_{\alpha} \int \int_{p \in \Omega_L \cap \Omega} \|\nabla \alpha_p - A_p(\nabla I_p - D_p)\|^2 dp. \quad (8)$$

with Dirichlet boundary condition  $\alpha|_{\partial\Omega} = \hat{\alpha}|_{\partial\Omega}$ . The local Dirichlet boundary condition  $\hat{\alpha}|_{\partial\Omega}$  is defined as:

$$\hat{\alpha}_p|_{\partial\Omega} = 1 \quad p \in \Omega_F; \quad 0 \quad p \in \Omega_B; \quad \alpha_g \quad p \in \Omega \quad (9)$$

where  $\alpha_g$  is the current matte value in an unknown region on the local boundary.

In the example image 300, which corresponds to the image 100 of FIG. 1, the local region size is fewer than  $200 \times 200$  pixels. Time to solve the local problem normally depends on the size of the local region. In instances where a local Poisson matting operation follows a global Poisson matting operation, because of existing boundary conditions, the local operation can be seamlessly propagated into the matte in a manner where boundary discontinuity is minimal.

An exemplary method allows for modification of  $A$  or  $D$  in a local region. For example, a user can modify  $A$  or  $D$  in a selected local region in an effort to produce a better approximation of  $\nabla \alpha$ . Further, two exemplary operations are optionally provided for such modification: channel selection and local filtering. Channel selection aims to reduce error associated with  $D$  whereas local filtering involves manipulation of  $A$  and  $D$  directly. Use of such operations can avoid a need to optimize a matte in a pixel-wise manner, and thereby allow for increased efficiency. Further, such operations may speed calculation of results.

FIG. 5 shows various exemplary processes related to channel selection. An image 510 includes local regions 512 and 514. In an exemplary channel selection process, a user may select a local region for refinement, for example, consider the local region 514. The local region 514 includes various background colors that may appear elsewhere in the image 510. As such, a user may select samples from a closely matching "blue" region of the image 510 (see the local region 512, which is green in color, yet may be considered "blue" as it is a background region). An enlarged grayscale image 524 and a corresponding optimized channel image 528 of the local region 514 indicate portions of the boundary  $\partial\Omega$ , which is shown in solid line on the left side of the image along the boundary of the unknown local region  $\Omega_L$  and the known, "definitely background" region  $\Omega_B$  while a dashed line along the boundary of the known, "definitely foreground" region  $\Omega_F$  and the unknown local region  $\Omega_L$ . Alpha mattes 534, 538 are computed from grayscale 524 and the optimized channel 528, respectively. The matte 538 generated from the optimized channel 528 is clearer when compared to the matte generated from the grayscale 524.

For color images, Equation (3) can be measured in different channels (e.g., any single R/G/B or grayscale channel). In various examples described herein, for global Poisson matting, the grayscale channel was used,  $\nabla \alpha = A_g(\nabla I_g - D_g)$ .

In general, the smooth background or foreground assumption makes  $|D_g|$  small such that  $A_g \nabla I_g$  is a typically good approximation of  $\nabla \alpha$ . Similarly, in a local region, an exemplary process constructs a new channel  $\gamma = aR + bG + cB$  with a smooth background or foreground in which  $|D_\gamma|$  is smaller than  $|D_g|$ . Thus, such an exemplary process may minimize the variance of the foreground or background colors, and the new channel  $\gamma$  as follows:

1. A user selects either background or foreground color samples  $\{(R_i, G_i, B_i)\}_{i=1}^N$  in an image using, for example, a

simple brush. Such a process is optionally automated in a manner that reduces user input.

2. Computation of weights (a b c) occurs to minimize sample variances  $\sum_i^N (\gamma_i - \gamma)^2$  in the new channel, which poses a linearly constrained quadratic optimization problem:

$$\min_{a,b,c} \sum_i [(a b c) \cdot (R_i G_i B_i)^T - (a b c) \cdot (\bar{R} \bar{G} \bar{B})^T]^2 \text{ s.t. } a + b + c = 1 \quad (10)$$

where (R G B) is the mean color value of the samples. The weights (a b c) are obtained by solving an augmented linear system. Such an exemplary process was used to produce the improved optimized channel matte **538** of FIG. **5**. In this example, error associated with D is reduced and the hair shape of the local region **514** is better recovered. Consequently, information from such a process may be applied to other regions.

As already mentioned, filtering may be used to refine or otherwise improve results. Filtering can operate directly on A and D. Local filters can be used to manipulate a matte gradient field. Described herein are various exemplary filter operations, referred to as a boosting brush, a highpass filter, a diffusion filter and a clone brush.

An exemplary boosting brush filter operation can be used, for example, when a matting result is smoother or sharper than what user may expect. In particular, such a boosting brush can be used to increase or decrease A directly (e.g.,  $A = (F - B)^{-1}$ ). Image series **610** of FIG. **6** includes use of a boosting brush that has a local Gaussian shape for each pixel p in a given brush area where  $A_p$  is modified to  $A'_p$  using the boosting brush operation:

$$A'_p = \left[ 1 + \lambda \exp\left(-\frac{\|p - p_0\|^2}{2\sigma^2}\right) \right] \cdot A_p \quad (11)$$

where  $p_0$  is the coordinate of the brush center,  $\sigma$  and  $\lambda$  are user defined parameters to control the size and strength of the boosting effect. Hence, the user can boost the whole or partial region by using brushes of various sizes. If  $\lambda > 0$ , this filter will increase A.

With respect to the series **610** of FIG. **6**, the top image is an input image **611**, the next is a matte gradient **612** prior to application of the brush operation, and the next is a matte gradient **613** after application of the brush operation. The lower two images are of alpha mattes **614**, **615** that correspond to the matte gradients **612**, **613**, respectively. The result generated through use of the exemplary brush operation is of higher quality. In particular, more contiguous hair strands can be distinguished as a smooth alpha matte is sharpened after applying the boosting brush.

An exemplary process optionally includes highpass filtering. For example, a channel selection operation can generate a smooth background or foreground, leading to low frequency background or foreground gradients. In such an example, D can be estimated using the low-frequency part of the image gradient:

$$D = K * \nabla I$$

where  $K = N(p; p_0, \sigma^2)$  is a Gaussian filter centered at pixel  $p_0$  and \* is the convolution operator. From Equation (7),  $\nabla \alpha = A(\nabla I - K * \nabla I)$ , where  $(\nabla I - K * \nabla I)$  corresponds to a highpass fil-

ter. The series **620** of FIG. **6** demonstrates that a clear alpha matte structure is recovered after applying highpass filtering.

With respect to the series **620** of FIG. **6**, the top image is an input image **621**, the next is a matte gradient **622** prior to application of the highpass operation, and the next is a matte gradient **623** after application of the highpass operation. The lower two images are of alpha mattes **624**, **625** that correspond to the matte gradients **622**, **623**, respectively. The result generated through use of the exemplary highpass operation is of higher quality.

An exemplary process optionally includes diffusion filtering. On the boundary of a solid object where alpha matte changes quickly, AVI generally provides a good approximation; however, the image gradient  $\nabla I$  is sensitive to noise and blocking effects that may be present in, for example, JPEG images. In the example series **730** of FIG. **7**, anisotropic diffusion was used to diffuse an image **731** that included background noise. The background noise in the image **731** exists in the matte **732** and carries over to the alpha matte **734**. In this example, the applied diffusion operation was an edge-preserving blurring process that aimed to remove such small scale noise. Accordingly, an image gradient  $\nabla I$  was re-computed from a diffused image (not shown). The gradient matte **733** exhibits less small scale noise than the gradient matte **732**. In addition, the alpha matte **735** has less small scale noise when compared to the alpha matte **734**. Thus, the exemplary diffusion process acts to suppress noise, which, in turn, can produce a better matte result.

An exemplary process optionally includes cloning, for example, using a clone brush. Such a clone brush can copy a matte gradient from a local region to another region. In the series **740** of FIG. **7**, a lower box represents a selected local region while an upper box represents a region to which clone information is applied, i.e., information from the lower box is applied (e.g., cloned or pasted) to the region of the upper box.

According to an exemplary clone technique, in some situations, cloning can be used to directly copy a matte gradient  $A(\nabla I - D)$  from a source region to a target region. In the series **740** of FIG. **7**, cloning is applied to a region (upper box of gradient matte **742**) where foreground and background are, to the eye, fairly indistinguishable. The resulting gradient matte **743** and alpha matte **745** exhibit more detail and less blur.

Other exemplary processes for enhancing images or mattes include an erase brush for erasing that can, for example, remove unwanted alpha matte regions directly; and an inverse brush that can inverse an incorrect sign of a matte gradient.

As described above, various enhancement or refinement processes may be used to arrive at a suitable result. For example, with various aforementioned local operations, a user can refine a matte in a selected region. An exemplary process is based on a global Poisson matting result and uses local Poisson matting as follows:

1. Apply channel selection to reduce the errors in D. For solid object boundaries, apply the diffusion filter to remove possible noise;
2. Apply the highpass filtering to obtain an approximation of D;
3. Apply the boosting brush to manipulate A; and
4. Optionally apply the clone brush if gradients are indistinguishable.

The aforementioned, erase brush and inverse brush can be optionally applied in any step. At each step, local Poisson matting can typically generate results very quickly (e.g., depending on resources and local region size).

An exemplary GUI utility provides a user with an option to observe the matting result and select any remaining unsatisfactory regions for further refinement.

## 11

An exemplary process can be applied to matting with multiple backgrounds. FIG. 8 shows various images **801-806** as pertaining to an exemplary process **800**. An exemplary process lets  $\{I_t\}_{t=1}^T$  be images of the same foreground  $F$  with multiple different backgrounds  $\{B_t\}_{t=1}^T$ . The exemplary process **800** may calculate the mean image without any information about backgrounds, as follows:

$$\bar{I} = \frac{1}{T} \sum_t (\alpha F + (1 - \alpha) B_t) = \alpha F + (1 - \alpha) \bar{B} \quad (12)$$

where

$$\bar{B} = \frac{1}{T} \sum_t B_t$$

is the mean background. In general,  $\bar{B}$  is a smoothed image for all backgrounds in  $\{B_t\}_{t=1}^T$ . The exemplary process **800** applies Poisson matting to the mean image as it may perform better than in any individual image in  $\{I_t\}_{t=1}^T$ . In the series of images **801-806**, global Poisson matting is used, followed by local Poisson matting for a region at the lower right part of the image. The top row of this series shows three input images **801, 802, 803** with different complex backgrounds; whereas, the bottom row shows the mean of all eight input images **804**, the computed alpha matte **805** and a composite image using Poisson matting **806**.

An exemplary process can be applied to de-fog an image. FIG. 9 shows an image **901** and a de-fogged image **902** according to an exemplary process **900**. In this example, the de-fogged image **902** is produced using the aforementioned boosting brush with several local operations.

A fog model can be represented as a matting equation:

$$I = I_c \cdot e^{-\beta d} + \text{Fog} \cdot (1 - e^{-\beta d}) \quad (13)$$

where Fog is the color of fog,  $I_c$  is the clear image without fog,  $\beta$  is the scattering coefficient of the atmosphere and  $d$  is the depth value. According to the exemplary process **900**, local assignment of information produces acceptable results. Consider taking the partial derivatives of (13) to obtain  $\nabla I_c = \nabla I \cdot e^{\beta d}$  with respect to assigned depth  $d$ . The aforementioned boosting brush is applied to locally modify  $e^{\beta d}$  in the selected region to fine tune the defogged image gradient. By solving Poisson equations, any modification to the image can be automatically and seamlessly propagated to generate the de-fogged image without any visible boundaries.

FIG. 10 shows a comparison **1000** of an exemplary Poisson technique **1020** to a traditional Bayesian technique **1010**. An image **1001** is selected and the two techniques applied. The result **1011** of the Bayesian technique **1010** includes discrete regions that do not accurately represent the fine hair of the girl in the image **1001**. In contrast, the result **1022** of the Poisson technique **1020** provides a more suitable representation of her hair.

The result **1022** relies on an exemplary local Poisson matting process. Most images are very complex not only in foreground and background colors, but also in their gradient fields. Therefore, in this example, Bayesian matting, which relies on sampling color pixels, does not perform as well.

A close inspection of input images and matting results, indicates that Bayesian matting fails in places where fore-

## 12

ground and background colors are similar, or their colors have large change so that correct samples are buried in the local region. However, Bayesian matting can have some advantages for certain natural images. An exemplary method optionally includes use of Poisson matting and Bayesian matting.

As discussed herein, various exemplary digital matting methods include use of Poisson equations or what is referred to as Poisson matting. By solving Poisson equations, Poisson matting can reconstruct a faithful matte from its approximated gradient field estimated from an input image.

#### Exemplary Computing Environment

The various exemplary technologies may be implemented in different computer environments. For example, various exemplary methods are typically computer-implementable. The computer environment shown in FIG. 11 is only one example of a computer environment and is not intended to suggest any limitation as to the scope of use or functionality of the computer and network architectures suitable for use. Neither should the computer environment be interpreted as having any dependency or requirement relating to any one or combination of components illustrated in the example computer environment.

FIG. 11 illustrates an example of a suitable computing system environment **1100** on which various exemplary methods may be implemented. Various exemplary devices or systems may include any of the features of the exemplary environment **1100**. The computing system environment **1100** is only one example of a suitable computing environment and is not intended to suggest any limitation as to the scope of use or functionality of the invention. Neither should the computing environment **1100** be interpreted as having any dependency or requirement relating to any one or combination of components illustrated in the exemplary operating environment **1100**.

Various exemplary methods are operational with numerous other general purpose or special purpose computing system environments or configurations. Examples of well known computing systems, environments, and/or configurations that may be suitable for implementation or use include, but are not limited to, personal computers, server computers, hand-held or laptop devices, multiprocessor systems, microprocessor-based systems, set top boxes, programmable consumer electronics, network PCs, minicomputers, mainframe computers, distributed computing environments that include any of the above systems or devices, and the like.

Various exemplary methods, applications, etc., may be described in the general context of computer-executable instructions, such as program modules, being executed by a computer. Such instructions may be stored on one or more computer-readable media. Generally, program modules include routines, programs, objects, components, data structures, etc., that perform particular tasks or implement particular abstract data types. Various exemplary methods may also be practiced in distributed computing environments where tasks are performed by remote processing devices that are linked through a communications network or other communication (e.g., infrared, etc.). In a distributed computing environment, program modules may be located in both local and remote computer storage media including memory storage devices.

With reference to FIG. 11, an exemplary system for implementing the various exemplary methods includes a general purpose computing device in the form of a computer **1110**. Components of computer **1110** may include, but are not limited to, a processing unit **1120**, a system memory **1130**, and a

13

system bus **1121** that couples various system components including the system memory **1130** to the processing unit **1120**. The system bus **1121** may be any of several types of bus structures including a memory bus or memory controller, a peripheral bus, and a local bus using any of a variety of bus architectures. By way of example, and not limitation, such architectures include Industry Standard Architecture (ISA) bus, Micro Channel Architecture (MCA) bus, Enhanced ISA (EISA) bus, Video Electronics Standards Association (VESA) local bus, and Peripheral Component Interconnect (PCI) bus also known as Mezzanine bus.

Computer **1110** typically includes a variety of computer readable media. Computer readable media can be any available media that can be accessed by computer **1110** and includes both volatile and nonvolatile media, removable and non-removable media. By way of example, and not limitation, computer readable media may comprise computer storage media and communication media. Computer storage media includes both volatile and nonvolatile, removable and non-removable media implemented in any method or technology for storage of information such as computer readable instructions, data structures, program modules or other data. Computer storage media includes, but is not limited to, RAM, ROM, EEPROM, flash memory or other memory technology, CD-ROM, digital versatile disks (DVD) or other optical disk storage, magnetic cassettes, magnetic tape, magnetic disk storage or other magnetic storage devices, or any other medium which can be used to store the desired information and which can be accessed by computer **1110**. Communication media typically embodies computer readable instructions, data structures, program modules or other data in a modulated data signal such as a carrier wave or other transport mechanism and includes any information delivery media. The term "modulated data signal" means a signal that has one or more of its characteristics set or changed in such a manner as to encode information in the signal. By way of example, and not limitation, communication media includes wired media such as a wired network or direct-wired connection, and wireless media such as acoustic, RF, infrared and other wireless media. Combinations of any of the above should also be included within the scope of computer readable media.

The system memory **1130** includes computer storage media in the form of volatile and/or nonvolatile memory such as read only memory (ROM) **1131** and random access memory (RAM) **1132**. A basic input/output system **1133** (BIOS), containing the basic routines that help to transfer information between elements within computer **1110**, such as during start-up, is typically stored in ROM **1131**. RAM **1132** typically contains data and/or program modules that are immediately accessible to and/or presently being operated on by processing unit **1120**. By way of example, and not limitation, FIG. **11** illustrates operating system **1134**, application programs **1135**, other program modules **1136**, and program data **1137**.

The computer **1110** may also include other removable/non-removable, volatile/nonvolatile computer storage media. By way of example only, FIG. **11** illustrates a hard disk drive **1141** that reads from or writes to non-removable, nonvolatile magnetic media, a magnetic disk drive **1151** that reads from or writes to a removable, nonvolatile magnetic disk **1152**, and an optical disk drive **1155** that reads from or writes to a removable, nonvolatile optical disk **1156** such as a CD ROM or other optical media (e.g., DVD, etc.). Other removable/non-removable, volatile/nonvolatile computer storage media that can be used in the exemplary operating environment include, but are not limited to, magnetic tape cassettes, flash memory cards, digital versatile disks, digital video tape, solid

14

state RAM, solid state ROM, and the like. The hard disk drive **1141** is typically connected to the system bus **1121** through a data media interface such as interface **1140**, and magnetic disk drive **1151** and optical disk drive **1155** are typically connected to the system bus **1121** a data media interface that is optionally a removable memory interface. For purposes of explanation of the particular example, the magnetic disk drive **1151** and the optical disk drive use the data media interface **1140**.

The drives and their associated computer storage media discussed above and illustrated in FIG. **11**, provide storage of computer readable instructions, data structures, program modules and other data for the computer **1110**. In FIG. **11**, for example, hard disk drive **1141** is illustrated as storing operating system **1144**, application programs **1145**, other program modules **1146**, and program data **1147**. Note that these components can either be the same as or different from operating system **1134**, application programs **1135**, other program modules **1136**, and program data **1137**. Operating system **1144**, application programs **1145**, other program modules **1146**, and program data **1147** are given different numbers here to illustrate that, at a minimum, they are different copies. A user may enter commands and information into the computer **1110** through input devices such as a keyboard **1162** and pointing device **1161**, commonly referred to as a mouse, trackball or touch pad. Other input devices (not shown) may include a microphone, joystick, game pad, satellite dish, scanner, or the like. These and other input devices are often connected to the processing unit **1120** through a user input interface **1160** that is coupled to the system bus **1121**, but may be connected by other interface and bus structures, such as a parallel port, game port or a universal serial bus (USB). A monitor **1191** or other type of display device is also connected to the system bus **621** via an interface, such as a video interface **1190**. In addition to the monitor **1191**, computers may also include other peripheral output devices such as speakers and printer, which may be connected through an output peripheral interface **1195**.

The computer **1110** may operate in a networked environment using logical connections to one or more remote computers, such as a remote computer **1180**. The remote computer **1180** may be a personal computer, a server, a router, a network PC, a peer device or other common network node, and typically includes many or all of the features described above relative to the computer **1110**. The logical connections depicted in FIG. **11** include a local area network (LAN) **1171** and a wide area network (WAN) **1173**, but may also include other networks. Such networking environments are commonplace in offices, enterprise-wide computer networks, intranets and the Internet.

When used in a LAN networking environment, the computer **1110** is connected to the LAN **1171** through a network interface or adapter **1170**. When used in a WAN networking environment, the computer **1110** typically includes a modem **1172** or other means for establishing communications over the WAN **1173**, such as the Internet. The modem **1172**, which may be internal or external, may be connected to the system bus **1121** via the user input interface **1160**, or other appropriate mechanism. In a networked environment, program modules depicted relative to the computer **1110**, or portions thereof, may be stored in a remote memory storage device. By way of example, and not limitation, FIG. **11** illustrates remote application programs **1185** as residing on the remote computer **1180** (e.g., in memory of the remote computer **1180**). It will be appreciated that the network connections shown are exemplary and other means of establishing a communications link between the computers may be used.

15

Although various exemplary methods, devices, systems, etc., have been described in language specific to structural features and/or methodological acts, it is to be understood that the subject matter defined in the appended claims is not necessarily limited to the specific features or acts described. Rather, the specific features and acts are disclosed as exemplary forms of implementing the claimed subject matter.

The invention claimed is:

1. A computer-implementable method comprising:  
specifying, by a computing device, a background region, a foreground region and an unknown region for an image wherein a boundary exists between the foreground region and the unknown region and wherein another boundary exists between the unknown region and the background region; and  
solving, by the computing device, a set of Poisson equations having boundary conditions for the two boundaries to provide a matte that distinguishes a foreground region from a background region in the unknown region.
2. The computer-implementable method of claim 1 further comprising:  
specifying a local unknown region wherein a boundary exists between a foreground region and the local unknown region and wherein another boundary exists between the local unknown region and a background region; and  
solving a set of Poisson equations having boundary conditions for the two local unknown region boundaries to provide a local matte that distinguishes a foreground region from a background region in the local unknown region.
3. The computer-implementable method of claim 2 further comprising incorporating the local matte into a global matte for the entire image.
4. The computer-implementable method of claim 2 further comprising repeating the specifying to specify different local region and solving a set of Poisson equations for the different local region.
5. The computer-implementable method of claim 2 further comprising filtering prior to the solving.
6. The computer-implementable method of claim 2 wherein the solving relies at least in part on a prior solution.
7. The computer-implementable method of claim 6 wherein the prior solution corresponds to a solution for the entire image.
8. The computer-implementable method of claim 6 wherein the prior solution corresponds to a solution for the local unknown region.
9. The computer-implementable method of claim 1 wherein the specifying includes receiving a trimap.
10. The computer-implementable method of claim 1 wherein the boundary conditions include a Dirichlet boundary condition.
11. The computer-implementable method of claim 1 wherein the boundary conditions include a Neumann boundary condition.

16

12. One or more computer storage media comprising processor executable instructions to perform the solving of claim 1.

13. A computer-implementable method comprising:  
receiving, by a computing device, a trimap for an image that specifies a background region, a foreground region and an unknown region for the image wherein a boundary exists between the foreground region and the unknown region and wherein another boundary exists between the unknown region and the background region;  
solving, by the computing device, a set of Poisson equations having boundary conditions for the two boundaries to provide a matte that distinguishes a foreground region from a background region in the unknown region; and  
refining, by the computing device, the matte by solving a set of Poisson equations for a local unknown region.
14. The computer-implementable method of claim 13 wherein the refining comprises:  
specifying a local unknown region wherein a boundary exists between a foreground region and the local unknown region and wherein another boundary exists between the local unknown region and a background region; and  
solving a set of Poisson equations having boundary conditions for the two local unknown region boundaries to provide a local matte that distinguishes a foreground region from a background region in the local unknown region.
15. The computer-implementable method of claim 13 wherein the refining comprises at least one operation selected from a group consisting of filtering and channel selection.
16. The computer-implementable method of claim 13 wherein the refining comprises at least one operation selected from a group consisting of boosting, highpass filtering, diffusion filtering and cloning.
17. One or more computer storage media comprising processor executable instructions to perform the solving and refining of claim 13.
18. A computer-implementable method comprising:  
specifying, by a computing device, a local unknown region for an alpha matte wherein a boundary exists between a foreground region and the local unknown region and wherein another boundary exists between the local unknown region and a background region; and  
solving, by the computing device, a set of Poisson equations having boundary conditions for the two boundaries of the local unknown region to provide a refined alpha matte that distinguishes a foreground region from a background region in the local unknown region.
19. The computer-implementable method of claim 18 further comprising filtering the alpha matte prior to the solving.
20. One or more computer storage media comprising processor executable instructions to perform the specifying and solving of claim 18.

\* \* \* \* \*